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The effect of material properties on the seismic performance of Arch Dams

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Abstract. The paper investigates the effect of material properties on the seismic performance of arch dam-reservoirfoundation interaction systems based on the Lagrangian approach using demand-capacity ratios. Type-5 arch dam is selected as a numerical application. The linear time history analyses of the arch dam-reservoir-foundation interaction system are carried out for different material properties. The foundation is taken into account as massless: behaviour of the reservoir is assumed to be linearly elastic, inviscid and irrotational. The north-south component of the Erzincan earthquake in 1992 is chosen as a ground motion. Dynamic equations of motions obtained from 3-D finite element modelling of the coupled system are solved by using the Newmark integration algorithm. The damage levels of the coupled system for the different material properties are demonstrated by using demand-capacity ratios and cumulative inelastic durations. The time histories and maximum values of the displacements and principal stresses, and performance curves, are obtained from linear analyses. It is clearly seen from the study that the different material properties affect the seismic behaviour of the dam.

1 Introduction

An arch dam, built to obtain energy, is a solid concrete hydraulic structure curved in plan and possibly in elevation, which transmits a large portion of the water pressure and other loads by means of thrust (arch action) to the abutment utilising the compressive strength of its material. Therefore, arch dams require sophisticated engineering knowledge in designing and construction. The possible failure of dams



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retaining large quantities of water presents a hazard for life and property during earthquakes. In addition, the structural damage to these structures can be a considerable economic loss for the government. Many studies have been done on the earthquake behaviour of arch dams by many researchers, past and present (Sevim et al., 2011a, b; Akköse et al., 2008, 2007; Oliveira and Faria, 2006; Alves and Hall, 2006; Shahkarami et al., 2004; Lotfi and Espander, 2004; USACE, 2003). The common aim of these studies is to provide the optimum arch dam system related to safety and economy. This means that the main gains are aimed at building dams safer, more economically and more useful. So, the selected or assumed material properties must be optimally safe and economical. Because material properties are the most important component of a dam for reliable design and construction.

It is known that the reservoir considerably affects the dynamic response of the dam during earthquakes. Three approaches are used to consider reservoir effects in the analyses: the Westergaard (Westergaard, 1933), Euler (Dungar, 1978) and Lagrangian (Wilson and Khalvati, 1983) approaches. In the Westergaard approach, a vibrated mass dispersion with the dam is considered. In this approach, the dam is rigid, the reservoir has constant depth and infinite extent in the upstream direction, the effect of the waves at the free surface is negligible, and the water is incompressible. In the Euler approach, the displacements are the variables in the structure; the pressures are the variables in the fluid. Since the variables in the fluid and structure are different in this approach, special interface equations are required to solve the coupled system. However, in the Lagrangian approach, the displacements are the variables in both the fluid and the structure. So there is no need for any extra interface equations in the Lagrangian approach. For that reason, compatibility and equilibrium are automatically satisfied at the nodes along the interfaces between fluid and structure.

The earthquake behaviour of arch dams must be evaluated using a 3-D model. The nonlinear procedures are required to assess the seismic damage level of concrete dams in earthquake-prone areas. However, it is generally known that nonlinear time history analysis of dam-reservoir-foundation systems demand too much memory and time on the computers. It is also possible to use linear procedures for qualitative estimating of the damage level of concrete arch dams subjected to earthquakes (Ghanaat, 2002; USACE, 2003). A linear earthquake analysis of a concrete dam subjected to strong ground motion gives peak tensile stresses greater than the dynamic tensile strength of concrete, so that nonlinear procedures are required to assess the seismic safety of concrete dams in earthquake-prone areas.

The main purpose of this study is to assess the seismic performance of arch dams including dam-reservoir-foundation interaction using demand-capacity ratios and cumulative inelastic durations obtained for different material properties. In this paper, firstly general literature review concerning seismic behaviour of arch dams is presented. Then the formulation of the Lagrangian approach and seismic damage criteria for arch dams are given. After that, a numerical example is presented with results of time history analyses applied for different material properties. And finally, conclusions inferred from the study are presented.

