

## Technical Note:

### Practical considerations on the use of down-sized time-domain reflectometry (TDR) probes

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#### Abstract

Nine time-domain reflectometry (TDR) probes, 2 to 10 cm long, were evaluated by comparing their measurement accuracy of TDR-pulse travel time in a sand and sandy loam soil, and electrical conductivity in NaCl solutions. TDR probes <2.5 cm in length generated trough-shaped TDR waveforms with rounded corners at the points of the pulse reflection from the probe ends. The sharpness of the pulse reflection on the waveforms increased with both the increasing probe length and soil-water content. The transition time for the propagation of TDR pulse at the probe entrance increased as the soil dried up. The increased transition time caused a rightward movement of the first peak of the waveform at the probe entrance. Because of such peak movement, TDR-support software algorithm determined travel path of TDR pulse through the probe that was smaller than the actual travel path. TDR-measured pulse travel time  $t_{\text{TDR}}$  varied erratically with the predicted pulse travel time  $t_g$  (from volumetric soil-water content) for the probes <2.5 cm in length. But, for all probes  $\geq 2.5$  cm in length,  $t_{\text{TDR}}$  varied linearly with  $t_g$  and followed the 1:1 line. TDR could not measure  $t_{\text{TDR}} < 300$  ps accurately. A minimum probe length  $L_{\text{min}}$  and the lowest allowable soil-water content  $q_{\text{min}}$  that the probe can accurately measure govern this lowest pulse travel time  $t_{\text{min}}$ . The mean absolute deviation between  $t_{\text{TDR}}$  and  $t_g$  was 77 ps for the 2.3 cm long probe and 1.39 ps for all probes  $\geq 2.5$  cm in length. All probes  $\geq 2.5$  cm in length measured electrical conductivity of salt solutions  $s_{\text{TDR}}$  that compared well with the electrical conductivity measured by a conductivity meter  $s_m$ . The length of the probes did not exert any noticeable influence on the accuracy of electrical conductivity measurement.

**Keywords:** TDR probe, pulse travel time, dielectric constant, electrical conductivity

#### Introduction

In spite of significant advances in the practical techniques and conceptual understanding of the time-domain reflectometry (TDR) technique over the last two decades, the TDR probe length currently used, usually above 10 cm, has limited the application of TDR in small-scale measurements such as in the laboratory study of water flow and solute transport in small columns. Using a 5 cm long probe, Topp *et al.* (1984) obtained considerably lower soil-water content by a compared with the gravimetric measurement and described the error in TDR-measurement in relation to the measurement accuracy of the TDR pulse travel time. Heimovaara (1993) reported increase in rise time of the reflected TDR pulse for probes <5 cm in length when used with coaxial cables >3.2 m and he did not use these

probes. Pulse rise time is defined as the time required for a TDR pulse to rise from 10% to 90% of its final value. Transition time of a TDR pulse defined by the time between the beginning of transition of the reflected pulse and 50% of the final value after complete reflection has also been described as a dominant error in measuring the travel time of the pulse (Hook and Livingston, 1995). The transition time is caused by the interaction of the energy of the high frequency TDR pulse with soil. Taking into account all these factors attempts were made in recent years to downsize TDR probes (1) by increasing clarity of the reflected signal using high bandwidth TDR system (Kelly *et al.*, 1995), (2) by improving the technique of waveform analysis (Yanuka *et al.*, 1988; Wraith *et al.*, 1993), and (3) by especially laying

out long probe rods on a short support material (Nissen *et al.*, 1998,1999).

