



Ion dynamics in electron beam–plasma interaction: particle-in-cell simulations

K. Baumgärtel

Leibniz-Institut für Astrophysik Potsdam, An der Sternwarte 16, 14482 Potsdam, Germany

Correspondence to: K. Baumgärtel (uk.baumgaertel@t-online.de)

Received: 17 March 2014 – Revised: 15 July 2014 – Accepted: 15 July 2014 – Published: 22 August 2014

Abstract. Electron beam–plasma interaction including ions is studied by particle-in-cell (PIC) simulations using a one-dimensional, electrostatic code. Evidence for Langmuir wave decay is given for sufficiently energetic beams, as in previous Vlasov–Maxwell simulations. The mechanism for the generation of localized finite-amplitude ion density fluctuations is analyzed. Amplitude modulation due to interference between the beam-generated Langmuir waves causes random wave localization including strong transient spikes in field intensity which create bursty ion density structures via ponderomotive forces. More dense beams may quench the decay instability and generate low-frequency variations dominated by the wave number of the fastest growing Langmuir mode.

Keywords. Space plasma physics (waves and instabilities)

1 Introduction

Electron beam-generated Langmuir wave forms, observed for more than 30 years under various space plasma conditions, often exhibit a spectral double peak near to the ambient plasma frequency ω_{pe} (Gurnett et al., 1993; Hospodarsky et al., 1994; Hospodarsky and Gurnett, 1995; Kellogg et al. 1996; Bale et al., 1996; Kojima et al., 1997; Pottellette et al., 1999; Sigsbee et al., 2010; Graham and Cairns, 2013a). It is commonly assumed to be produced by the interference of the dominant Langmuir wave of the instability and a second Langmuir wave of comparable amplitude but slightly different frequency. Various efforts have been made to understand the origin of the second Langmuir wave. A well-known nonlinear wave interaction process which is able to produce such a scenario is the parametric decay of the most unstable Langmuir mode into a counterpropagating second Langmuir wave and a forward propagating ion acoustic wave. This process

has been proposed long ago as basic mechanism for the interpretation of type III solar radio bursts (Cairns and Melrose, 1985). In this resonant three-wave interaction the frequency of the ion acoustic mode is very small against the plasma frequency which makes it very difficult to resolve separated peaks in the plasma frame. However, the resonance conditions require a significant difference in the wave numbers of the two high-frequency waves. That is, in case of a relative motion between the observer (spacecraft) and the main plasma (e.g., solar wind), the Doppler shift may enlarge the frequency difference such that high-resolution detectors are able to identify the two peaks. It turned out that, in several cases, using estimated beam velocities, the predictions of the three-wave parametric decay via ion sound waves are consistent with the observed beat frequencies (Hospodarsky and Gurnett, 1995; Kellogg et al., 1996; Graham and Cairns, 2013a).

It should be mentioned, however, that a variety of other types of electron beam-driven Langmuir amplitude modulations have been observed which do not fit into the above parametric decay scheme. Among them are spectra with power at ω_{pe} only (e.g., Sigsbee et al., 2010), a double peak in absence of ion acoustic activity (e.g., Sigsbee et al., 2010), multiple spectral peaks (e.g., Graham and Cairns, 2013a), a single peak with side-band structure (e.g., Gurnett et al., 1981; Thejappa et al., 2013), Langmuir eigenmodes localized in density wells (Ergun et al., 2008; Graham and Cairns, 2013b) and waveforms resulting from the interaction of Langmuir waves with electrostatic whistler/lower hybrid waves instead of ion sound (Stasiewicz et al., 1996).

The interpretation of electron beam-driven Langmuir wave forms has been the target of a number of particle-in-cell (PIC) simulations (Omura et al., 1996; Akimoto et al., 1996; Muschietti et al., 1996; Matsukiyo et al., 2004; Usui et al.,

2005; Baumgärtel, 2013) and electrostatic Vlasov simulations (Umeda, 2006; Silin et al., 2007; Umeda, 2007; Umeda and Ito, 2008; Daldorff et al., 2011; Sauer and Sydora, 2012). Studies which include ion dynamics (in some cases with a reduced proton-to-electron mass ratio) show clearly that the heavy particles indeed contribute to the evolution of the instability. Evidence was given for the classical Langmuir decay instability to occur for sufficiently energetic beams (Umeda, 2007; Umeda and Ito, 2008).

