

## Short-term retreat statistics of a slowly eroding coastal cliff

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**Abstract.** The frequency, spatial distribution, and dimensions of coastal cliff retreats, a basic statistic underlying cliff top hazard assessment, are presented for 7.1 km of unprotected and slowly retreating coastal cliffs near Point Loma in San Diego, California, US. Using 8 airborne light detection and ranging (lidar) surveys collected over 5.5 years, 130 individual cliff edge failures (primarily rockfalls, block falls, and topples) were detected. Footprint areas varied from 3 to 268 m<sup>2</sup>, maximum landward retreats from 0.8 to 10 m, and alongshore lengths from 2 to 68 m. The failures with the largest landward retreats were also relatively long, and 13% of the slides accounted for 50% of the lost cliff area over the study period. On this short (5.5 years) time scale, “no change” was the most common observation (84% of the cliff edge). Probability distributions of non-zero cliff retreat during each time interval usually had a single peak between 1 and 2.5 m. Intervals with high mean retreat had elevated numbers of failure in all class sizes, and also contained the largest individual retreats. Small and medium slides tended to reoccur preferentially (relative to randomly) near previous small and medium slides, forming short-term hot spots, while large slides were less likely to reoccur near previous large slides. Cumulative distributions of landslide failure parameters (area, mean retreat, maximum retreat, and length) follow an inverse power-law for medium to large size events, similar to previously reported distributions of coastal and inland landsliding.

interact with complex site-specific local geology to produce temporally and spatially variable retreat (Trenhaile, 1987; Sunamura, 1992). The limited available historical observations provide mean (time-and-alongshore averaged) retreat rates, but extrapolation of these rates to estimate site-specific future risk is problematic because the magnitude variability (in space and time) of cliff retreat is not considered (Cammers, 1976; Lee et al., 2001; Moore and Griggs, 2002; Quinn et al., 2009). Retreat magnitude variability and episodicity are included in recent probabilistic characterizations of cliff retreat (e.g. Lee et al., 2001, 2002; Hall et al., 2002; Williams et al., 2004; Teixeira, 2006; Milheiro-Oliveira, 2007; Furlan, 2008). These models highlight both the need for, and the scarcity of, observations of even basic statistics such as the dependence of cliff retreat frequency on retreat magnitude.

The statistics of inland mass movements have been studied extensively (e.g. Hovius et al., 1997; Pelletier et al., 1997; Dai and Lee, 2001; Dussauge-Peisser et al., 2002; Guzzetti et al., 2002; Hergarten, 2003; Brardinoni and Church, 2004; Brunetti et al., 2009; ten Brink et al., 2009). Historical records of coastal cliff failure statistics are relatively sparse. Dong and Guzzetti (2005) investigated the frequency statistics of soft cliff retreat for two data sets. The first (obtained from Hall et al., 2002) consisted of 32 (26 non-zero) measurements made along eight transects over four time intervals ranging from 7 to 29 years at East End in East Sussex, England. The second data set included 198 (168 non-zero) yearly measurements from 1953 to 1990 along six transects on the Holderness coast, England. For both datasets, the frequency of cliff retreat decreases with event size, and medium to large size events follow an inverse power-law distribution.

Teixeira (2006) investigated the frequency statistics and geometric relationships of coastal mass movements in Miocene aged rock cliffs of the Algarve, Portugal. These datasets consisted of 140 field measurements obtained over

### 1 Introduction

Seacliff retreat threatens cliff top infrastructure, and estimates of future cliff positions are needed for coastal planning. Multiple marine and subaerial erosive processes



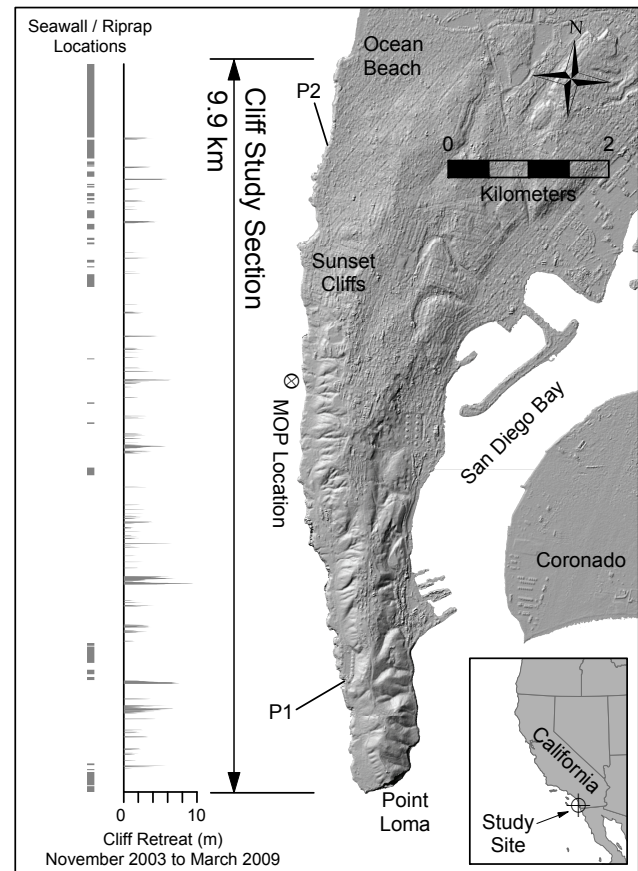
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nine years, and 177 events obtained from aerial photographs over 44 years. The cumulative frequency of cliff retreat for both datasets fit a power-law distribution above a critical value, and deviated for relatively small events. Teixeira (2006) also found power-law relationships between volume, horizontal area, and retreat. Marques (2008) further investigated the magnitude-frequency statistics of strong, slowly retreating coastal cliffs ( $< 10 \text{ cm yr}^{-1}$ ) in terms of volume, horizontal area, and cliff retreat. The database included about 600 events from regional scale observations obtained from aerial photographs spanning up to 53 years in Portugal and Morocco, and smaller scale insitu field observations (from Teixeira, 2006) in Portugal.

Rosser et al. (2007) used high resolution monthly terrestrial laser scans collected over 32 months in the North York Moors National Park, UK to compile a large database of over 500 000 coastal rockfalls. Rockfall volume and scar area (parallel to the rock face) followed a power law, and the cumulative distribution followed a linear trend for log volume versus normalized frequency. Their results suggested that rock type influenced scar geometry, and that smaller rockfalls often preceded larger failures.

Lim et al. (2010) recently compiled a database over 100 000 coastal rockfalls using monthly terrestrial laser scanning and orthophotography over 20 months at Staithes, North Yorkshire, UK. They found a linear trend in the non-cumulative distribution of log volumes, including the small changes that were resolved with their uniquely high-resolution observations. These results suggest under-sampling of small cliff failures caused the deviation of the magnitude-frequency relationships found previously in coastal (Dong and Guzzetti, 2005; Teixeira, 2006; Marques, 2008) and inland (e.g. Hovius et al., 1997; Stark and Hovius 2001; Dussauge-Peisser et al., 2002; Malamud et al., 2004) observations.

The different methods, measured parameters, and failure types make comparisons of failures from different studies difficult. For example Teixeira (2006) and Marques (2008) report horizontal (planimetric) area while Rosser et al. (2007) and Lim et al. (2010) consider area parallel to the cliff face. Some studies focus on magnitude-frequency relationships of cliff retreat (Dong and Guzzetti, 2005; Teixeira, 2006) while others on failure volume (Rosser et al., 2007; Lim et al., 2010). Cliff edge retreat failures, a subset of the cliff failures, are generally used in models to establish structural setbacks, while volumetric statistics are more appropriate for processed-based modeling. Many authors note that additional cliff failure inventories are required to assess the generality and predictive utility of observation-based, statistical characterizations of cliff retreat. The present study uses 8 airborne lidar surveys collected over 5.5 years to describe basic two dimensional (planimetric), short-term (5.5 yr) statistics of cliff edge failures over 7.1 km of unprotected coastal rock cliffs in southern California, US.