Kelly *et al.* (1995) used an expensive 20 GHz digital sampling oscilloscope that generated TDR pulses with 25 ps rise time. This oscilloscope displayed clear waveforms with sharp reflections at the ends of the probe and allowed use of probes as small as 2.5 cm long. Malicki *et al.* (1992) reported using 5.4-cm long probes with a TDR moisture meter operating with a pulse of 250 ps rise time. Neither of these two TDR systems was more popular among users than the Tektronix 1500 series TDR cable testers. Dalton and van Genuchten (1986) and Keng and Topp (1983) used Tektronix cable tester and experimentally found 10 cm as the practical lowest length of probe with a  $\pm 0.02 \text{ m}^3 \text{ m}^{-3}$  uncertainty in the measured water content over the entire range of soil-water content. They could, however, use shorter probes in soil with high water content. Amato and Ritchie (1995) claimed to obtain reliable determination of soil-water content over  $0.07 \text{ m}^3 \text{ m}^{-3}$  using a 2.1 cm long probe. The clarity of the waveforms that they interpreted (e.g., their Fig.3) for this determination was very poor. This raises concern about the interpretation of such waveforms, especially manually, obtaining accurate travel time or travel path of the pulse. Amato and Ritchie (1995) did not evaluate their probe by determining soil-water content using TDR-support software, which is now an obvious requirement for most TDR applications. Nissen *et al.* (1998) constructed a 1.5 cm long probe by winding coils on a core material. This coil probe was coated to prevent penetration of water between the windings of the coil and, therefore, could not measure electrical conductivity of soil. Nissen *et al.* (1999) introduced a printed circuit board probe in which a 3-line serpentine wave guide was produced in a copper cladding of a circuit laminate, 5 cm long, 1 cm wide, and 0.064 to 0.1 cm thick. Being a plate, this probe could be installed only along the water flow lines. Both probes of Nissen *et al.* (1998) and Nissen *et al.* (1999) needed additional calibration and produced unusual shape waveforms that most software could not analyse.

Only limited successes have so far been achieved in using small TDR probes for measuring dielectric constant and soil-water content, occasionally under specific conditions. The measurement of electrical conductivity with small probes was ignored in most studies. This study investigated the performance of small probes in measuring TDR pulse travel times in soils and electrical conductivity of salt solutions using a Tektronix 1502C cable tester and TDR support software, called WinTDR99, developed by Or *et al.* (1999). The objective was to identify the factors that control the length of TDR probes and the limiting values of the factors to obtain accurate TDR measurements with small probes.

## Materials and methods

### DIELECTRIC CONSTANT, SOIL-WATER CONTENT, AND TDR WAVEFORM MEASUREMENT

Nine 3-rod probes, 2 to 10 cm long, were constructed using 0.1-cm diameter stainless steel rod and 350 cm long RG-58A/U coaxial cable of resistance 50 W. The probe head consisted of 1-cm thick, 0.8-cm wide and 1.8-cm long acrylic block. The centre-to-centre spacing between the two outer rods was 1.1 cm and that between the central and outer rods was 0.55 cm. Before using these probes for measurement in soil, they were first calibrated in pure water with its known dielectric constant (78.39 at 25 °C) using WinTDR99. This calibration was necessary to determine the effective length of the probes for accurate measurement of TDR pulse travel time. During the calibration, the point of initial reflection of the pulse from the probe entrance was identified for all probes.

The bottom 4 cm of an acrylic column, 5-cm long, 5-cm inner diameter, and the base closed with a ceramic plate, was filled with air-dry sand. One TDR probe was inserted in the sand 2 cm above the bottom of the column keeping the three rods of the probe in a horizontal plane. The sand was saturated from the bottom of the column using a Mariotte bottle. Step-wise suctions ranging from 0 to 150 cm of water were applied at the bottom of the column using a hanging water column to drain the sand. The drainage water was collected for each suction until equilibrium condition in the sand was reached. The dielectric constant of the sand and TDR waveform were recorded for each step of suction at equilibrium using WinTDR99 (both for the fixed initial reflection at its location obtained in pure water and for the relocated initial reflection in each measurement). The measurement was continued until soil-water content decreased to such an extent that the program algorithm failed to analyse the waveform properly. After all measurements had been made, the water content of the sand was determined gravimetrically by drying it at 105°C for 24 hrs and was converted to volumetric water content,  $\theta_v$ . This experiment was carried out using 2.0, 2.3, 2.5, 3.0, 3.5, 4.0, 4.5, 4.8, and 10.0-cm long probes in sand as well as in a sandy loam soil. In the case of the 10-cm long probe, the diameter of the soil column was 10 cm. The experiments were repeated three times for each probe at a constant room temperature of  $25 \pm 1^\circ\text{C}$ .