2 Finite element formulation of fluid-structure systems by Lagrangian approach

The formulation of the fluid system based on the Lagrangian approach is given according to references (Wilson and Khalvati, 1983; Calayır, 1994). In this approach, fluid is assumed to be linearly elastic, inviscid and irrotational. The equations of motion of the fluid system have a similar form with those of the structure system when the Lagrangian approach is considered in the formulations. To obtain the coupled equations of the fluid-structure system, the determination of the interface condition is required. Because the fluid is assumed to be inviscid, only the displacement in the normal direction to the interface is continuous at the interface of the system. Assuming that the positive face is the structure and the negative face is the fluid, the boundary condition at the fluid-structure interface is,

$$\boldsymbol{U}_{n}^{-} = \boldsymbol{U}_{n}^{+} \tag{1}$$

where U_n is the normal component of the interface displacement (Akkaş et al., 1979). Using the interface condition, the equations of motion of the coupled system-to-ground motion including damping effects are given by,

$$\mathbf{M}_{c}\ddot{\boldsymbol{U}}_{c} + \mathbf{C}_{c}\dot{\boldsymbol{U}}_{c} + \mathbf{K}_{c}\boldsymbol{U}_{c} = \boldsymbol{R}_{c}$$
⁽²⁾

in which \mathbf{M}_{c} , \mathbf{C}_{c} and \mathbf{K}_{c} are the mass, damping and stiffness matrices for the coupled system and U_{c} , \dot{U}_{c} , \ddot{U}_{c} and \mathbf{R}_{c} are the vectors of the displacements, velocities, accelerations and external loads of the coupled system, respectively.



Fig. 1. Performance curve for linear elastic analysis of arch dams (Ghanaat, 2002; USACE, 2003).

3 Damage criteria for Arch Dams

The earthquake performance of arch dams is evaluated in accordance with displacements, stresses, demand-capacity ratios (DCR) and the cumulative inelastic duration. DCR for arch dams is defined as the ratio of the calculated arch or cantilever stresses-to-tensile strength of the concrete used in the dam. The dam response to the maximum design earthquake is considered to be within the linear elastic range of behaviour with little or no possibility of damage if computed DCR values are less than or equal to 1. The dam is considered to exhibit a nonlinear response in the form of opening and closing of contraction joints and cracking of the horizontal joints (lift lines) and concrete if the estimated DCR values exceed 1. The level of nonlinear response or opening and cracking of concrete is considered acceptable if the DCR value < 2, overstressed region is limited to 20 percent of the dam surface area, and the cumulative inelastic duration falls below the performance curve given in Fig. 1 (Ghanaat, 2002; USACE, 2003). The maximum permitted DCR for linear analysis of concrete dams is 2. A demand-capacity ratio of 2 allows stresses up to twice the static tensile strength of the concrete or to the level of dynamic apparent tensile strength, as long as the overstressed region is less than 20 percent of the dam surface area. The cumulative duration beyond a certain level of DCR is obtained by multiplying the number of stress values exceeding that level by the time-step of the time history analysis. The cumulative inelastic duration in Fig. 1 refers to the total duration of all stress excursions beyond a certain level of demand-capacity ratio.



Fig. 2. The view in plan and vertical crown cross-section of Type-5 arch dam.



Fig. 3. Some views of the Type-5 arch dam-reservoir-foundation system.



Fig. 4. Finite element model of downstream face of the dam.

4 Numerical example

A double curvature Type-5 arch dam, which was suggested in "Arch Dams" symposium in England in 1968, is selected as a numerical example (Arch Dams, 1968). The geometric properties of the Type-5 arch dam are given in Fig. 2. The height of the dam is a selected 120 m and computed thickness of the dam at the top is 5.35 m and at the base is 23.35 m. The type-5 arch dam is developed considering the reservoir and foundation. Some views of the finite element model of the dam-reservoir-foundation system are given in Fig. 3. The finite element model of the downstream face of Type-5 arch dam, and sections and node selected for comparison of the results, are given in Fig. 4. There are three unknown displacements at each nodal point in the dam, foundation and reservoir finite element model. 4355 nodes and 3188 finite element are used in the modelling of the Type-5 arch dam-reservoir-foundation system. 148 solid, 1560 solid and 1480 fluid finite elements concerning the dam, foundation and reservoir, respectively, are considered in the finite element model of the coupled system.

In this study, the length of the reservoir is taken to be as much as three times the dam height to represent the impounded water (USACE, 2003). In the finite element model of Type-5 arch dam, the dam-reservoir-foundation interaction effects are represented by the Lagrangian approach. The coupling elements are defined in the interface



Fig. 5. The time-history of ground motion acceleration of the 1992 Erzincan Earthquake.

of fluid-structure to hold equal the displacements between two reciprocal nodes. So, compatibility and equilibrium are automatically satisfied at the nodes along the interfaces between dam-reservoir-foundation. The length of the foundation was taken into account as much as the dam height in the downstream, downward and cross directions. Because of the massless foundation, the analyses considered only the effects of foundation flexibility. So the foundation model extended to a distance beyond which its effects on deflections and natural frequencies of the dam become negligible (US-ACE, 2003).

