



Attribution of hydrologic forecast uncertainty within scalable forecast windows

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Abstract. Hindcasts based on the extended streamflow prediction (ESP) approach are carried out in a typical rainfall-dominated basin in China, aiming to examine the roles of initial conditions (IC), future atmospheric forcing (FC) and hydrologic model uncertainty (MU) in streamflow forecast skill. The combined effects of IC and FC are explored within the framework of a forecast window. By implementing virtual numerical simulations without the consideration of MU, it is found that the dominance of IC can last up to 90 days in the dry season, while its impact gives way to FC for lead times exceeding 30 days in the wet season. The combined effects of IC and FC on the forecast skill are further investigated by proposing a dimensionless parameter (β) that represents the ratio of the total amount of initial water storage and the incoming rainfall. The forecast skill increases exponentially with β , and varies greatly in different forecast windows. Moreover, the influence of MU on forecast skill is examined by focusing on the uncertainty of model parameters. Two different hydrologic model calibration strategies are carried out. The results indicate that the uncertainty of model parameters exhibits a more significant influence on the forecast skill in the dry season than in the wet season. The ESP approach is more skillful in monthly streamflow forecast during the transition period from wet to dry than otherwise. For the transition period from dry to wet, the low skill of the forecasts could be attributed to the combined effects of IC and FC, but less to the biases in the hydrologic model parameters. For the forecasts in the dry season, the skill of the ESP approach is heavily dependent on the strategy of the model calibration.

1 Introduction

Reliable hydrologic forecasts are crucial in many hydrologic sectors, for example, flood control, irrigation, water supply, etc. Forecast skill is mainly affected by three factors: the uncertainty of hydrologic models used to derive the streamflow from atmospheric forcing (precipitation, temperature, etc.), the uncertainty of initial conditions of the basin at the beginning of the forecast, and the uncertainty of atmospheric forcing during the forecast horizon. These factors are referred to as the “uncertainty triplet” (Zappa et al., 2011). Examination of the three types of uncertainty and their joint impacts on the forecast skill is therefore not only beneficial for the understanding of rainfall–runoff processes, but also for facilitating hydrologic applications with process-based hydrologic models.

Previous studies revealed that the dominance of IC and FC in the hydrologic forecast skill varies with season and location (Mahanama et al., 2011, 2008; Shukla and Lettenmaier, 2011; Singla et al., 2012; Maurer and Lettenmaier, 2003). For hydrologic forecasts, IC is frequently referred to as the initial water storage (e.g., soil moisture, snow water equivalent) of the entire basin. Li et al. (2009) found that IC dominates the forecast skill with lead time of up to 1 month, where beyond that FC becomes the main contributor to the forecast skill. However, for some basins over the US, initial soil moisture contributes significantly to the forecast skills of all seasons except spring, and the contribution can last up to six months (Mahanama et al., 2011). The dominance of IC is related to the persistence of soil moisture and/or snow water equivalent (SWE). It is not surprising that SWE dominates the forecast

skill over those basins in which streamflow are mainly generated by snowmelt (Koster et al., 2010). For a short lead time (within the concentration time of the basin) or during a dry period, soil moisture is the only source of streamflow observed at the outlet of the basin (Kirkby, 1978). The persistence of IC is also affected by the future atmospheric conditions. Wood and Lettenmaier (2008) found that IC yields forecast skill for up to five months during the transition between the wet and dry seasons, but for the reverse transition, FC is critical. IC is also proved to have a stronger impact during the inter-monsoon seasons in Sri Lanka (Mahanama et al., 2008). More recently, Shukla et al. (2013) examined the relative roles of IC and FC in seasonal hydrologic forecast at a global scale. Their results are consistent with previous studies. Mahanama et al. (2011) defined a parameter κ (variance ratio of initial water storage and total rainfall within forecast period) to combine the effect of IC and FC, allowing the estimates of the potential forecast skills.

In this study, we will continue with the discussion of the impact of IC and FC on hydrologic forecast by implementing hindcasts with the ESP (extended streamflow prediction) approach (Day, 1985). In particular, due to the persistence of IC and the impact of FC, we believe that there should be certain proper time ranges which we termed as “forecast windows” (see the definition in Sect. 3), beyond which the forecast is not reliable any more. The impact of IC and FC will be discussed under the framework of the “forecast window”. In addition, we will try to combine the effect of the two factors by defining a new dimensionless parameter, based on which the relationships of forecast skill and the combined effect of IC and FC can be derived.

The third member of the “uncertainty triplet” is model uncertainty (MU). The rainfall–runoff model based forecasting approach (e.g., ESP) requires the model to provide accurate initial conditions of the basin at the beginning of the forecast. The forecast skill will undoubtedly be impaired with model uncertainty (Walker et al., 2005; Demirel et al., 2013). MU could be induced by systematic biases in model input, the structure of the model, and model parameters, etc. (Walker et al., 2005). While errors in the model input and structure may not be readily reduced, we will only focus on the uncertainty of model parameters in this study through a process of model calibration, assuming that the input as well as the model structure is robust. Shi et al. (2008) demonstrated the influence of hydrologic model calibration in the improvement of seasonal streamflow forecasting.