**Fig. 1.** Location map of the Sunset Cliffs to Point Loma study area showing alongshore projected locations of seawall/riprap and the cumulative cliff retreat (unprotected cliffs) occurring during the study period (October 2003 to March 2009). At least two locations (P1 and P2) with seawall/riprap experienced significant erosion.

## 2 Study area

### 2.1 General description

The southern California study area extends from the southwest end of Point Loma to Ocean Beach in southern San Diego County, California (Fig. 1) consisting of 9.9 km of shoreline. The cliff top in the northern section is developed with the residential communities of Sunset Cliffs and Ocean Beach, while the southern section contains important infrastructure including a wastewater treatment plant, the Point Loma lighthouse, and US Navy facilities. Cliff retreat has undermined Sunset Cliffs Blvd. (Shepard and Grant IV, 1947), and resulted in building condemnation (Flick, 2005). Riprap and seawalls protect about 28% (2.8 km) of the cliffs, mostly in the northern section (Fig. 1). Tides are mixed with a maximum range of about 2 m.

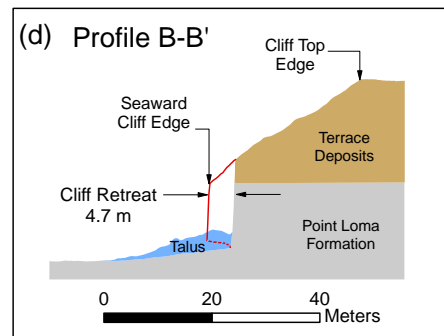
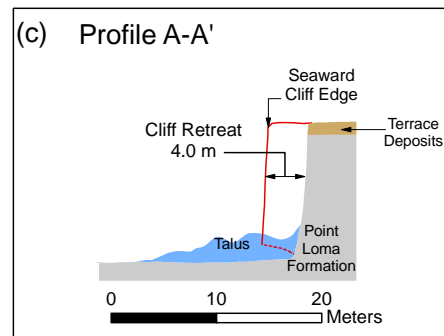
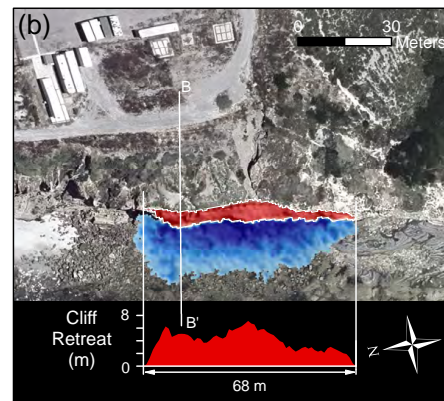
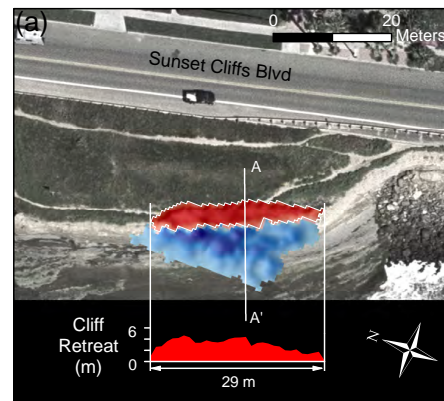


**Fig. 2.** Oblique photo showing the general stratigraphy and landscape of the study area (photo by Darren Wright, California Data Information Program).

## 2.2 Geology

Point Loma is a rock promontory uplifted by the Rose Canyon section of the Rose Canyon-Newport-Inglewood Fault. The seacliffs exposed on the seaward side of the promontory are generally 20 to 30 m high (range of 5 to 40 m), and are composed of two geologic units (Fig. 2). The lower unit is the Point Loma Formation, a lithified Cretaceous interbedded fine grain sandstone and shale, unconformably overlain by the Bay Point Formation, a poorly consolidated Pleistocene sandstone terrace deposit (Kennedy, 1975). The contact between the two units decreases in elevation towards the north, where it intersects the cliff base in the heavily armored section of Ocean Beach. The Point Loma Formation often forms a vertical cliff face except where undercut, while the weaker Bay Point Formation tends to form slope angles of about  $30^\circ$  (Figs. 2 and 3). There are two common cliff profiles; (1) nearly entirely vertical and composed primarily of the Point Loma Formation, and (2) a sloped upper cliff composed of the Bay Point Formation (Fig. 3). According to Emery and Kuhn (1982), both profiles indicate that marine erosion dominates subaerial erosion. However, Kuhn and Shepard (1984) and Flick (1994) document accelerated local erosion caused by concentrated surface runoff, and the relative importance of marine versus subaerial processes is unknown. Although the statistical failure properties described are for unprotected cliffs, they may be affected by adjacent armored cliffs and cliff top development.

Joints, fractures, and a series of northeasterly intersecting faults create weak areas in the lower cliff, resulting in alongshore variable cliff resistance, and a highly irregular shoreline containing sea caves, wave cut notches, surge channels, small headlands, a few pocket beaches, and an occasional sea stack, arch, or blow-hole. The shore platform,



**Fig. 3.** Areas of large cliff failures (red) and resulting talus deposition (blue) that occurred in (a) Interval 5, and (b) Interval 2. Lower inset: cliff retreat versus alongshore location. (c) Schematic cut-away view on profiles A-A' and (d) B-B' before (red line) and after the cliff failures. Typical notch profiles in (c) and (d) were estimated from oblique photos ([www.californiacoastline.org](http://www.californiacoastline.org)). Scale bars in panels (c) and (d) represent both the cross-shore and vertical cliff dimensions.

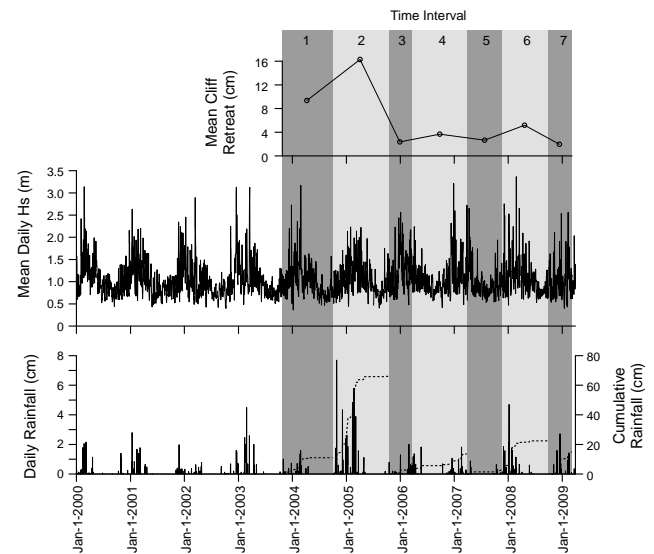
composed of the Point Loma Formation, is often submerged at the cliff base and lacking beach sand (with the exception of a few narrow pocket beaches), with wave attack during average or higher tide stages. At some locations, the shore platform elevation allows wave attack at all tide stages. Cliff undercutting at the cliff base from wave action is often present and can result in cliff instability, as at other cliffs (Hampton, 2002; Kogure et al., 2006; Young and Ashford, 2008; Budetta, 2010). Cliff failures in the Point Loma Formation generally occur as rock falls, block falls, and topples (Varnes, 1978).