The main idea of the study is to investigate the effects of different material properties on the seismic performance of arch dams. For this purpose, the changes in foundation and reservoir material properties are selected as constant. However, the material properties of the dam are listed in three groups. In the first group, three elasticity modules are selected as Case E1, E2, and E3; Poisson ratio and mass density are constant. In the second group, three Poisson ratios are selected as Case P1, P2, and P3; elasticity modulus and mass density are constant. In the third group, three mass densities are selected as Case W1, W2, and W3; elasticity modulus and Poisson ratio are constant. The material properties of first cases of each group are defined as the same. Therefore, totaly seven different material properties are defined and seven different linear time history analyses are performed to investigate the seismic performance of Type-5 arch dam. The tensile strength of each material is selected as constant to evaluate the results in the performance curves equally. In the study, material properties selected in the analyses are summarized in Table 1.

Linear analyses are performed using ERZIKAN/ERZ-NS component of the 1992 Erzincan earthquake (Fig. 5) (Url-1, 2011) which occurred in the North Anatolian Fault. The acceleration is applied to the dam trough upstream-downstream direction. Because of the computational demand of this method, only the first 6.5 seconds of the earthquake were used during calculations. Such an abbreviated duration of time was not expected to adversely affect the results as the first few seconds of the Erzincan Earthquake were the most effective (Fig. 5). Element matrices are computed using the Gauss numerical integration technique (Bathe, 1996). The Newmark method is used in the solution of the equation of



Fig. 6. The variation of maximum displacements on II-II section of the arch dam for Case E.

motions. Rayleigh damping is considered in the analyses and damping ratio is selected as 5%. Linear analyses of the coupled system are carried out by using ANSYS finite element program (ANSYS, 2010).

4.1 The effects of elasticity modulus on the seismic performance of Type-5 Arch Dam

In this part of the study, three elasticity modules are selected as E1, E2, and E3; Poisson ratio and mass density are constant (Table 1). The variation of maximum horizontal displacements on II-II section (Fig. 4) of Type-5 arch dam obtained from linear analyses for E1, E2, and E3 cases are depicted in Fig. 6. The maximum displacements are obtained at the crest point and its values occurred as 7.2 cm, 7.8 cm, and 8.1 cm for E1, E2, and E3 cases, respectively.

The time histories of horizontal displacements in an upstream-downstream direction at the nodal point 48 (Fig. 4) of the arch dam are plotted for each case in Fig. 7a–c. The time histories of displacements are seen as similar, however, displacements increase with decreasing of elasticity modulus.

The variation of maximum and minimum principal stresses along I-I section (Fig. 4) are plotted in Fig. 8 for each case. It can be seen from Fig. 8 that the highest maximum and minimum principal stresses obtained from Case E1, E2 and E3, respectively. The maximum principal stresses are similar in the abutment and the middle parts of the dam. However, the minimum principal stresses are similar only in the abutment parts, but the highest stresses occur in the middle parts of the dam for Case E1, E2 and E3, respectively.

The time histories of maximum principal stresses (tensile stress) at nodal point 48 for each case are plotted by displaying the demand-capacity ratios (DCR) in Fig. 9a–c. In this study, the tensile strength of the concrete material is selected as 3 MPa. It is clearly seen from Fig. 9 that some values of

Table 1. Material properties of Type-5 arch dam-reservoir-foundation system.

	Group	Case	Material Properties			
			Elasticity Modulus (MPa)	Poisson Ratio	Mass Density (kg m ⁻³)	Tensile Strength (MPa)
Dam	1	E1	3.0E4	0.15	2500	3
		E2	2.5E4	0.15	2500	3
		E3	2.0E4	0.15	2500	3
	2	P1	3.0E4	0.15	2500	3
		P2	3.0E4	0.20	2500	3
		P3	3.0E4	0.25	2500	3
	3	W1	3.0E4	0.15	2500	3
		W2	3.0E4	0.15	2200	3
		W3	3.0E4	0.15	2800	3
Reservoir		Fluid 80	2.07E3	_	1000	_
Foundation		Solid 45	2.1E4	0.3	-	-



Fig. 7. The time histories of displacements at the nodal point 48 of arch dam for Case E.

the maximum principal stresses are over than DCR = 1 for all cases. It means that the maximum principal stresses occurred on the dam are much more than tensile strength of concrete used in the dam body.