The algorithm of WinTDR99 first estimates the length of travel path of the TDR pulse through the probes using the point of initial and final reflections of the pulse. Unlike other TDR-support softwares, WinTDR99 draws two tangent lines at the inflection points of the waveforms on either side of the first peak at the probe entrance and assumes the initial

reflection at the intersection of these tangent lines. The point of final reflection is located at the intersection of a tangent passing through the inflection point on the waveform after the local minimum and a tangent passing through the local minimum. The inflection points are located at the largest positive and the largest negative first derivatives of the waveforms around the points of reflection. The travel time of the TDR pulse  $t$  (s) in a probe of length  $L$  (m) and the dielectric constant of the surrounding media  $\epsilon$  are related by electro-dynamic equation as:

$$t = \frac{L\sqrt{\epsilon}}{c} \quad (1)$$

where  $c$  is the velocity of TDR pulse in free space ( $3 \times 10^8$  m s<sup>-1</sup>). The dielectric constant  $\epsilon$  and volumetric water content  $\theta$  for the sand and sandy loam soil are related by the equation of Topp *et al.* (1980) given by:

$$\epsilon = 3.03 + 9.3\theta + 146\theta^2 - 76.7\theta^3 \quad (2)$$

The first derivatives of the waveforms were calculated to check the clarity of the inflection points on the waveforms for all probes. The travel time of the TDR pulse  $t$  was calculated from  $\epsilon$  using Eqn. 1 and was denoted by  $t_{\text{TDR}}$  (ps), called the measured pulse travel time. In addition to  $t_{\text{TDR}}$ , the pulse travel time was predicted independently from the gravimetrically measured soil-water content  $\theta_g$  using Eqns. 2 and 1 and was denoted by  $t_g$  (ps). The predicted travel times  $t_g$ , considered to be an accurate estimate of  $t$ , were compared with  $t_{\text{TDR}}$  to evaluate the accuracy of TDR measurements for different probes at different water contents.

#### ELECTRICAL CONDUCTIVITY MEASUREMENT

The thin-section approach of Giese and Tiemann (1975) was used in WinTDR99 to calculate electrical conductivity  $\sigma$  (dS m<sup>-1</sup>) by analysing TDR waveforms. The governing equation is given by:

$$\sigma = \frac{10\epsilon_0 c}{L} \frac{Z_0}{Z_u} \left( \frac{2V_0}{V_f} - 1 \right) \quad (3)$$

where  $\epsilon_0$  is the dielectric permittivity of free space ( $8.9 \times 10^{-12}$  F m<sup>-1</sup>),  $Z_0$  the characteristic impedance of the probe ( $\Omega$ ),  $Z_u$  the output impedance of the TDR cable tester (50  $\Omega$  for Tektronix 1502C),  $V_0$  the incident pulse voltage,  $V_f$  the reflected pulse voltage after multiple reflections were suppressed, and  $c$  and  $L$  are as described before. The algorithm of WinTDR99 selected  $V_0$  and  $V_f$  from the waveforms.  $Z_0$  was determined in a separate calibration by

immersing the probes in pure water and using its known dielectric constant  $\epsilon_w$  (78.39 at 25°C) according to:

$$z_0 = Z_u \sqrt{\epsilon_w} \left( \frac{V_1}{2V_0 - V_1} \right) \quad (4)$$

where  $V_1$  is the minimum voltage on the TDR waveform between the initial and final reflections of the pulse from the two ends of the probe and was obtained from the waveforms.

Nine NaCl solutions, 0.001 to 0.1M, were prepared and kept at 25±1°C for 48 hours to achieve homogeneous salt solutions. The electrical conductivity of these solutions was measured first by a HORIBA ACT D-20 digital conductivity meter of Horiba Jobin, Yvon Co., Ltd., Japan and then by all TDR probes  $\geq 2.5$  cm in length. The other two probes,  $<2.5$  cm in length, were not used for electrical conductivity measurement since they could not be used to measure soil-water content.

## Results and discussion

#### WAVEFORM EVALUATION

TDR probes  $<2.5$  cm in length provided trough-shaped waveforms with rounded corners over the entire range of soil-water content. These waveforms had no well-defined sharp reflections from the probe ends. Figure 1 shows three waveforms for the 2 cm long probe and three waveforms for the 4 cm long probe.