The analyses in Sect. 3 are based on the following hypotheses: (1) forecast skill varies with initial forecast date and forecast window; and (2) the combined effect of IC and FC determines the reliable forecast window in hydrologic forecasting. We will test these hypotheses over the upper Hanjiang River basin (UHRB) in China by examining the relative roles of IC, FC and MU on hydrologic forecast. UHRB is a typical rainfall-dominant river basin (see descriptions in Sect. 2), which is also the headwater of the south-to-north

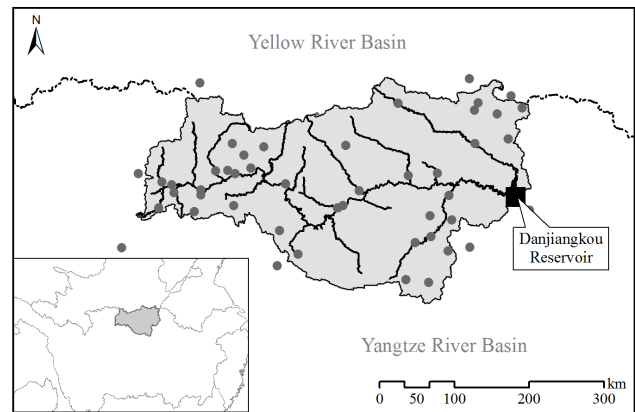


Fig. 1. Location of upper Hanjiang River basin (UHRB) in China. Dashed line is the boundary of the Yangtze River basin. The grey dots are rain gauges. The black square is Danjiangkou reservoir station.

water transfer (SNWT) project in China. This study will broaden the application fields of the ESP approach by testing its validity in rainfall-dominant rather than snow-dominant basins. The results will shed light on future application of the ESP approach in similar basins.

The paper is organized as follows. The study area and methods will be described in Sect. 2; Sect. 3 will present results, with conclusions and discussion following in Sect. 4.

2 Study area and methods

2.1 Study area

The study area is the upper Hanjiang River basin (abbreviated as UHRB below, see Fig. 1 for its geographic location), which is a sub-basin of the Yangtze River in China. The drainage area of UHRB is $9.52 \times 10^4 \text{ km}^2$. It is a typical monsoon-climate region, characterized by the summer dominant rainfall within the year and great distinctions between rainy and dry seasons (Guo et al., 2009). Figure 2 shows the intra-annual cycle of monthly rainfall and runoff averaged from 1970–2000 over UHRB. Clearly, the runoff regime in this basin is dominated by the rainfall pattern. The integral runoff from May through October (the wet-season period) accounts for about 80 % of the annual total. Based on the rainfall and runoff regimes presented in Fig. 2, we divided the water year into four stages: pre-wet season (May to July), post-wet season (August to October), pre-dry season (November and December) and post-dry season (January to April of the following year). The distinct variations of the basin state and rainfall pattern within the four stages have some implications on the forecast skill of the ESP approach, as will be discussed in the next section.

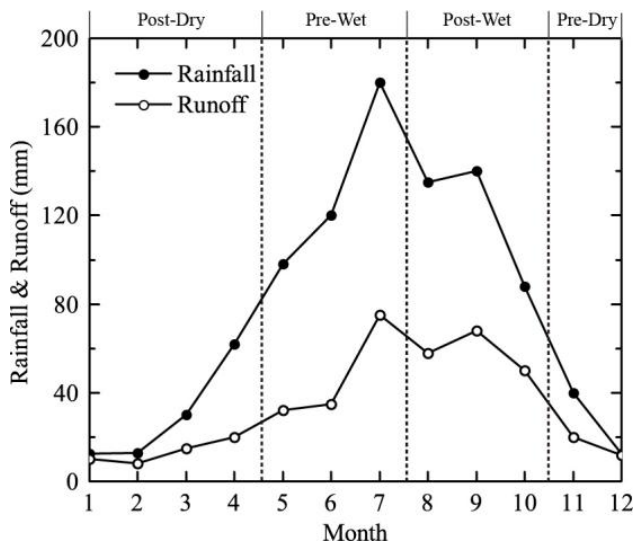


Fig. 2. Rainfall and runoff regimes over upper Hanjiang River basin (UHRB). Runoff is the total amount of monthly inflow (m^3) to Danjiangkou reservoir divided by basin area (km^2). Rainfall is the mean value of all the rain gauges weighted by area. The unit is in mm.

2.2 The ESP approach

ESP is a widely used approach for hydrologic forecasting (Werner et al., 2004), and usually serves as a reference for validating climate model-based seasonal hydrologic prediction (Wood et al., 2005; Luo and Wood, 2008; Yuan et al., 2013). The basic idea of ESP is to run a candidate hydrological model with observed meteorological forcing through a spin-up period to the time of the forecast. Then, the model with the spun-up initial basin state is driven by an ensemble of forcing (precipitation, temperature, etc.) that is randomly sampled from the observed historical records (Day, 1985). An ensemble of the streamflow traces is then generated, containing the information of forcing uncertainty on the forecast (see Fig. 1 of Wood and Lettenmaier, 2008, for schematic illustration of the ESP approach). The arithmetic mean value of the ensemble forecasts is selected as the issued forecast.

2.3 Model setup

The hydrological model used in this study is Tsinghua Representative Elementary Watershed model (referred to as THREW model) (Tian, 2006). It is a semi-distributed hydrological model, based on the theory of representative elementary watershed proposed by Reggiani et al. (1999). The model consists of a set of balance equations for mass, momentum, energy and entropy, including associated constitutive relationships for various exchange fluxes, at the scale of a well-defined spatial domain. Details of the model can be found in Tian (2006, 2009). The THREW model has been successfully applied in several previous studies (Mou et al.,

Table 1. Calibration and validation statistics for the simulated streamflow of UHRB at Danjiangkou reservoir station.

	Nash–Sutcliffe efficiency (NSE)			Water balance (WB)
	Daily	Weekly	Monthly	
Calibration period (1970–1980)	0.85	0.98	0.99	−0.06
Validation period (1981–2000)	0.81	0.96	0.99	−0.05

2008; Yang et al., 2013; Li et al., 2012; Liu et al., 2012; Tian et al., 2006, 2012).

The study period is 1970–2000, which is divided into two parts with the purpose of model calibration and validation. The calibration period is 1970–1980 and the rest is used for model validation. The model calibration procedure is as follows: initial values and the reliable ranges of each parameter are determined according to the physical attributes of UHRB and previous THREW modeling experience (see Sun et al., 2013, for the information of the key parameters in the model). An automatic optimization algorithm, ϵ -NSGAI (Reed et al., 2003; Deb et al., 2002), is then used for further calibration. The value of each parameter is finally determined based on the automatic calibration results. This calibration procedure enables the parameters to bear clear physical meanings and maintains the performance of the model as well. The objective function for the automatic calibration is the Nash–Sutcliffe efficiency coefficient (NSE) (Nash and Sutcliffe, 1970), as widely used in previous hydrological modeling studies.