### 2.3 Historical erosion

Historical photographs of Sunset Cliffs-Point Loma (Shepard and Grant IV, 1947; Shepard and Wanless, 1971; Kuhn and Shepard, 1984) show the collapse of sea arches and sea caves, the erosion of sea stacks, and an earthquake-triggered cliff failure. Kennedy (1973) used old photographs and observations to estimate an average cliff retreat rate of  $1.2 \text{ cm yr}^{-1}$  over 75 years, and noted that some sea caves extend landward as much as 18 m from the cliff face. Average cliff retreat of  $8 \text{ cm yr}^{-1}$  between 1952 and 1994 was estimated using orthorectified aerial photographs (Benumof and Griggs, 1999; Moore et al., 1999; Benumof et al., 2000). Spaulding and Crampton (2001) estimated retreat rates of 2 to  $6 \text{ cm yr}^{-1}$  for a small portion of Sunset Cliffs over a 70-year period beginning in 1928 from aerial photographs. Hapke and Reid (2007a) used 1934 T-sheets and a 1998 lidar survey to estimate cliff retreat rates along cross-shore transects that average to  $17 \text{ cm yr}^{-1}$ . Several studies (Shepard and Grant IV, 1947; Kennedy, 1973; Spaulding and Crampton, 2001) indicated no observable erosion at some locations over considerable time periods, while others (Kuhn and Shepard, 1984; Hapke and Reid, 2007b) found local cliff retreat rates as large as  $100 \text{ cm yr}^{-1}$ . The large range of average long-term cliff retreat estimates results from differences in data quality, time period evaluated, cliff armoring, and study section. There is general agreement that cliff retreat is episodic in both space and time. Shepard and Wanless (1971) state “the coast is retreating, although very unevenly”, while Kennedy (1973) noted cliff retreat is “regionally negligible and locally high”.

### 2.4 Climate

San Diego’s semi-arid Mediterranean climate is characterized by dry summers and occasionally wet winters, with 85% of rainfall from November through March. Annual precipitation amounts vary from about 10 to 60 cm, and average 25 cm. Rainfall during the study period was average or less, except for winter 2004 to 2005 (Interval 2), when rainfall exceeded twice the annual average (Fig. 4).



**Fig. 4.** Top: mean section cliff retreat occurring during each time interval. Center: mean daily significant wave height ( $H_s$ ) at a virtual buoy located seaward of the cliff section in 10 m water depth (monitoring and prediction point location (MOP), Fig. 1). Bottom: daily rainfall totals and cumulative daily rainfall during each interval (dotted line) at Cabrillo National Monument (<http://www.wrh.noaa.gov/sgx/obs/rtp/cabrillo.html>) located at the southern end of the study area. Gray bars indicate time periods between lidar surveys used in this study.

### 2.5 Waves

The seacliffs are exposed to swell from distant storms in both hemispheres and waves generated by local winds. During winter, swell from the North Pacific and the Gulf of Alaska are most energetic, whereas swell from the South Pacific dominates in summer. The seasonal cycle produces maximum wave energy in winter (Fig. 4). Wave conditions vary alongshore, and were estimated from a wave buoy network (CDIP, <http://cdip.ucsd.edu>) and a spectral refraction wave model that accounts for the effects of complex bathymetry in the southern California Bight, varying beach orientation, and wave exposure (O’Reilly and Guza, 1991, 1998). Mean daily significant wave height ( $H_s$ ) at a virtual buoy or “Monitoring and Prediction point” (MOP) located in 10 m water depth seaward of the cliff section (Fig. 1), shows that wave heights were typical during the study period (Fig. 4). Although wave conditions vary alongshore, the patterns of seasonal and interannual variation are similar at all the study cliffs. Complex small scale cliff-base geometry precludes detailed estimates of location-specific marine erosional forces.

## 2.6 Seismicity

Minor ground motions are relatively common in the tectonically active San Diego region. However, no earthquakes with magnitude  $> 5.0$  occurred within 100 km of the study site, during the study period ([www.data.scec.org](http://www.data.scec.org)).

## 3 Methods

### 3.1 Lidar data collection

Eight airborne lidar surveys (Table 1) were conducted between October 2003 and March 2009 with an Optech Inc. Airborne Laser Terrain Mapper (ALTM) 1225. Each airborne survey consisted of 2 to 4 passes with a  $40^\circ$  swath at an altitude ranging from 300 to 1150 m resulting in a point density of approximately 2 to 4 points  $m^{-2}$ . The alongshore aircraft trajectory was located approximately 0 to 100 m seaward of the seacliffs. ALTM elevation points are computed using three sets of data: laser ranges and their associated scan angles, platform position and orientation information, and calibration data and mounting parameters (Wehr and Lohr, 1999). GPS receivers in the aircraft and on the ground at control points provide platform positioning. The GPS receivers record pseudo-range and phase information for post-processing. Platform orientation information comes from an Inertial Measurement Unit (IMU) containing three orthogonal accelerometers and gyroscopes. An aided-Inertial Navigation System (INS) solution for the aircraft's attitude is estimated from the IMU output and the GPS information.

### 3.2 Digital elevation model

Lidar data was occasionally obtained in over-hanging locations such as seaclaves and notches, however the partial coverage did not permit construction of fully 3-D terrain models, and volume statistics could not be estimated. Therefore, the point data were processed into 0.5 m resolution 2.5-D digital elevation models using the second of two returns (the most representative of the ground surface) and a modified "natural neighbors" interpolation that removes over-vertical features and maintains vertical cliff edges and complex topography (see Appendix A, LEM-DEM).

### 3.3 Change detection and cliff retreat

Vertical topographic change for the seven time intervals (Table 1), obtained by differencing successive digital elevations models to create digital change grids (DCG), shows erosion (negative changes) at failure locations, and accretion (positive changes) at cliff base talus deposits (Fig. 3). Sources of errors in the DCGs include the basic lidar observations, spatial interpolation, and vegetation. The

vertical root mean square difference between two surveys ( $RMS_Z$ , Federal Geographic Data Committee, 1998), a measure of the total error, was estimated using three control sections of stabilized slopes and seawalls that represent the range of slopes and vegetative conditions of the studied seacliffs. The average  $RMS_Z$  of all control sections and intervals was 18 cm, and ranged from 10 to 24 cm.

The DCGs were filtered and edited to remove noise and identify the individual failures causing seaward cliff edge retreat. First, all grid cells with a vertical change of less than 2 m ( $\gg RMS_Z$ ) were removed. Next, a minimum topographic footprint was imposed, requiring at least 12 connected cells of negative change, thus enforcing a minimum change area of  $3 m^2$ . The vertical and footprint thresholds, selected through trial and error and tested on the control surfaces, significantly reduced noise. Finally, the digital data footprints were visually inspected, yielding the topographic footprints of individual seaward cliff-edge failures during each time interval. The seaward cliff edge was used as the shoreline reference feature because cliff retreat is readily identifiable for landslides occurring in both profile types (Fig. 3). The seaward edge was coincident with the cliff top edge when the upper cliff slope was vertical (Fig. 3c). These interval changes could represent combined individual, adjacent landslides that occurred during a particular time interval.