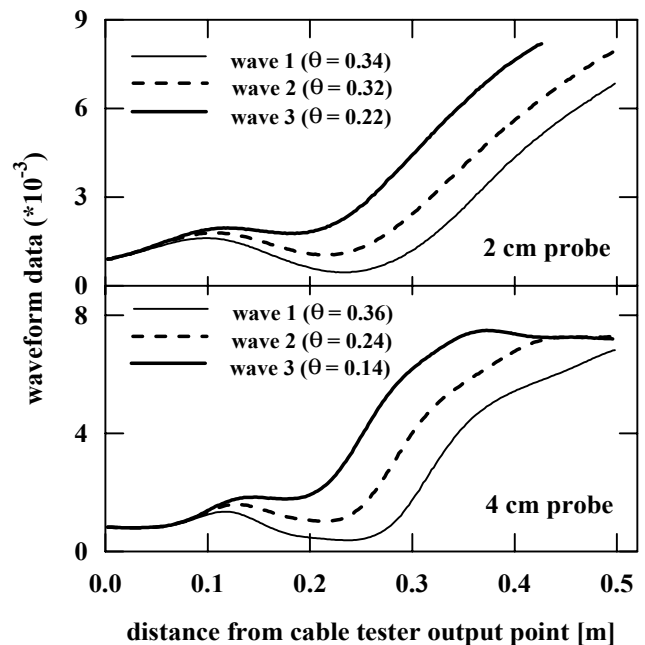


Fig. 1. TDR waveforms retrieved for three different soil-water contents in sand for a 2 cm and 4 cm long probe.

for the 4 cm long probe retrieved in sand. The soil-water content was 0.34, 0.32 and 0.22  $\text{m}^3 \text{m}^{-3}$  for the waveform 1, 2 and 3, respectively for the 2 cm long probe and 0.36, 0.24 and 0.14  $\text{m}^3 \text{m}^{-3}$ , respectively for the 4 cm long probe. The combined effects of the large rise time ( $\leq 200$  ps, Tektronix, 1987) and the large transition times of the TDR pulse for small travel times in the small probes caused trough-shaped waveforms.

The TDR system operates on a frequency bandwidth, which is the range of frequencies from zero to the highest frequency component of the TDR signal that the instrument can measure. The frequency bandwidth is inversely proportional to the rise time of the TDR pulse (Oliver and Cage, 1971, p.372-373). A small rise time of the TDR pulse causes sharp reflections from the ends of a probe and generates a clear signal. The travel time of the TDR pulse through the 2 cm long probe came close to or shorter than the rise time of the reflected pulse depending on the soil-water content (Eqn.1). The short travel time of the pulse made the points of reflection on the waveform from the ends of the probe unclear (Lancaster, 1992). The accuracy of measurement of the TDR cable tester also limits the clarity of the reflected waveforms. Figure 1 reveals that the sharpness of the reflection of the TDR pulse increases both with the increasing probe length and soil-water content. Figure 2 illustrates the three-point moving average of the first derivatives of the waveforms presented in Fig. 1. The

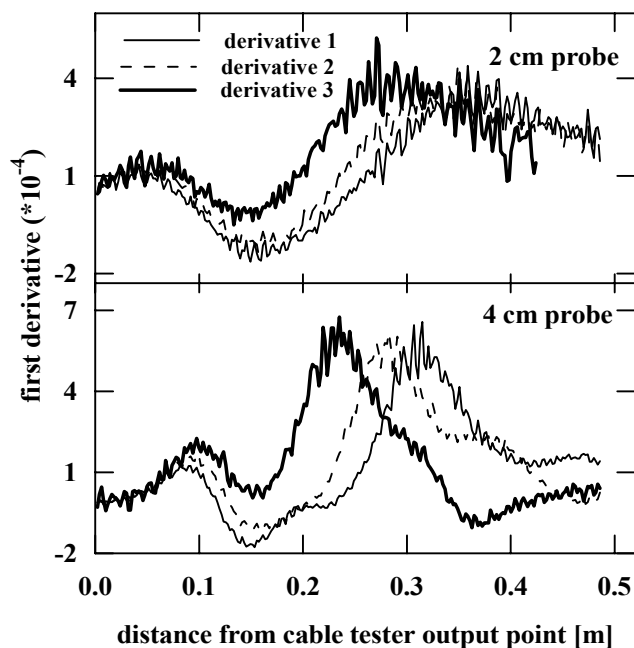


Fig. 2. First derivatives of the TDR waveforms shown in Fig. 1 for the 2 cm and 4 cm long probes.

peaks on the first derivatives represent the inflection points of the waveforms and were more rounded for the 2 cm long probe than for the 4 cm long probe. Sharp inflection points on the first derivatives of the waveforms are always needed to determine the initial and final points of reflection of the TDR waveforms accurately by a program algorithm.