The performance curves at nodal point 48 (Fig. 4) of the arch dam are presented in Fig. 10 for Case E1, E2, and E3. The level of nonlinear response or opening construction joints and/or cracking of concrete is considered acceptable if the DCR value < 2 (USACE, 2003). The results show that demand-capacity ratios for Case E2 and E3 are less than 2 and the cumulative inelastic durations at all demand-capacity ratios almost falls below the acceptance curve. It can be stated that the linear analyses of the dam-reservoir-



Fig. 8. The maximum (a) and minimum (b) stresses at section I-I of arch dam for Case E.



Fig. 9. The time histories of maximum stresses at nodal point 48 of the arch dam for Case E.

foundation system is sufficient for Case E2 and E3 and no or little damage may occur on the dam body. However, the demand-capacity ratios for Case E1 exceed 2 and the cumulative inelastic duration is substantially greater than the acceptable level. It is thought that Case E1 will cause significant damage on the dam body. Therefore, nonlinear analysis of the coupled system under material properties with Case E1 would require a more accurate estimate of the damage.



Fig. 10. Performance curves at nodal point 48 of the arch dam for Case E1, E2 and E3.



Fig. 11. The variation of maximum displacements on II-II section of the arch dam for Case P.

4.2 The effects of Poisson ratio on the seismic performance of Type-5 Arch Dam

In this part of the study, three Poisson ratios are selected as P1, P2 and P3; elasticity modulus and mass density are constant (Table 1). The variation of maximum horizontal displacements on II-II section (Fig. 4) of Type-5 arch dam obtained from linear analyses for P1, P2 and P3 cases are depicted in Fig. 11. The maximum displacements are obtained at the crest point and its values are almost near to each other.

The time histories of horizontal displacements in an upstream-downstream direction at the nodal point 48 (Fig. 4) of the arch dam are plotted for each case in Fig. 12a–c. The time histories of displacements for each case are similar to each other. This shows that different Poisson ratios do not change the results affluently.



Fig. 12. The time histories of displacements at the nodal point 48 of arch dam for Case P.



Fig. 13. The maximum (**a**) and minimum (**b**) stresses at section I-I of arch dam for Case P.

The variation of maximum and minimum principal stresses along I-I section (Fig. 4) are plotted in Fig. 13 for each case. It can be seen from Fig. 13 that the distribution of the maximum and minimum principal stresses obtained from Case P1, P2 and P3 are similar to each other.

The time histories of maximum principal stresses (tensile stress) at nodal point 48, which is the most representative crest point of the downstream side of the dam, for each case are plotted by displaying the demand-capacity ratios (DCR) in Fig. 14a–c. It is clearly seen from Fig. 14 that some values of maximum principal stresses are over than DCR = 1 for all cases. It means that the maximum principal stresses which occurred on the dam are much more than tensile strength of concrete used in the dam body.

The performance curves at nodal point 48 (Fig. 4) of the arch dam are presented in Fig. 15 for Case P1, P2 and P3. The level of nonlinear response or opening construction joints and/or cracking of concrete is considered acceptable if the DCR value < 2 (USACE, 2003). The results show that demand-capacity ratios for all three cases are more than 2 and the cumulative inelastic durations at all demand-capacity ratios almost exceed the acceptance curve. It can be stated that the linear analyses of dam-reservoir-foundation system is insufficient for Case P1, P2 and P3 and some or significant damage may occur on the dam body. Therefore, nonlinear analysis of the coupled system under material properties with Case P1, P2 and P3 would require more accurate estimates of the damage.



Fig. 14. The time histories of maximum stresses at nodal point 48 of the arch dam for Case P.



Fig. 15. Performance curves at nodal point 48 of the arch dam for Case P1, P2 and P3.

4.3 The effects of mass density on the seismic performance of Type-5 Arch Dam

In this part of the study, three mass densities are selected as W1, W2 and W3; elasticity modulus and poisson ratio are constant (Table 1). The variation of maximum horizontal displacements on II-II section (Fig. 4) of Type-5 arch dam obtained from linear analyses for W1, W2 and W3 cases are depicted in Fig. 16. The maximum displacements are obtained at the crest point and its values are near to each other. But they are a little higher for higher mass density values.