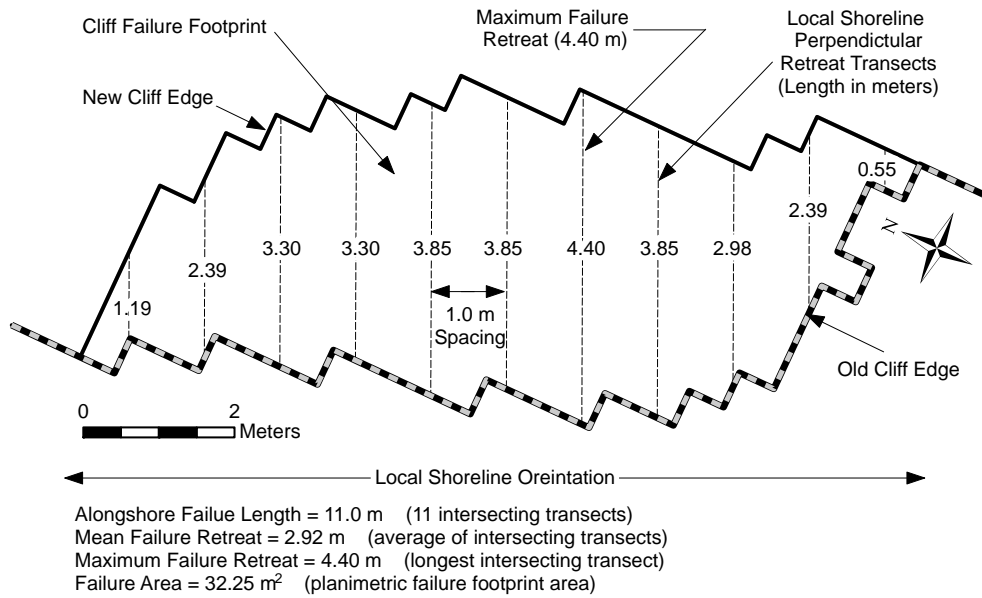
### 3.4 Cliff failure parameters

Cliff failure footprints were sampled on local cross-shore oriented transects spaced 1.0 m alongshore (Fig. 5). The DCGs usually were not aligned with the local shoreline orientation, resulting in a range of retreat measurements (including values less than the grid size) rather than increments of the 0.5 m grid size. The alongshore failure length was defined as the number of transects intersecting the failure footprint. Mean failure retreat was estimated as the average of intersecting transects for each slide, while the maximum failure retreat represents the longest intersecting transect. The cliff footprint area was measured as the planimetric area on the DCGs. Note this method can result in small differences between the measured planimetric area, and area calculated as the product of alongshore failure length and mean failure retreat, but provides a simple automated way to estimate cliff failure attributes with locally changing shoreline orientation.

## 4 Results and discussion

### 4.1 Erosion at protected cliffs

Retreat at cliffs with riprap or seawalls was relatively minor, however at least two protected locations (P1 and P2, Fig. 1) experienced significant erosion. At P1 during Interval 2, a mid-cliff failure in the Point Loma Formation occurred

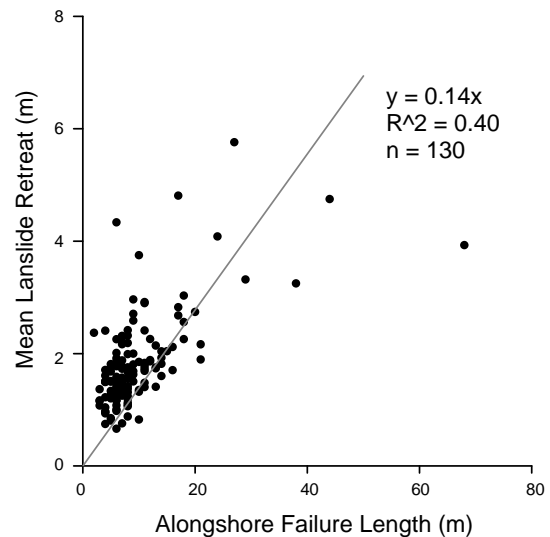


**Fig. 5.** Example of a cliff failure footprint, local shoreline perpendicular retreat transects, and estimated failure attributes and geometry. Intersecting transects cross the failure footprint, determined on a 0.5 m grid. The old cliff edge (thick dashed gray/black line) and new cliff edge (thick solid black line) bound the cliff failure footprint.

between a rock revetment at the cliff base and an upper cliff retaining wall. Erosion (primarily of the terrace deposits) at location P2 occurred during Intervals 1 through 4 and 7, and involved a seawall failure with loss of residential property. These events (and others at protected cliffs) are excluded from further consideration because cliff protection significantly alters cliff failures.

**4.2 Cliff failure footprint, geometry, correlations, and probabilities**

The 130 individual cliff edge failure footprints ranged in area from 3 to 268 m<sup>2</sup> with a mean of 22 m<sup>2</sup> (Appendix A, Table A1). Alongshore failure lengths ranged from 2 to 68 m with a mean of 10 m. The mean and maximum failure retreat measured perpendicular to the local shoreline orientation ranged from 0.7 to 5.8 m, and from 0.8 to 10.0 m, respectively. Although the alongshore failure length and mean retreat distance are correlated (mean retreat ~0.14 length, Fig. 6), there is considerable variation in the length/retreat ratio, with the largest variation for large slides. For example, the largest mean retreats (between 3 and 6 m) have alongshore lengths varying by a factor of 17 (between 4 and 68 m). The shortest of slides with relatively large mean retreat (between 3 and 6 m) usually occurred in areas with relatively complex alongshore shape, whereas the longest slide was relatively straight alongshore. Geologic discontinuities (e.g. joints and faults) can exert strong control on cliff failure dimensions (Kogure and Matsukura, 2010), and likely affected the observed failure geometries.



**Fig. 6.** Mean failure retreat versus alongshore failure length for the 130 slides.

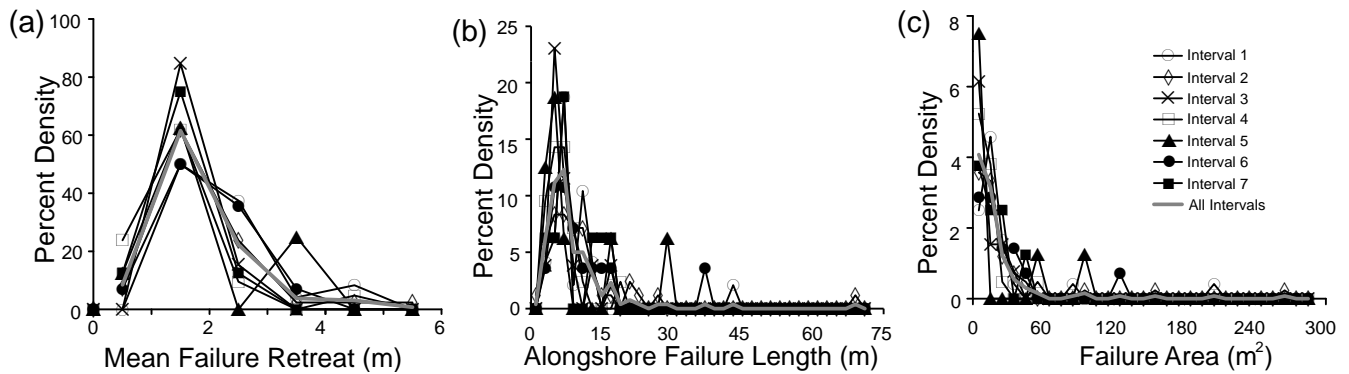
The larger area, infrequent failures contributed substantially to the mean (cliff-wide) retreat over the entire study period. For example, the 17 (13% of the total number of failures) largest failures comprised 50% of the total lost cliff area. The single largest failure extended 68 m alongshore (Interval 2, Fig. 3b), equivalent to 3.7 cm of retreat averaged over the entire study section. This single failure was equivalent or more than the mean retreat in Intervals 3, 4, 5 or 7 (Table 1).