Another water balance related metric WB, together with NSE, is used to evaluate the performance of the model during the two periods. WB takes the form as

$$\text{WB} = \frac{R_{\text{obs}} - R_{\text{sim}}}{R_{\text{obs}}}, \quad (1)$$

where R_{obs} and R_{sim} are the total observed and simulated runoff (in mm), respectively.

The statistics are summarized in Table 1. The THREW model performs quite well in UHRB. The values of daily NSE in both the calibration and validation period are above 0.80. The value of monthly NSE is as high as 0.99 (see Yang et al., 2013, for more detailed evaluations of the THREW model performance in UHRB). The evaluation statistics indicate that the model accurately captures the dynamics of the streamflow during 1970–2000 over UHRB, given the observed atmospheric forcing.

However, this lumped calibration strategy might only present the overall performance of the model during the whole simulation period. It is not necessary a guarantee of the performance over each sub-period (e.g., dry seasons). We will present further details of another model calibration strategy used in this study in the next section.

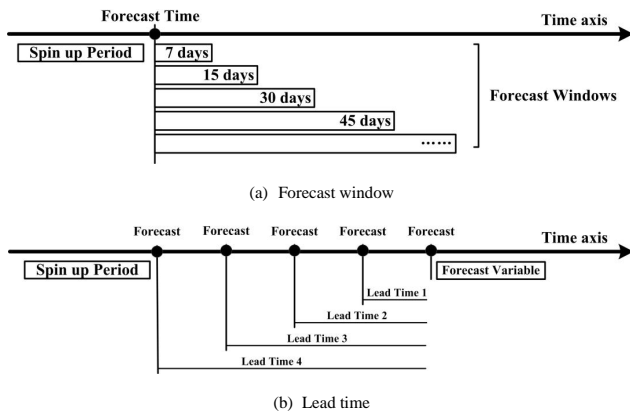


Fig. 3. Schematic illustration of (a) Forecast Window and (b) Lead time.

3 Results

In this section, we present the evaluation of the impacts of IC and FC on the forecast within different forecast windows (see Sect. 3.1 for the definition of forecast window) and at two contrasting initial states. The combined effects of IC and FC is then discussed by defining a new parameter β . The effect of MU (the uncertainty of model parameters) will be examined in Sect. 3.2.

3.1 The impact of IC and FC

3.1.1 Definition of forecast window (FW)

A forecast window (FW) proposed in this study can be regarded as an integration time window initiating from the forecast date. It differs from lead time, which is a frequently used term in hydrologic forecasting (see Fig. 3). Lead time is the gap between the time that the forecast is issued and the occurrence of the forecasted variable. For example, if we are interested in the total streamflow volume of this July, supposing the forecast time is issued some day in January, then the lead time should be about 6 months (the time gap between January and July). The model needs to run from January till the end of July. In this context, this study focused on the cases with no lead time (equal to zero). They could be regarded as “real-time” forecasts but with different FWs. The forecasted variable is the integral streamflow volume within each FW.

3.1.2 Evaluation of the impact of IC and FC

“Virtual” experiments are designed in this section for the reason of avoiding the incorporation of model uncertainty (MU) effect. In these “virtual” experiments, the forecasts are evaluated against retrospective streamflow simulations (driven by actual atmospheric forcing) instead of actual streamflow observations, assuming that the model is “perfect”. The design of the experiment is summarized in Table 2. Eight differ-

Table 2. Details of the experiment designs (for different forecast window).

Initial forecast date	Forecast windows	Ensemble members	Hindcast period
1 February	7 days, 15 days, 30 days, 60 days,	31	1970–2000
1 July	90 days, 120 days, 150 days, 183 days		

ent forecast windows are set: 7, 15, 30, 60, 90, 120, 150 and 183 days. We also chose two contrasting forecast dates, 1 February and 1 July of each year (in the middle of the winter and summer season, respectively), representing the dry and wet initial states of the basin. The seasonal regime of soil moisture bears a similar but flattened shape compared to the precipitation regime in Fig. 1, based on which the two initial dates were selected (figure not shown). Each set of the forecasts were made for a 30 yr period (from 1970 to 2000).

The results are evaluated by using the Pearson correlation coefficient ρ . ρ decreases with the extension of forecast window for both initial dates (Figs. 4 and 5). However, the patterns are a little different. For the dry scenario (the initial date is 1st February), ρ is 0.99 for the 7-day window, and gradually drops below 0.50 for the window exceeding 90 days; while for the wet scenario (the initial date is 1 July), the maximum correlation coefficient is 0.70 for the 7-day forecast window, and quickly reduces to 0.46 for 30-day window. The forecasts almost equal the climatological mean when the forecast window exceeds 90 days under this scenario. The contrasting behaviors of the two scenarios indicate that the consistency of the forecast seems to bear a wider range of forecast windows for the dry scenario.