The time histories of horizontal displacements in the upstream-downstream direction at the nodal point 48 (Fig. 4) of the arch dam are plotted in Fig. 17a–c for each case. The time histories of displacements for each case are similar to each other. This shows that different mass densities do not change the results affluently.

The variation of maximum and minimum principal stresses along I-I section (Fig. 4) are plotted in Fig. 18 for each case. It can be seen from Fig. 18 that the distribution of the maximum and minimum principal stresses obtained from Case W1, W2 and W3 are similar to each other. Also, the highest values of minimum principal stresses for each case are near. However, the highest values of minimum principal stresses are obtained from W3, W1 and W2, respectively.



Fig. 16. The variation of maximum displacements on II-II section of the arch dam for Case W.



Fig. 17. The time histories of displacements at the nodal point 48 of arch dam for Case W.

The time histories of maximum principal stresses (tensile stress) at nodal point 48, which is the most representative crest point of downstream side of the dam, for each case are plotted by displaying the demand-capacity ratios (DCR) in Fig. 19a–c. It is clearly seen from Fig. 19 that some values of maximum principal stresses are over than DCR = 1 for all cases. It means that the maximum principal stresses occurred on the dam are much more than tensile strength of concrete used in dam body.

The performance curves at nodal point 48 (Fig. 4) of the arch dam are presented in Fig. 20 for Case W1, W2 and W3. The level of nonlinear response or opening construction joints and/or cracking of concrete is considered acceptable if the DCR value < 2 (USACE, 2003). The results show that demand-capacity ratios for all three cases are more than 2



Fig. 18. The maximum (a) and minimum (b) stresses at section I-I of arch dam for Case W.



Fig. 19. The time histories of maximum stresses at nodal point 48 of the arch dam for Case W.

and the cumulative inelastic durations at all demand-capacity ratios almost exceed above the acceptance curve. It can be stated that the linear analyses of dam-reservoir-foundation system is insufficient for Case W1, W2 and W3 and some or significant damage may occur on the dam body. Therefore, nonlinear analysis of the coupled system under material properties with Case W1, W2 and W3 would require more accurate estimates of the damage.

5 Conclusions

The study presents the effects of material properties on the seismic performance of arch dam-reservoir-foundation systems by using demand-capacity ratios. The 3-D time history analyses of the coupled system are performed for three different material groups. In the first group, the elasticity modulus is selected changeable; in the second group, the Poisson ratio is selected changeable; and in the third group, the mass density is selected changeable. The time histories and maximum values of the displacements and principal stresses, and performance curves, are obtained from linear analyses to determine the material effects on the seismic performance of the Type-5 arch dam.

- The first group analyses show that Type-5 arch dam has a nonlinear behaviour under selected earthquake for higher elasticity modulus of the dam. While demandcapacity ratio exceeds to 2, and the cumulative inelastic duration is substantially greater than the acceptable



Fig. 20. Performance curves at nodal point 48 of the arch dam for Case W1, W2 and W3.

level for Case E1; it is less than 2, and the cumulative inelastic duration at all demand-capacity ratios almost falls below the acceptance curve for Case E2 and E3.

- The second group analyses show that Type-5 arch dam has a nonlinear behaviour under selected earthquake for all assumed Poisson ratios of the dam. However, the displacement and principal stress results are very near to each other for Case P1, P2 and P3. This implies that the changes on Poisson Ratio are not affected by dam behaviour.
- The third group analyses show that the results obtained for different mass density values are similar to the second group analyses results. However, it can be stated that the changes on mass density are more effective on the seismic performance of the Type-5 arch dam than the changes on Poisson ratio.
- The results show that demand-capacity ratios for smaller elasticity modules and mass densities are less than 2, and the cumulative inelastic duration at all demand-capacity ratios almost falls below the acceptance curve. The dam response under the earthquake can be considered to be within the linear elastic range of behaviour with little or no possibility of damage. However, demand-capacity ratios for higher elasticity modules and mass densities exceed 2, and the cumulative inelastic duration is substantially greater than the acceptable level. It is thought that the dam will exhibit a nonlinear response in the form of cracking of the concrete and/or opening of the construction joints. Then a nonlinear analysis would be required for a more accurate estimate of the damage.
- In this study, the changes of selected material properties are about 20–30 %, however, the changes of the results

are smaller, especially obtained for Poisson ratios and mass densities. On the other hand, if it is necessary to compare material properties, the author can suggest that the elasticity modulus is more effective on the seismic performance of Type-5 arch dam than the Poisson ratio and mass density.

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