It was noticed that the first peak of the waveform and the two inflection points around it that are located at the largest positive and the largest negative first derivatives, moved rightward with decreasing soil-water content in all experiments. The movement of the first peak can be visualised in Fig. 1 and that of the inflection points is estimated for the 4 cm long probe in Fig. 2. Consequently, the point of the initial reflection of the waveform also moved rightward as the soil dried up due to the increased transition time of the pulse as it entered from the probe head to the probe rod.

#### PULSE TRAVEL TIME EVALUATION

The travel time of the TDR pulse through a particular probe is a function of the dielectric constant of the surrounding soil (Eqn. 1), and it decreased as soil-water content decreased. Figure 3(a) (top half) illustrates the variation of the measured pulse travel time  $t_{\text{TDR}}$  with the predicted pulse travel time  $t_{\text{g}}$  in sand and sandy loam soil for the 2.3 cm and 4.0 cm long probes. The measured pulse travel time  $t_{\text{TDR}}$  varied erratically with  $t_{\text{g}}$  for all probes  $< 2.5$  cm in length and consistently for all probes  $\geq 2.5$  cm in length. For the 2.3-cm long probe,  $t_{\text{TDR}}$  was large when the soils were saturated but decreased sharply in response to a small decrease in soil-water content. Then  $t_{\text{TDR}}$  decreased gradually with further decrease in soil-water content until the program algorithm failed to analyse the waveforms at certain low water content. This behaviour of  $t_{\text{TDR}}$  can be explained in terms of the length and wall effects of the probe. The sampling volume of TDR was small for the small probes and the pore water interacted with the probes in the same way as it interacted with the soil particles. This caused jumps in the measured pulse travel time by TDR as the soil dried or wetted. At certain low soil-water content, the base of the TDR waveform moved up above its first peak (as estimated in Fig. 1) and the program algorithm could not draw a proper tangent at the base of the waveform and failed to analyse the waveform properly. This situation occurred for all nine probes below certain limiting soil-water content specific to the length of the probe. For all probes  $\geq 2.5$  cm in length,  $t_{\text{TDR}}$  varied linearly with  $t_{\text{g}}$  both in sand and sandy loam soil as illustrated in Fig. 3a (top) for the 4.0 cm probe.

Figure 3b (bottom) visualises a comparison between  $t_{\text{TDR}}$  measured under two different treatments of the initial