To further illustrate the impact of IC/FC and their relative role in the forecast, we employed an analytical framework, as developed by (Wood and Lettenmaier, 2008) and used by Li et al. (2009). It is effective to discern relative impacts of IC and FC on the forecasts, as well as the dynamic competence of the two factors with the increase of forecast window. The basic idea of this framework is to re-sort the forecasts according to IC (soil moisture) and FC (precipitation forcing). Two-dimensional images are produced based on the resorted matrix of the forecasts. The columns of each 2-D image in Figs. 6 and 7 can be regarded as a reverse-ESP (R-ESP) approach which was introduced by Wood and Lettenmaier (2008) (see also Fig. 2 of Li et al., 2009, for more details of R-ESP and ESP). The basic idea of R-ESP is to drive an ensemble of ICs, which are derived by resampled meteorological ensembles during the spin-up period, using the accurate meteorological forcing. R-ESP reveals the influence of IC uncertainty on the forecast, while ESP focuses on the impact of FC. The patterns of the images reflect the relative impact of IC and FC: if these are horizontally structured,

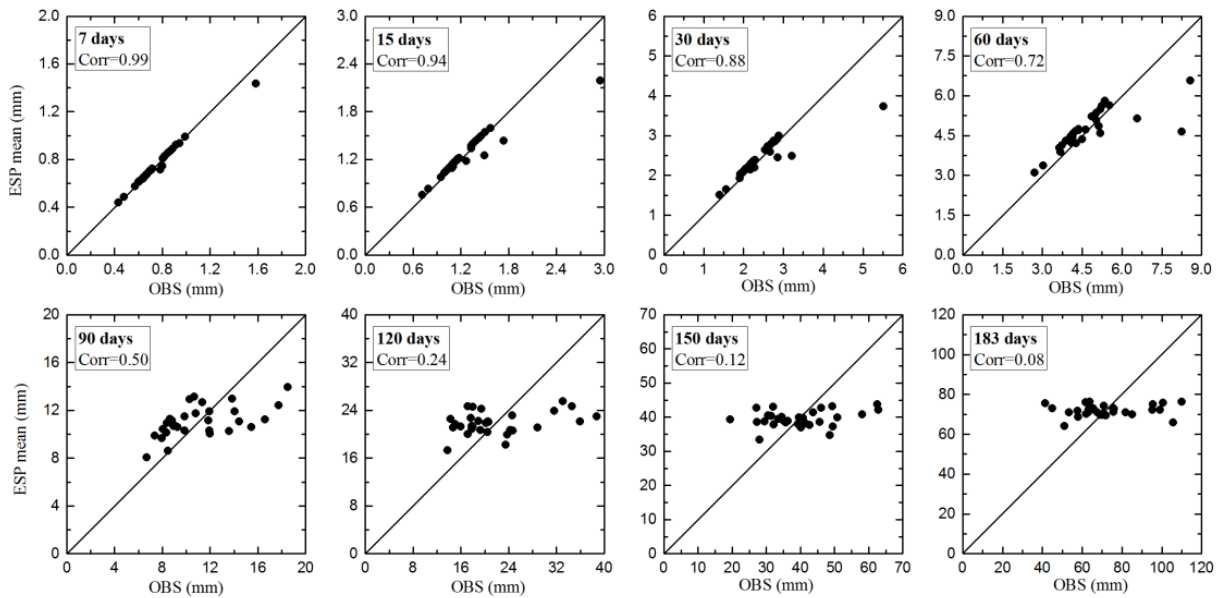


Fig. 4. Evaluation of the ESP approach for different forecast windows. The initial forecast date is 1st February.

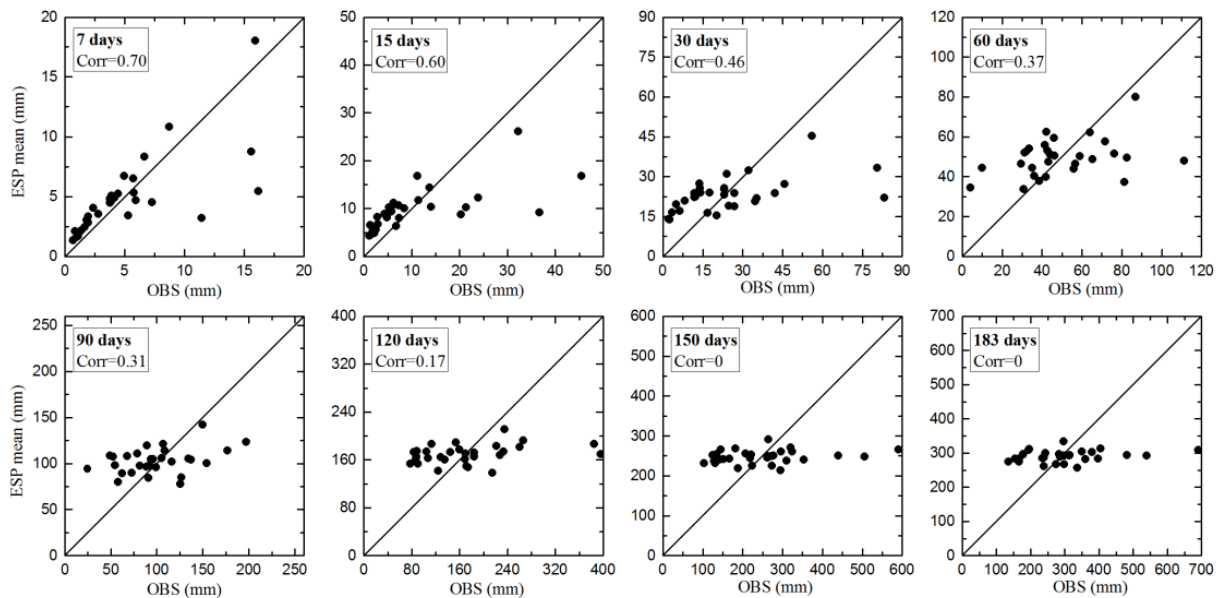


Fig. 5. The same as Fig. 4 but the initial forecast date is 1st July.

the forecasts are largely determined by IC, and FC has a relatively small impact; while FC dominates the forecast if the image is vertically structured. A “hatched” image indicates a combined influence of IC and FC.