**Table 1.** Interval information.

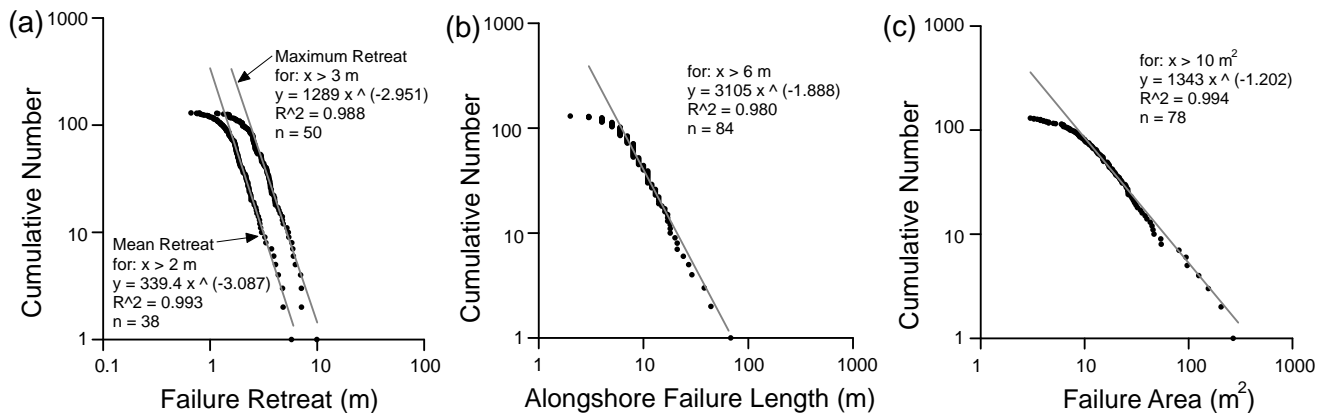
Interval	1	2	3	4	5	6	7	1–7
Start Date	25 Oct 2003	29 Sep 2004	19 Oct 2005	24 Mar 2006	28 Mar 2007	23 Nov 2007	28 Sep 2008	25 Oct 2003
End Date	29 Sep 2004	19 Oct 2005	24 Mar 2006	28 Mar 2007	23 Nov 2007	28 Sep 2008	8 Mar 2009	8 Mar 2009
Time Length (Days)	340	385	156	369	240	310	161	1961
Time Length (Years)	0.9	1.1	0.4	1.0	0.7	0.8	0.4	5.4
Mean Retreat (cm)	9.4	16.3	2.4	3.7	2.7	5.2	2.0	41.7
Mean Retreat Rate (cm yr <sup>-1</sup> )	10.0	15.4	5.7	3.6	4.1	6.1	4.5	7.8
Maximum Retreat (m)	10.0	7.1	5.8	5.9	4.8	6.0	3.7	10.0
Extent of Cliff Retreat (m)	248	473	98	155	78	155	81	1288/1153*
Area Lost (m <sup>2</sup> )	655	1146	166	254	186	367	137	2910
Number of Landslides	24	42	13	21	8	14	8	130/102**

\* 1288 (sum of interval extent)/1153 (extent considering amalgamation over the combined intervals).

\*\* 130 (sum of interval slides)/102 (slides considering amalgamation over the combined intervals).



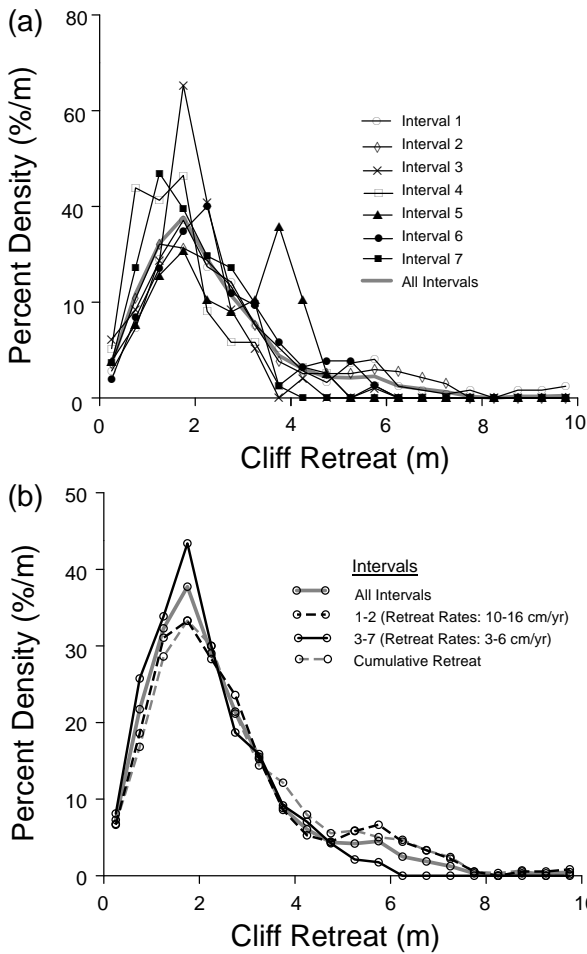
**Fig. 7.** Probability density of individual failures (a) mean retreat (% m<sup>-1</sup>), (b) alongshore length, (% m<sup>-1</sup>) and (c) area (% m<sup>-2</sup>) during each time interval, and averaged over all intervals (see legend).



**Fig. 8.** Log of the cumulative number of failures versus log of (a) mean and maximum failure retreat, (b) alongshore length, and (c) area.

Probability density functions characterizing the calculated mean failure retreat (Fig. 7a), alongshore distance (Fig. 7b), and area (Fig. 7c) of individual slides are generally similar between intervals and are right skewed. The cumulative distributions of individual failure parameters; mean and maximum retreat (Fig. 8a), alongshore distance (Fig. 8b), and area (Fig. 8c), all fit well to inverse power-law distributions for relatively medium-large size events. The

scaling exponent of the cliff-edge failure area cumulative distribution ( $b = 1.2$ , Fig. 8c), is similar to the  $b \sim 1.0$  found by Marques (2008). Unimodal cliff failure probability density functions (Fig. 7), and power-law cumulative distributions for medium-large events were also reported by Dong and Guzzetti (2005) and Marques (2008). Small events were not reliably detected in these studies, and areas  $< 3 \text{ m}^2$  are excluded from the present statistics.

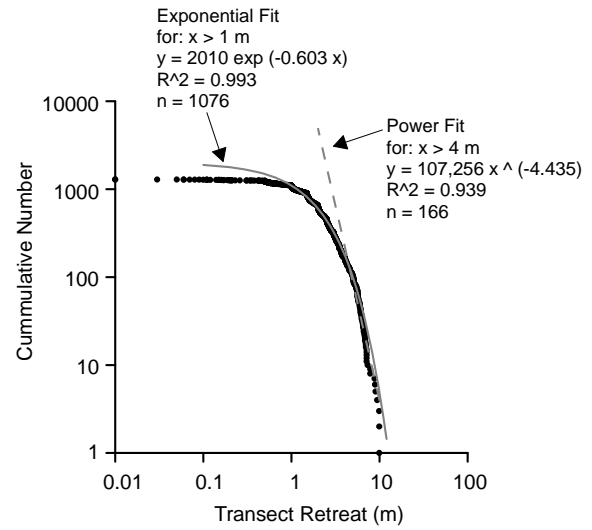


**Fig. 9.** Probability density functions of transect (a) cliff retreat occurring during each time interval, and (b) combined time periods with relatively high (Intervals 1 and 2) and low retreat rates (Intervals 3 through 7). The probability density functions are based on 0.5 m intervals and plotted along the x-axis using the mid-interval location.