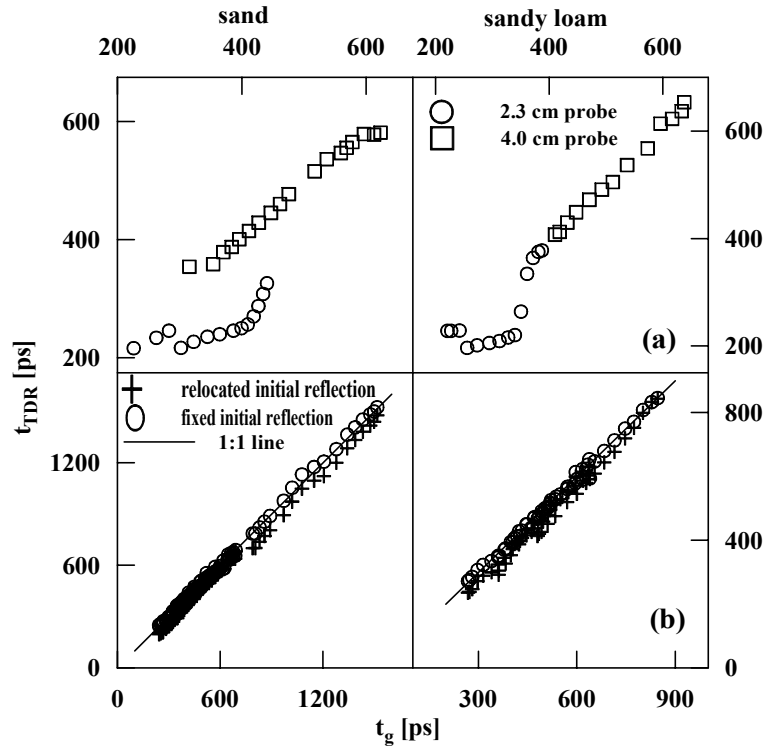


Fig. 3. Relationship between TDR-measured pulse travel time  $t_{TDR}$  and predicted pulse travel time  $t_g$  in sand and sandy loam soil for: (a) the fixed initial reflection of the TDR pulse on the waveforms of 2.3 cm and 4 cm long probes and (b) both fixed and relocated initial reflection of the TDR pulse on the waveforms of all probes = 2.5 cm in length.

reflection (fixed and relocated) and  $t_g$  for all probes  $\geq 2.5$  cm in length. TDR underestimated  $t_{TDR}$  over the whole range of soil-water content when the point of initial reflection on the waveforms was relocated. The deviation between  $t_{TDR}$  and  $t_g$  increased with decreasing  $t_g$ . This result suggests fixing the initial reflection of the TDR pulse when TDR measurement is intended by using WinTDR99. For the fixed initial reflection of the pulse on the waveform,  $t_{TDR}$  varied linearly with  $t_g$  for all probes  $\geq 2.5$  cm in length and followed the 1:1 line both in sand and sandy loam soil (Fig. 3(b)). The coefficient of determination of this linear relationship was  $r^2 = 0.998$  for sand (no. of observation = 111) and 0.995 for sandy loam soil (no. of observation = 57). The 1:1 relationship between  $t_{TDR}$  and  $t_g$  with a slope of 1.010 (SE =  $\pm 0.0043$ ) for sand and 1.001 (SE =  $\pm 0.0097$ ) for sandy loam soil ensured that TDR measured the pulse travel time accurately with the probes  $\geq 2.5$  cm in length when the point of initial reflection was kept fixed.

The mean absolute deviation between  $t_{TDR}$  and  $t_g$  was 77 ps for the 2.3 cm long probe and 1.39 ps for all probes  $\geq 2.5$  cm in length. These results indicate the failure of the small probes,  $< 2.5$  cm, in the measurement of pulse travel time in soils. Amato and Ritchie (1995) quantified the error in travel

time measurement in air using short-circuited probes ranging from 1 to 15 cm in length. They obtained high coefficients of variation (2.8 – 7.3%) for travel times  $< 100$  ps and relatively low ( $< 3\%$ ) values for higher travel times. Assuming the dielectric constant of air = 1 and the velocity of TDR pulse in air =  $3 \times 10^8$  m s $^{-1}$ , Eqn. (1) results in a 100 ps pulse travel time from a 3-cm long probe. Thus, the accuracy criterion in the observation of Amato and Ritchie (1995) further confirms the results stated above.

Since TDR cable tester measures the pulse travel time  $t_{TDR}$  through the probes to estimate  $\epsilon$  and  $\theta$  based on Eqns. (1) and (2), respectively, it is assumed that there is a minimum measurable travel time of the pulse  $t_{min}$  for a particular length of a probe  $L$  and dielectric constant of the soil  $\epsilon$ . When the travel time  $t$  ( $= L\sqrt{\epsilon}/c$  in Eqn. 1) becomes greater than  $t_{min}$ , which would be possibly close to the rise time of the pulse (200 ps), the TDR measurement of  $\epsilon$  and  $\theta$  will be accurate. For a particular  $L$  and  $t_{min}$ ,  $\epsilon_{min}$  can be given based on Eqn 1, and Eqn. 2 gives the corresponding minimum water content  $\theta_{min}$ . Roughly speaking, it was observed that TDR could not measure accurately the pulse travel time  $< 300$  ps (Fig. 3) that was close to the rise time of the pulse (200 ps). In practical measurements, this

approximate lowest travel time could be obtained for various combinations of probe length and soil-water content. Assuming  $t_{\min} = 300$  ps, it is possible to determine the lowest measurable  $q$  for a particular length of the probe  $L$  greater than 2.5 cm by:  $\theta > f(L)$ ; ( $L \geq 2.5$  cm). However, it should be noted that these smallest probes would measure  $\varepsilon$  accurately but the accuracy in the determination of  $\theta$  would depend on the accuracy of  $\varepsilon - \theta$  relationship such as Eqn. 2.