Organized structures could be observed in both Figs. 6 and 7. For the forecasts initialized on the 1 February (Fig. 6), the patterns of the images are characterized by horizontal stripes for forecast windows less than 60 days (2 months). The patterns change into more vertical stripes when the window exceeds 90 days. For the forecast of 90 day forecast win-

now, a hatched pattern is displayed. IC is the dominant impact on the forecasts within 2 month forecast window when ESP has most skill; while this dominance changes to FC for larger forecast windows (exceeding 90 days), and ESP loses its skill as well. The 90 day window is the divide of the dominance of the two factors. Both the IC and FC could impact the forecasts within the 90 day forecast window. For the forecasts initialized on the 1 July (Fig. 7), the dominance of IC is constrained to 30 days. For the rest of forecast

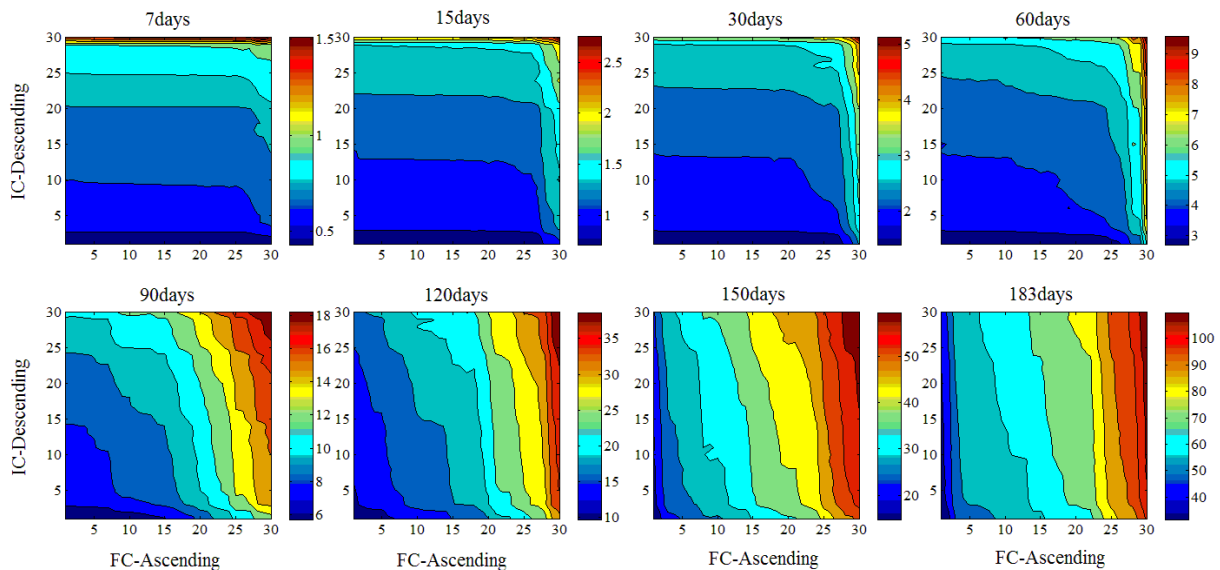


Fig. 6. Runoff forecasts (unit: mm) by ESP (row) and R-ESP (column) for UHRB. Forecasts are initialized on 1 February. Precipitation forcing (units: mm) is sorted from dry to wet in ascending order, and Initial conditions (units: mm) is sorted from wet to dry in descending order.

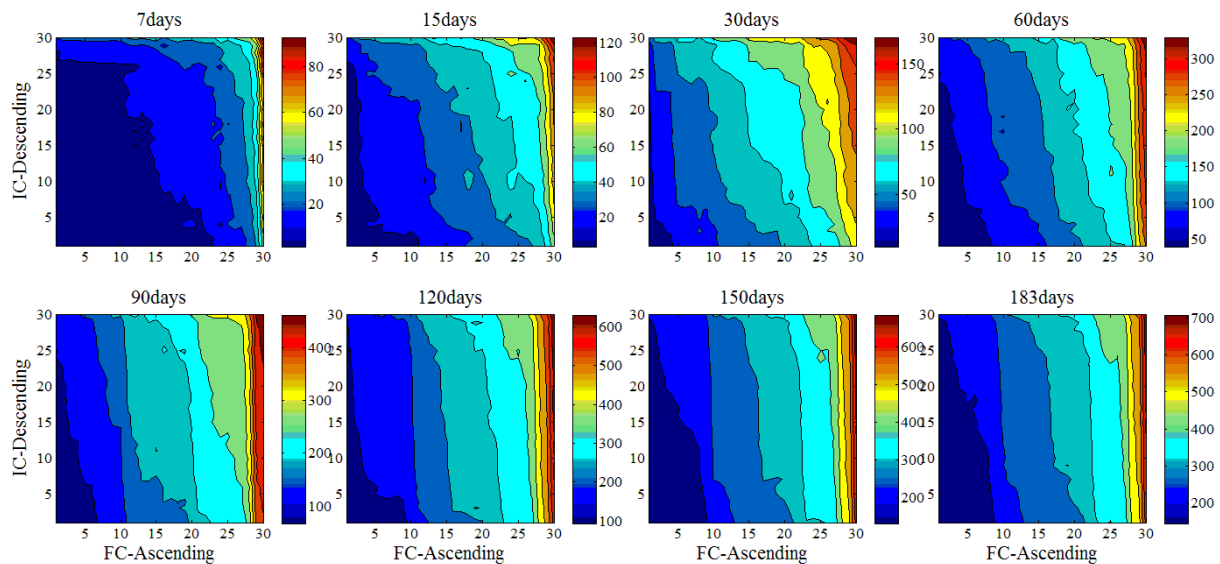


Fig. 7. The same as Fig. 6 but the forecasts are initialized on 1 July.

windows (exceeding 30 days), FC dominates the forecasts and the forecast skill decays as well.

The possible explanations for the results are the 1 February represents relatively dry state of the basin within the year, since it is in the middle of the dry seasons and the antecedent precipitation is scarce. The lack of soil moisture to the saturation state cannot be easily filled up with subsequent rainfall events. Thus, the IC could persist for a long period until the total rainfall within the forecast window is able to compensate the initial soil moisture anomaly. This could explain why the “hatched” image occurs for the 90-day case (Fig. 6)

and is converted to “vertical” when the wet season (May to August) begins. For the wet scenario (forecasts initialized on the 1 July), the basin has already been saturated or near-saturated. In this case, the accumulated soil moisture in the basin will contribute significantly to the future streamflow regime, just as most snow-dominated basins behave. However, unlike snow-dominated basins, UHRB will experience rainy weather in the subsequent months (August, September and October). Several heavy precipitation events could easily recharge the basin and eliminate the persistence of the soil moisture completely, so the IC is not able to persist for a long

Table 3. Details of the experiment designs (for deriving the relationships of β and the forecast skills).