**4.3 Footprint transect retreat measurements**

The 130 individual cliff edge failures from all time intervals were sampled on transects spaced 1 m alongshore, resulting in approximately 1300 non-zero transects. Transect retreats ranged from 0.01 to 10 m, with a mean and median of 2.3 m and 2.0 m, respectively. The maximum cumulative cliff retreat at single location during the study period was 10 m (1.8 m yr<sup>-1</sup>). Approximately 84% of the cliff edge experienced no detectable retreat over the study period based on the described methods.

The shapes of the retreat probability density functions for each time interval were similar, with a single peak ranging between 1 and 2.5 m (Fig. 9a), except for the bimodal Interval 5. The retreat events of combined large mean retreat intervals (1 and 2), small mean retreat intervals (3 through 7),



**Fig. 10.** Log of cumulative number of transect retreats versus log of transect retreat.

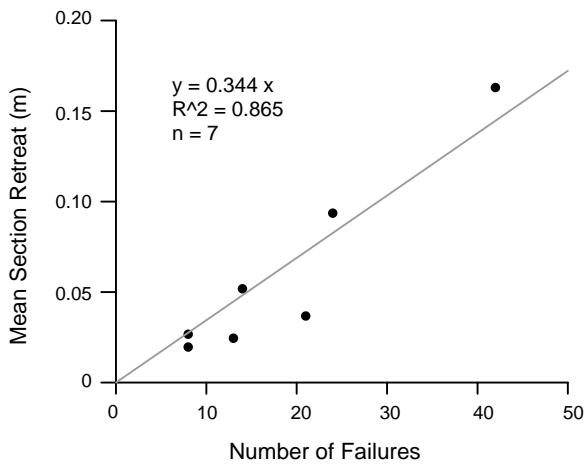
all-intervals, and cumulative retreat are all positive skewed with a peak around 2 m (Fig. 9b). However, the retreat distribution during large and small mean retreat intervals are significantly different (k-s test,  $p = 0.000031$ , compare bold dashed with bold solid curve in Fig. 9b). During intervals of large mean section retreat, larger retreat events occur more often than expected compared to intervals with low mean section retreat. The converse is also true suggesting the distributions of cliff retreat may differ for time periods with varying amounts of overall failure activity.

The distributions of cumulative (e.g. total on transects) and average-all-interval retreat differ (Fig. 9b) because locations that retreat more than once are amalgamated into a single value in the cumulative distribution. The cumulative distribution of all individual retreat measurements (Fig. 10) fits better to an exponential distribution rather than a power-law, particularly for medium size events where the power-law fit deviates for values > 4 m. A single failure affects multiple adjacent transect retreat measurements, and the non-independence of transects probably contributed to power law deviation, along with amalgamation and under sampling of small areas.

**4.4 Mean interval cliff retreat**

The mean cliff retreat (averaged over the unprotected cliff section, including transects with no change) during each interval ranged from 2 to 16 cm. The average retreat rate of 7.8 cm yr<sup>-1</sup> is consistent with rates measured from 1952 to 1994 of about 8 cm yr<sup>-1</sup> (Benumof and Griggs, 1999; Moore et al., 1999; Benumof et al., 2000). Maximum mean cliff retreat, number of failures, and the extent of alongshore change (Table 1) all occurred during Intervals 1 and 2.





**Fig. 11.** Mean retreat (over the unprotected cliffs) versus the number of failures during each time interval.

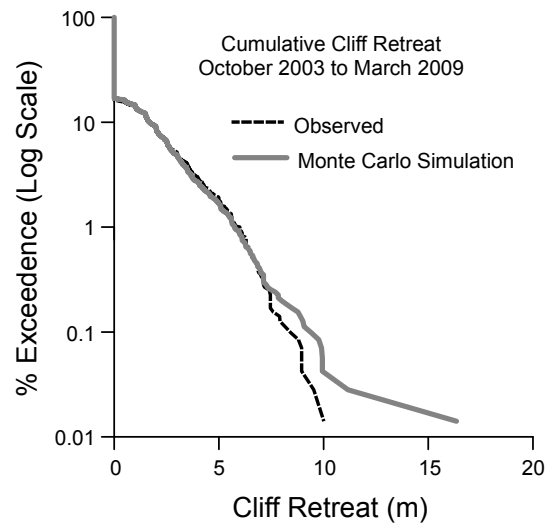
If the size distribution of retreats were constant from interval to interval, then the mean retreat and number of failures in the interval would be linearly related, as was only approximately observed (Fig. 11). Mean retreat values in Intervals 1 and 2 were elevated above the best fit line because large slides occur disproportionately more often in the intervals with the most slides (Fig. 11).

#### 4.5 Spatial distribution of cliff retreat

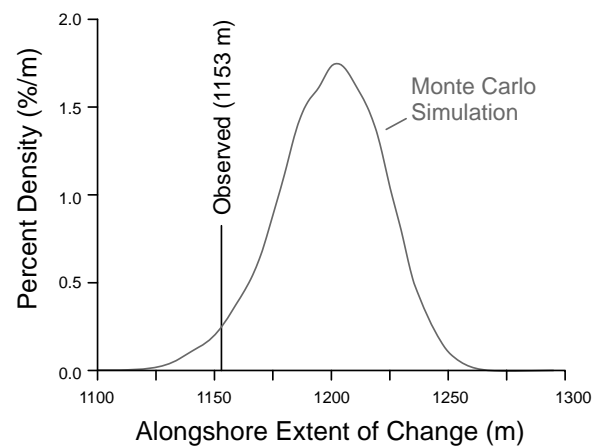
Retreat occurred along less than 3% of the cliff length in all intervals except Interval 2, when 7% of the section retreated. In total, about 1150 m of the unprotected cliffs experienced measurable cliff retreat during the study period. Forty eight of the failure footprints were spatially adjacent to at least one other failure resulting in 20 amalgamated footprints and 135 m of cliff retreating more than once.

The potential presence of short-term cliff retreat hot spots (Young et al., 2009a) was investigated with a simple Monte Carlo simulation of cliff retreat for the study period. The simulated cliff retreat for each time interval used the observed interval failure events and random spatial placement along the 7.1 km (unprotected) cliff section.

The random spatial placement of the Monte Carlo simulation over-predicted the maximum cumulative cliff retreat by 6 m (Fig. 12), and the observed alongshore extent of cliff retreat was about 50 m smaller than the Monte Carlo mean (Fig. 13). The differences between the Monte Carlo simulation and observations are consistent with cliff retreat history at a particular location influencing subsequent cliff retreat. For example, the simulated alongshore extent of failures can be made to match the observations by forcing some small to moderate failures to coincide with previous events, creating non-random, short-term hot spots. Small failure events could redistribute stress to nearby locations causing strain accumulation and concentrating future failures



**Fig. 12.** Observed and Monte Carlo simulation (100 realizations) of % exceedence of cumulative transect cliff retreat. The most common cumulative retreat is zero. The observed and modeled cumulative retreat distributions differ for large, infrequent events, but the distributions are overall only marginally different (k-s test,  $p = 0.21$ ).