#### COMPARISON OF ELECTRICAL CONDUCTIVITY

Figure 4 illustrates the relationship between the TDR-measured electrical conductivity of NaCl solutions  $\sigma_{\text{TDR}}$  and the electrical conductivity measured by the conductivity meter  $\sigma_m$  for all probes  $\geq 2.5$  cm in length. The  $\sigma_m - \sigma_{\text{TDR}}$  relationship was linear in an arithmetic paper with a slope of 0.9996 (SE =  $\pm 0.0024$ ). The coefficient of determination  $r^2$  was 0.9996 (no. of observation = 70). Since the small values clustered together, log-log scale was used to show them clearly. At very low electrical conductivity of the solutions,  $\sigma_m < 0.2$  dS m $^{-1}$  for tap water, TDR underestimated electrical conductivity. The observed 1:1 relationship between the two independently measured electrical conductivities showed the applicability of the probes to measure electrical conductivity. The length of the probe did not influence the accuracy of measurement.

#### Summary

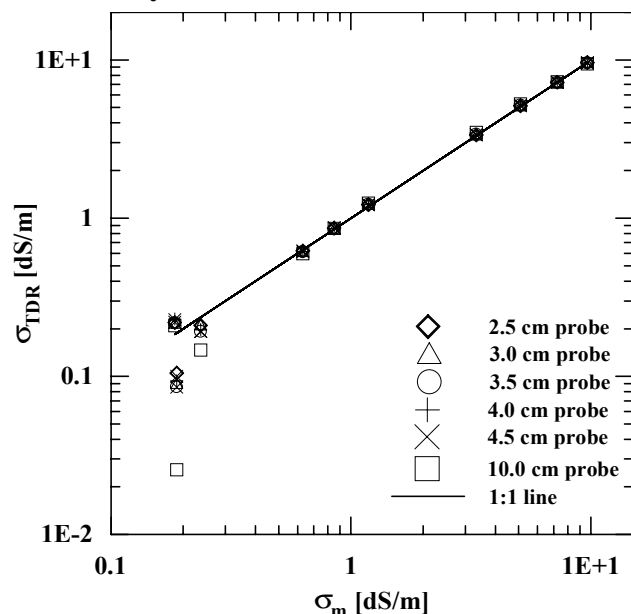


Fig. 4. Relationship between electrical conductivity of salt solutions measured by TDR probes  $\geq 2.5$  cm in length  $s_{\text{TDR}}$  (dS m $^{-1}$ ) and electrical conductivity of the same salt solutions measured by a conductivity meter  $s_m$  (dS m $^{-1}$ ). The  $s_m - s_{\text{TDR}}$  relationship was linear in an arithmetic paper; the purpose of using log-log scale is to show the small values clearly.

Small TDR probes,  $< 2.5$  cm long, provided trough-shaped waveforms with rounded corners at the points of their reflection from the probe ends due to the combined effect of the rise time and large transition time of the TDR pulse. The sharpness of the reflection point on the waveform increased both with the increasing probe length and soil-water content. The transition time of the TDR pulse at the probe entrance increased with decreasing soil-water content and caused a rightward movement of the first peak of the waveform at the probe entrance. Consequently, the algorithm of WinTDR99 determined the length of travel path of the pulse through the probes that was smaller than the actual travel path.

TDR-measured pulse travel time  $t_{\text{TDR}}$  varied erratically with the predicted pulse travel time  $t_g$  for the small probes,  $< 2.5$  cm long. For the longer probes,  $\geq 2.5$  cm in length,  $t_{\text{TDR}}$  versus  $t_g$  plot followed the 1:1 line. TDR could not measure  $t_{\text{TDR}} < 300$  ps accurately. A minimum probe length  $L_{\min}$  and the lowest allowable soil-water content  $\theta_{\min}$  that the probe can measure accurately, govern this lowest pulse travel time  $t_{\min}$ . The electrical conductivity of salt solutions measured by the probes  $\geq 2.5$  cm in length agreed well with that measured by a conductivity meter stating the suitability of the probes to measure electrical conductivity. Probe length did not influence noticeably the accuracy of electrical conductivity measurement.

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