Initial forecast date	Forecast windows	Ensemble members	Hindcast period
1 Jan, 1 Feb, 1 Nov, 1 Dec	3 days, 7 days, 15 days, 20 days 30 days, 45 days, 60 days, 90 days	31	1970–2000

period. It seems that the persistence of IC is not solely determined by the magnitude of the initial anomaly, but also by the subsequent meteorological conditions. The forecast skill of the ESP approach is determined by the combined effects of IC and FC, which will be examined by defining a new parameter in the next section.

3.1.3 Combined effects of IC and FC

Based on the analyses in Sect. 3.1.2, we propose a new parameter that tries to synthesize the effect of IC and FC on the forecasts and generalize the relationships to the forecasts with more diverse ICs. The new parameter beta (β) is a dimensionless ratio of total initial water storage and incoming rainfall within forecast windows, defined here as

$$\beta = \log(R_{sm}/R_p), \tag{2}$$

where R_{sm} is the total initial water storage (e.g., soil moisture, residual water in the river, expressed as “depth” and the unit is mm), representing the influence of IC; R_p is the total rainfall (in mm) within the forecast windows, representing the influence of FC. We take the logarithm of the ratio for mathematical reasons.

We employed MARE (mean absolute relative error) as the evaluation metric of the forecasts. The form is

$$\text{MARE} = \frac{1}{n} \sum_{i=1}^n \left| \frac{\text{Fst}_i - \text{Obs}_i}{\text{Obs}_i} \right| \times 100\%, \tag{3}$$

where Fst_i and Obs_i are the forecasted and observed total streamflow volume within forecast windows, respectively; n is the number of forecast years, and $n = 30$ in this study.

A new set of forecast windows are used, these are 3, 7, 10, 15, 20, 30, 60 and 90 days, since the ESP approach presents no skill for the forecasts beyond 90 days in this study. The first day of each month is chosen as the forecast date. The details of the experiment are summarized in Table 3. The experimental configurations in this section are also devoid of model uncertainty. An exponential function ($y = ae^{bx}$) is employed to fit the relationship between the parameter (β) and evaluation metric (MARE) of the forecasts. The parameters and evaluation values (R^2) of the fitted lines are listed in Table 4.

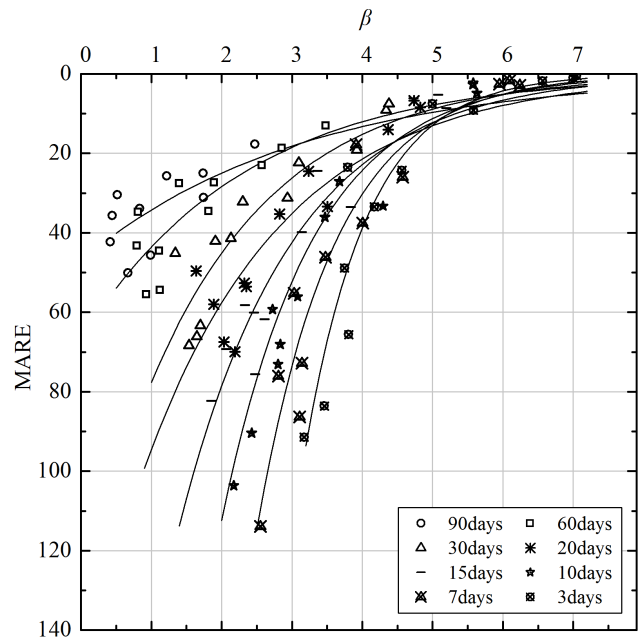


Fig. 8. Scatter plots of β and MARE. The curves are fitted exponential lines for each group of forecasts with the same forecast window. The parameters of the lines are summarized in Table 4.

The accuracy of the forecasts increases exponentially with β , corresponding to our above analysis that the forecasts skill will be mainly determined by IC if the initial water storage has a comparatively larger value than the total rainfall within the forecast windows. However, the variability of total precipitation within forecast window also plays a role. As shown in Fig. 8, the forecast accuracy becomes less sensitive to β as the forecast window increases. This is probably because the total rainfall within larger forecast windows enables the basin to be fully recharged several times, which eliminates the persistence of IC. In addition, the inter-annual variability of the total rainfall decays with the integrating time window (e.g., the variability of seasonal precipitation is usually smaller than that of weekly precipitation), which should come as no surprise. Thus, a larger value of total precipitation with smaller variability will induce smaller sensitivity of forecast accuracy to β .

It is also noteworthy that although the fitted lines asymptotically converge to 0, there will be upper bounds for the forecast accuracy in reality. As can be observed in Fig. 8, the upper bounds of forecast skill for 3 days are much higher than 90 days, indicating that short-term forecasts are potentially more accurate than long-term forecast using the ESP approach. However, we also notice that short-term forecasts are not necessarily more accurate than long-term counterparts (the relatively larger vertical spans for the smaller forecast window lines in Fig. 8). Since the model is assumed to be error free, the possible explanation could be the variability of the total precipitation within forecast windows. For