**Fig. 13.** Probability density function of alongshore extent of change based on a Monte Carlo simulation of random placement (solid curve). Only about 3% of the realizations had alongshore change extents less than or equal to the observed 1153 m, suggesting observed failures tended to reoccur at some locations.

in both space and time. That is, the observed failures may be part of a progressive failure (Bjerrum, 1967; Bishop, 1971; Petley et al., 2005), or sequence of successive coastal failures (e.g. Hutchison, 1969; Brunsden and Jones, 1976; Alveirinho Dias and Neal, 1992; Collins and Sitar, 2008; Young et al., 2009a) where an initial failure may result in adjacent unstable rock masses (Chowdhury et al., 2010). Rosser et al. (2007) suggested that small failures preceded larger events at the same and nearby locations. Lim et al. (2010) emphasized that

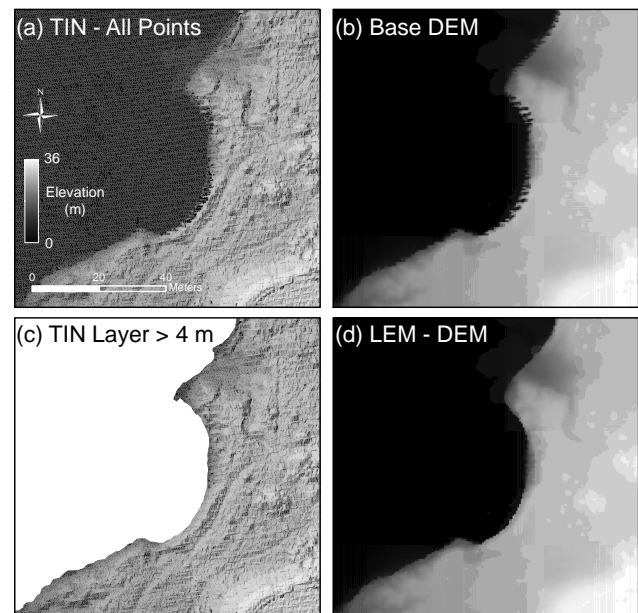
sequential failures are a “connected process“, and stressed the importance of including non-random events in coastal cliff erosion models. The random simulation over-prediction of maximum cumulative retreat suggests that a large failure is relatively unlikely to be followed by more large failures at the same location over short time periods. All locations that retreated at least 6.9 m during one time interval did not retreat in any other interval. Longer data sets are required to test these preliminary suggestions.

#### 4.6 Temporal distribution of cliff retreat

Relationships between erosional processes or failure triggering events (waves, rainfall, and seismicity) and cliff retreat could not be established statistically. Although the most cliff retreat and rainfall both were in Interval 2, the second largest amount of retreat occurred during time Interval 1, when rainfall was relatively light (Table 1, Fig. 4). The retreat in Interval 1 might have resulted from wave action, however Intervals 4, 6, and 7, had similar wave conditions with relatively little cliff retreat. Heavy rainfall in Interval 2 might have triggered failures that would have otherwise occurred from wave action in subsequent time intervals, resulting in abnormally large cliff retreat during Interval 2 and low retreat afterwards. Longer data sets are required to confirm the suggestion that, in these slowly retreating cliffs, non-random failure sequences serve to decouple failures from local environmental forcing. In the comparatively softer, more erosive cliffs in northern San Diego County, cliff erosion and rainfall in the study period were well correlated (Young et al., 2009b).

### 5 Summary

This cliff failure inventory provides the basic statistics of cliff edge retreat caused by medium and large size planimetric cliff changes along 7.1 km of unprotected rocky coastal cliffs over 5.5 years. Footprint areas of the 130 individual cliff edge failures ranged between 3 and 268 m<sup>2</sup>. On this short (5.5 year) time scale, “no change” was the most common observation (84% of the cliff edge). Probability distributions of non-zero cliff retreat during each time interval usually had a single peak between 1 and 2.5 m. Intervals with high mean retreat had elevated numbers of failure in all class sizes, and also contained the largest individual retreats. Small and medium failures tended to reoccur preferentially (relative to randomly) near previous small and medium failures, forming short-term hot spots. Large failures were less likely than random to reoccur near previous large failures, but longer records are needed to confirm this statistically tentative result. Cumulative distributions of failure parameters (area, retreat, and length) follow an inverse power-law for medium to large size events and roll off for (poorly sampled) small events, similar to previously reported distributions of coastal and inland mass movements.



**Fig. A1.** Example of the “Layered Elevation Mosaic” – Digital Elevation Model (LEM-DEM) technique. **(a)** Initial TIN created from all points and the associated DEM **(b)**, showing how points collected in seacaves and notches produce pits and a jagged, incorrect cliff edge. **(c)** A TIN layer produced from points greater than 4 m in elevation, showing the removal of seacave and notch points. **(d)** The final LEM-DEM which has eliminated the over vertical surfaces while maintaining the complex cliff topography and a well-defined cliff edge.

## Appendix A

### LEM-DEM

Simple interpolation of the lidar point data can produce pits and a faulty cliff edge (Fig. A1a and b). These problems were alleviated using an automated method termed here as a Layered Elevation Mosaic (LEM). The method consists of (1) sorting the point data by elevation into a series of layers, where each layer is assigned an increasing minimum elevation, (2) creation of triangulated irregular networks (TIN) for each layer, (3) conversion of each TIN to a DEM, and (4) creating a mosaic of all the DEM layers by maximum elevation. For this study, the elevation layers were incremented by 3 m. For example, the elevation range for the layers were: minimum–maximum (layer 1, base layer, Fig. A1b), 1-m maximum (layer 2), 4-m maximum (layer 3, Fig. A1c), 7-m maximum (layer 4), and so on. After triangulating each point layer, facets with edges longer than 2 m were removed to maintain coverage only in areas with satisfactory point density. Next, each TIN layer was converted into a 0.5-m resolution DEM with a “natural neighbors” interpolation. The boundaries of each DEM were assigned prior to the interpolation to ensure cell alignment

between each DEM. Lastly, the final LEM-DEM (Fig. A1d) was produced by selecting the maximum grid cell elevation from all the DEM layers.