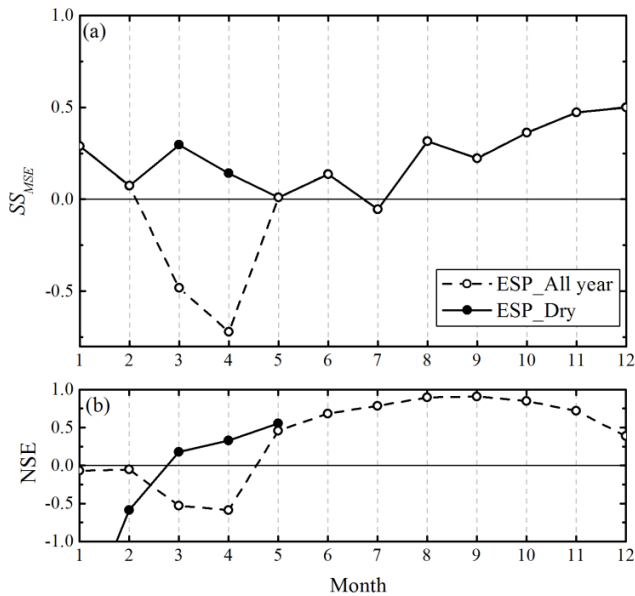


Fig. 9. (a) Forecast skills of ESP based on different sets of model parameters; (b) model performances for each month. “ESP_all year” (circles) represent using the default parameters of the model (the whole year). “ESP_Dry” (dots) uses the new-calibrated parameters of the model (only January to May).

short-term forecast, the variability of FC should also be considered in addition to IC, especially for the cases when FC takes the dominance of the forecast skill.

Figure 8 also shows the potential ability of the ESP approach to make accurate forecasts within different forecast windows over UHRB. We note that this analytical framework of β is able to combine the effects of IC and FC, and provide a first-order understanding of when and to what extent the forecast skill may be achieved based on the ESP approach in UHRB.

The form of β proposed in this study is similar to the parameter kappa (κ) defined by Mahanama et al. (2011). The forecast window is fixed to three months in their study, which enables kappa focusing on variance instead of total amount. In this study, forecast skills need to be evaluated among different forecast windows. It is obvious that the inter-annual variability of rainfall decays with the extension of the accumulation period and is also negatively correlated with the total rainfall within the forecast window. In the newly proposed parameter (β) the inter-annual variability of rainfall has been, to some extent, expressed in terms of total amount. However, as discussed above, the variability of FC probably matters to the skill for short-term forecasts (with small forecast windows), especially when FC instead of IC dominates the forecast skills. This effect is still absent in the new parameter so far. Future studies should introduce the inter-annual variability of rainfall into the parameter in an explicit way. The ultimate goal is to propose a proper parameter, based on

Table 4. Parameters of the exponential function and the R^2 value in the relationships of β and the forecast skills.

Forecast windows	a	b	R^2
3 days	3153	-1.1	0.90
7 days	1055	-0.89	0.92
10 days	561	-0.77	0.96
15 days	270	-0.62	0.92
20 days	155	-0.49	0.81
30 days	134	-0.54	0.82
60 days	67	-0.43	0.71
90 days	50	-0.32	0.56

which the forecast skill of the ESP approach could be evaluated and compared within different forecast windows.

3.2 The impact of MU

Model uncertainty (MU) is another factor that influences the forecast. The essence of the ESP approach is to utilize the IC of the basin provided by the hydrological model through the spin-up period. Thus, the reliability of the IC greatly impacts the final accuracy of the forecast. The model used in this study has been calibrated against NSE, with the evaluation metrics summarized in Table 1. Although the model presents a remarkably good performance during the whole simulation period, its performance in each separate month varies. As shown in Fig. 9b, the value of NSE is above 0.90 for July, August, September and October. These four months are also the wettest during the year in UHRB. For dry months (January to April), NSE is below 0. The value of NSE is -0.58 and -0.64 for March and April, respectively.

Previous studies revealed the problems of model calibration using single objective function. The mathematical form of NSE results in the over-weighting of high flows in the calculation. Even though the simulation of low flow is poor, NSE will not be affected, since the magnitude is small relative to the high flow period. In this study, we also carried out a different model calibration strategy. The low flows (streamflow from January to May) are extracted from each year, constituting a new time series. The model is again calibrated with the same calibration procedure, but only for the new low-flow time series. NSE is still used as the calibration metric because of its simplicity. The new NSE values for each month (January to May) are shown in Fig. 9b. Model performance in March, April and May is improved, while for January and February, the new calibration does not make any improvement.

Considering our purpose here is to examine the influence of MU (the uncertainty of model parameters) on the forecast accuracy of ESP approach, we will also not endeavor to improve the model performance for each month, but only

focus on the accuracy of forecasts on March and April after the new model calibration. We set the forecast window to 30 days, which has been frequently used in previous studies (e.g., Smith et al., 1992; Hashino et al., 2007; Wang et al., 2011) and proved to be effective under different ICs in previous section.

The skill of the forecast in ESP approach is evaluated by SS_{MSE} , defined as

$$SS_{MSE} = 1 - \frac{\sum_{i=1}^n (Fst_i - Obs_i)^2}{\sum_{i=1}^n (Obs_i - \overline{Obs})^2}, \quad (4)$$

where Obs_i and Fst_i are the observed and forecasted monthly streamflow volume (in mm), respectively; \overline{Obs} is the mean value of the observed streamflow volume (in mm), representing the climatological forecast; n is the total number of forecast years, and $n = 30$ in this study. This has the same form as Nash–Sutcliffe efficiency, but is being used for assessing the model performances in individual months. A score of 1 corresponds to a perfect forecast.

During October–December, the ESP approach presents high forecast skill (Fig. 9a). For March and April, the skill score is far below 0, indicating no forecast skill for this period. However, this does not indicate the uselessness of ESP approach. When the forecasts are made based on the recalibrated models (especially for March and April), the skill scores are significantly improved. The improvement of the forecast skill in March and April reinforces our hypothesis that MU (errors in model parameters) influences the forecast accuracy in the ESP approach, especially for those low flow events that are difficult to simulate with hydrologic models.

It is noteworthy that the forecast skill score is low in May, June and July, although the model performs quite well in this month. The low skill of the forecasts in May, June and July implies that the ESP approach is no better than climatology for the monthly streamflow forecast of pre-wet seasons in UHRB, which probably could be attributed to the combined effects of FC and IC in this season (as discussed in previous subsections). For post-wet season forecasts (August, September and October) and pre-dry season forecasts (November and December), the ESP approach has skill. Our results are similar to the study of Wood and Lettenmaier (2008), which showed that the forecast skill is higher during the transition period from the wet to dry season than otherwise. However, our analyses also show that the forecast skill is improved in the post-dry season (March and April, especially) after recalibrating the hydrologic model used in the ESP. The forecast skill in January and March is still comparable with that in post-wet and pre-dry seasons, indicating the potential of the ESP approach with a well-calibrated hydrologic model. Future efforts should focus on the improvement of the model performance in the post-dry season period (January to April).

It should be noted that our analyses on model uncertainty are preliminary. Considering the forecast skill is always influenced by the model uncertainty, it is necessary to provide a complete assessment of the model uncertainty. There are a large number of studies focusing on the model uncertainty analyses (e.g., Beven, 1989). Generalized Likelihood Uncertainty Estimation (GLUE), proposed by Beven and Binley (1992), proves to be a useful analytical framework, which could reflect all sources of errors (input, parameter and model structure) in the modeling process and allow the uncertainties associated with those errors to be carried forward into the simulations (see Beven and Binley, 1992, for more details of the framework). Ensemble modeling approaches, for example, BMA (Bayesian model averaging, Hoeting et al., 1999), provide possible ways to reduce the uncertainty of the model structure. However, we assume that the structure of the model used in this study is “perfect”, and focus on the parameter uncertainty only. Future studies should aim to focus on all the sources of model uncertainty and their influence on the forecast skill.

4 Conclusions and discussion

In this paper, we have investigated the influence of IC, FC and MU on hydrologic forecast based on the hindcasts using ESP approach over UHRB in China. The concept of forecast window (FW) is introduced in this study and the combined effects of IC and FC within the forecast window is discussed by implementing “virtual” experiments without considering the uncertainty of hydrologic model (structure, parameter, etc.). The improvement of the model performance also increases the skill of the ESP approach significantly for low flow forecast, indicating the impact of MU (the uncertainty of model parameters) on hydrologic forecast. The results are summarized as below.

1. For dry initial states, the forecast is consistently good within forecast windows up to 90 days. For wet initial states the persistence decays with the windows exceeding 30 days. The contrasting behaviors of the two scenarios highlight the role of IC and FC on the forecast.
2. IC controls the forecast skills within smaller forecast windows. The dominance of IC on the forecast is shifted to FC with the increase of the forecast windows. A dimensionless parameter β is proposed to depict the combined effects of IC and FC. The forecast skill increases exponentially with β , and varies greatly in different forecast windows. The analytical framework of β provides a first-order understanding of when and to what extent the forecast skills may be achieved based on ESP approach.

3. The model calibration strategy used in this study emphasizes the model behavior during the wet season, while for the dry season the model behaviors cannot be guaranteed. This affects the accuracy of the ESP approach for predicting low flows. By re-calibrating the model for low flows, the uncertainty of model parameters is reduced within the dry season, which significantly improves the model performance as well as the forecast skill in the dry-season period.
4. The performance of the ESP approach for monthly streamflow forecasts is more skillful during the transition period from wet to dry than otherwise over UHRB. For the transition period from dry to wet, the lower skill of the forecasts could be attributed to the combined effects of IC and FC, but less to the biases in the hydrologic model. Other innovative ways should be explored for monthly streamflow forecasts during this season (from dry to wet, e.g., by improving the prediction of future atmospheric forcing using sophisticated physical or statistical methods (Zhou et al., 2011)).

To the best of the authors' knowledge, the concept of forecast window (FW) is proposed in this study for the first time. We suggest that the concept of forecast window (FW) might have some implications on the hydrological forecasts based on the ESP approach. The dominance of IC and FC within FWs reflects the potential ability of ESP. For different scenarios with various combinations of IC and FC, there should be certain "behavioral forecast windows" (BFWs), beyond which ESP-based hydrologic forecasts are not accurate. In addition, BFW can also be related to the physical attributes of each basin (e.g., sizes, maximum concentration time, etc.). Li et al. (2009) disclosed that the basin size matters in the ESP skill. The relationship derived in this study is only for the specific basin (UHRB in this study). More different basins with diverse physical attributes (e.g., size, vegetation conditions, etc.) should be examined in future studies so as to make the relationship more general. BFW is crucial in the practical implementation of ESP approach by providing a guideline for the design of forecasting systems and the confidence of the forecast results. However, the framework designed to examine FW and BFW in this study does not consider lead time in the forecasts. These can be regarded as zero lead time scenarios. Besides, the influence of MU is not considered in the framework. Future studies will further examine the behaviors of FW and BFW with varying lead time and model uncertainty (structure and parameter) incorporated.

There are a number of ways (e.g., pre-processing, post-processing) to further improve the performance of the ESP approach. For instance, Yang et al. (2013) improved the forecast skills of ESP approach by using a reduced set of the ensemble members. The members in the reduced ensemble were selected from the historical records when they have the same climate signals (e.g., SOI, PDO) as the forecast

year. Similar studies could be found in Hamlet and Lettenmaier (1999), Lamb (2010) and Wang et al. (2011). Instead of using the randomly sampled members, the "pre-processing" process enhances the representativeness of future forcing ensembles. Similarly, "post-processing" aims to remove the bias of the streamflow ensembles, which could also improve the forecast skill. Possible "post-processing" methods were evaluated in previous studies (e.g., Kang et al., 2010; Wood and Schaake, 2008; Hashino et al., 2007). Shi et al. (2008) demonstrated that "post-processing" could reduce the forecast error as much as the correction of forecast errors through hydrologic model calibration. Yuan and Wood (2012) also found that post-processed streamflow forecasts directly from a global climate forecast model, where its land surface model is un-calibrated, has comparable performance to a well-calibrated hydrologic model driven by downscaled and bias-corrected meteorological forcing.

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