**Table A1.** Landslide attributes.

Time Interval	Area (m <sup>2</sup> )	Along-shore Length (m)	Mean Transect Retreat (m)	Max Transect Retreat (m)	UTM Northing	UTM Easting
1	80.75	17.00	4.81	6.26	3 621 773	475 949
1	8.25	6.00	1.39	2.46	3 620 899	475 815
1	18.5	8.00	2.42	3.94	3 620 832	475 828
1	18.5	11.00	1.73	2.74	3 620 120	475 980
1	20	11.00	1.83	2.68	3 620 109	475 985
1	15.25	8.00	1.99	3.02	3 619 375	475 995
1	17.25	8.00	2.19	3.36	3 619 198	476 046
1	10	6.00	1.86	2.78	3 617 575	476 211
1	11	7.00	1.57	2.50	3 617 430	476 287
1	11	8.00	1.38	1.50	3 617 421	476 287
1	26.25	11.00	2.41	4.00	3 617 112	476 367
1	15	7.00	2.17	3.57	3 616 717	476 552
1	205.5	44.00	4.75	9.94	3 616 625	476 531
1	26	12.00	2.26	3.41	3 616 150	476 696
1	8.75	7.00	1.31	2.02	3 616 081	476 737
1	29.5	14.00	2.04	3.54	3 615 501	476 868
1	19.5	8.00	2.32	3.73	3 615 281	476 886
1	35.75	10.00	3.75	5.22	3 615 203	476 940
1	7	6.00	1.17	1.71	3 615 153	476 991
1	16.75	11.00	1.48	2.11	3 614 866	477 026
1	6.5	4.00	1.49	2.55	3 614 425	477 038
1	10	4.00	2.41	3.73	3 615 279	476 893
1	22.75	13.00	1.75	3.03	3 622 296	476 107
1	15.25	7.00	2.31	3.35	3 615 148	476 995
2	15	7.00	2.21	3.53	3 621 382	475 955
2	34.5	16.00	2.12	3.07	3 621 219	476 017
2	4.25	3.00	1.37	1.54	3 617 366	476 311
2	6.25	6.00	1.08	2.32	3 617 346	476 305
2	3.75	3.00	1.15	1.77	3 617 194	476 309
2	11.75	8.00	1.72	2.34	3 617 193	476 313
2	32.25	11.00	2.92	4.40	3 614 656	477 024
2	3.25	4.00	0.75	1.19	3 615 991	476 687
2	14	8.00	1.76	2.37	3 621 903	476 018
2	6	7.00	0.76	1.15	3 619 217	476 037
2	13	8.00	1.56	2.25	3 618 706	476 052
2	23	12.00	1.88	2.53	3 618 347	476 090
2	19	11.00	1.78	3.02	3 618 328	476 099
2	22.25	14.00	1.60	3.61	3 617 505	476 200
2	16.75	11.00	1.69	4.08	3 617 097	476 400
2	39.75	21.00	1.90	3.66	3 616 842	476 569
2	7	4.00	1.61	2.34	3 615 232	476 960
2	9.5	7.00	1.25	1.88	3 615 227	476 953
2	8	6.00	1.26	2.96	3 614 659	477 013
2	17.75	13.00	1.41	2.30	3 618 233	476 089
2	19.75	11.00	1.82	2.75	3 615 492	476 866
2	12.25	9.00	1.50	2.59	3 614 579	477 056
2	6	4.00	1.71	2.56	3 619 631	475 982
2	268.25	68.00	3.93	7.13	3 617 464	476 268
2	44.5	21.00	2.16	4.73	3 615 213	477 001
2	9	6.00	1.77	3.50	3 614 801	477 014
2	20.75	9.00	2.59	3.76	3 614 587	477 058
2	11.75	6.00	2.01	3.67	3 614 500	477 048
2	13.5	9.00	1.63	3.03	3 619 646	475 978
2	7.25	6.00	1.17	1.50	3 619 223	476 034
2	155	27.00	5.76	7.14	3 621 898	476 009
2	97	24.00	4.08	7.00	3 621 479	475 941
2	9.5	8.00	1.13	2.00	3 621 404	475 927
2	13	6.00	2.25	2.63	3 620 826	475 838
2	10	6.00	1.59	2.41	3 620 653	475 875
2	4.5	2.00	2.37	2.63	3 619 522	475 989
2	21.5	12.00	1.86	3.61	3 619 336	476 003
2	15	9.00	1.69	2.53	3 619 189	476 052
2	28.75	13.00	2.14	3.41	3 619 180	476 057
2	17.25	10.00	1.85	2.99	3 619 129	476 068
2	9	10.00	0.83	1.51	3 618 989	476 076
2	45.5	17.00	2.68	4.51	3 618 492	476 061
3	7.25	5.00	1.68	2.52	3 618 459	476 046
3	6.25	6.00	1.01	1.99	3 618 436	476 063
3	4.5	4.00	1.22	1.78	3 618 262	476 098
3	6.25	5.00	1.20	2.64	3 618 248	476 090
3	8.75	5.00	1.81	2.38	3 617 471	476 229
3	6.25	5.00	1.27	1.94	3 617 467	476 265
3	11	8.00	1.56	2.50	3 617 239	476 295
3	21.75	13.00	1.74	2.64	3 617 165	476 328
3	12	7.00	1.73	2.45	3 617 115	476 366
3	7.75	6.00	1.43	2.01	3 617 073	476 405
3	26.25	9.00	2.96	5.79	3 616 914	476 517
3	9.5	7.00	1.43	2.17	3 616 689	476 549
3	38.25	18.00	2.26	3.16	3 616 328	476 599
4	4.5	6.00	0.66	0.79	3 616 169	476 678
4	9	5.00	1.76	2.53	3 616 161	476 688
4	8	5.00	1.75	2.38	3 616 158	476 693
4	54	20.00	2.74	4.74	3 616 078	476 739
4	14.5	9.00	1.81	2.64	3 615 980	476 733
4	12.75	8.00	1.71	3.16	3 615 477	476 856
4	13.5	10.00	1.35	2.50	3 615 216	476 987
4	3.75	4.00	0.94	1.69	3 615 143	476 998
4	15	7.00	2.31	3.46	3 614 897	477 011
4	3.5	4.00	0.97	1.72	3 614 652	477 025
4	7.5	8.00	0.88	2.01	3 614 426	477 042
4	8.5	8.00	1.09	1.88	3 622 302	476 107
4	14.25	10.00	1.32	2.63	3 622 286	476 112
4	12	8.00	1.68	3.20	3 616 142	476 700
4	6.75	5.00	1.51	2.21	3 615 042	476 995
4	11.5	8.00	1.42	2.54	3 617 289	476 308
4	5.25	4.00	1.50	2.01	3 615 198	477 013
4	24.5	6.00	4.34	5.93	3 621 637	475 947
4	4	5.00	0.85	1.64	3 621 631	475 943
4	4.25	4.00	1.04	1.56	3 621 203	476 024
4	16.5	11.00	1.40	3.25	3 619 591	475 978
5	9.75	8.00	1.24	2.11	3 618 382	476 072
5	94.5	29.00	3.32	4.82	3 616 983	476 486
5	54.5	18.00	3.03	4.01	3 616 091	476 734
5	8.25	6.00	1.27	1.89	3 615 208	476 977
5	5	5.00	1.50	3.00	3 615 044	476 995
5	7.25	4.00	1.50	2.00	3 614 885	477 010
5	3.75	5.00	0.81	1.45	3 614 422	477 043
5	3.25	3.00	1.08	1.52	3 614 604	477 056
6	31.25	15.00	2.04	4.31	3 619 220	476 033
6	46.5	17.00	2.83	5.38	3 621 899	476 006
6	17.25	9.00	2.00	3.00	3 620 624	475 899
6	8.5	6.00	1.53	2.72	3 620 215	475 932
6	125.25	38.00	3.25	5.99	3 619 771	476 019
6	13.25	7.00	1.88	2.61	3 619 188	476 055
6	6.25	6.00	0.98	1.77	3 618 732	476 053

6	11.25	6.00	1.92	2.00	3 618 307	476 106
6	25.25	14.00	1.82	2.57	3 618 255	476 092
6	25	9.00	2.71	4.05	3 617 805	476 159
6	10.5	7.00	1.50	2.12	3 617 556	476 216
6	13	7.00	1.77	2.53	3 617 300	476 307
6	30.25	11.00	2.90	5.43	3 616 411	476 588
6	3	3.00	1.17	1.50	3 616 387	476 600
7	28	16.00	1.70	2.52	3 616 061	476 739
7	6.75	5.00	1.34	2.70	3 616 058	476 733
7	42.75	18.00	2.56	3.65	3 614 797	477 010
7	26	14.00	1.93	3.39	3 614 659	477 017
7	10.25	8.00	1.19	1.50	3 614 436	477 038
7	8.75	8.00	1.06	1.50	3 614 393	477 056
7	10.25	8.00	1.31	2.25	3 621 763	475 952
7	4	4.00	0.97	1.34	3 615 484	476 865

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