The PIC simulations presented in this short contribution first confirm Langmuir wave decay as a transient process in the evolution of the beam–plasma system (Sect. 3). Then the mechanism for the generation of localized finite-amplitude ion density variations is examined (Sect. 4). After presenting simulation results in time representation, including the course of the energy partition (Sect. 4), it is shown that a more dense beam may create a modified wave scenario, with low-frequency fluctuations dominated by k_L , the wave number of the fastest growing Langmuir mode (instead of $2k_L$ for decay) and a spectral double peak of the high-frequency field seen even in the plasma frame (Sect. 6).

2 Simulation model

A one-dimensional electrostatic standard particle code is used with periodic boundary conditions. The initial condition is set up by Maxwellian distributions of background electrons and ions while the electron beam is represented by a drifting Maxwellian (V_b drift velocity). In order to keep a tolerable degree of energy conservation, the electric field for the acceleration of electrons and ions is calculated by an implicit momentum method according to the philosophy of Langdon (1985), based on the current equation

$$\frac{\partial E}{\partial t} = j = \frac{e}{\epsilon_0} (n_e v_e - n_i v_i) \quad (1)$$

with n_e, v_e, n_i, v_i the particle density and bulk velocity of electrons and protons, respectively. The moments n_e and v_e are built with both beam and background electrons. In order to check the accuracy of the field calculation via Eq. (1), the field is additionally calculated from the Poisson equation

$$\frac{\partial E}{\partial x} = -\frac{e}{\epsilon_0} (n_e - n_i). \quad (2)$$

A comparison of both results did not give rise to corrections. Our frame of reference is that of the background particles at rest. The presence of an electron beam is then equivalent to a current. To avoid this initial current, one may compensate it by a small drift of the background electrons in direction opposite to the beam, as done in a number of simulation studies. The evolution of the instability then starts with zero electric field. Otherwise, in 1-D geometry, the initial current is the source of “beam-aligned” plasma oscillations

Table 1. PIC simulation parameters.

Beam density	$n_b/n_o = 0.0057, 0.05$
Beam velocity	$V_b/v_{the} = 16$
Beam temperature	$v_{thb} = v_{the}$
Proton temperature	$v_{thi} = 0.02 v_{the}$, i.e., $T_i/T_e = 0.73$
Proton-to-electron mass ratio	1836
Simulation box length	$3000\lambda_D$
Total number of electrons	1 500 000
Time step	$0.025 \omega_{pe}^{-1}$
Final time	$2000 \omega_{pe}^{-1}$
Number of grid points	1024

$$E(t) = -\frac{m_e n_b}{e n_o} V_b \omega_{pe} \sin(\omega_{pe} t + \phi) \quad (3)$$

with an arbitrary phase ϕ (Baumgärtel, 2013). This $k = 0$ mode is present from the very beginning prior to the onset of the instability, with an amplitude controlled by beam density and beam velocity. For thin beams ($n_b/n_o \lesssim 0.01$) where the frequency of the fastest growing mode is very close to ω_{pe} , no additional signal can be expected from this oscillation in the power spectrum. This may change for denser beams ($n_b/n_o \gtrsim 0.05$) which downshift the frequency of the dominant mode, resulting in a peak at ω_{pe} and another below ω_{pe} . We start the simulations generally with background electrons at rest; that is, we accept an initial current and the associated plasma oscillations.

In the simulations, time and frequencies are scaled according to the electron plasma frequency ω_{pe} , distance is in units of the Debye length λ_D , densities and velocities are normalized by the equilibrium density n_o and the thermal velocity v_{the} of the background electrons, respectively. As a consequence, the longitudinal electric field is then scaled by $E_0 = m_e/c v_{the} \omega_{pe}$. For nominal solar wind parameters $n_o = 4 \text{ cm}^{-3}$, $T_e = 10 \text{ eV}$ the field unit corresponds to $E_0 = 1.8 \text{ V m}^{-1}$. For this reference plasma, the mostly used beam velocity $V_b = 16v_{the}$ is equivalent to $V_b \approx 0.07c$ with c the light velocity. The plasma parameters listed in Table 1 are thought to be representative so that the simulation results may be used to some extent for comparison with observations. Table 1 contains in addition technical simulation parameters.

3 Langmuir wave decay

As known from former simulations, for a beam speed of the order of $V_b/v_{the} \sim 10$, the longitudinal field starts growing after a period of some tens of ω_{pe}^{-1} , dependent on the level of the initial field noise. In this initial stage the waves grow exponentially at the linear growth rate. As a result of a simulation run with $V_b/v_{the} = 16$, Fig. 1 depicts the spatial variation of field and proton density and the corresponding power spectra from an early part of the time development

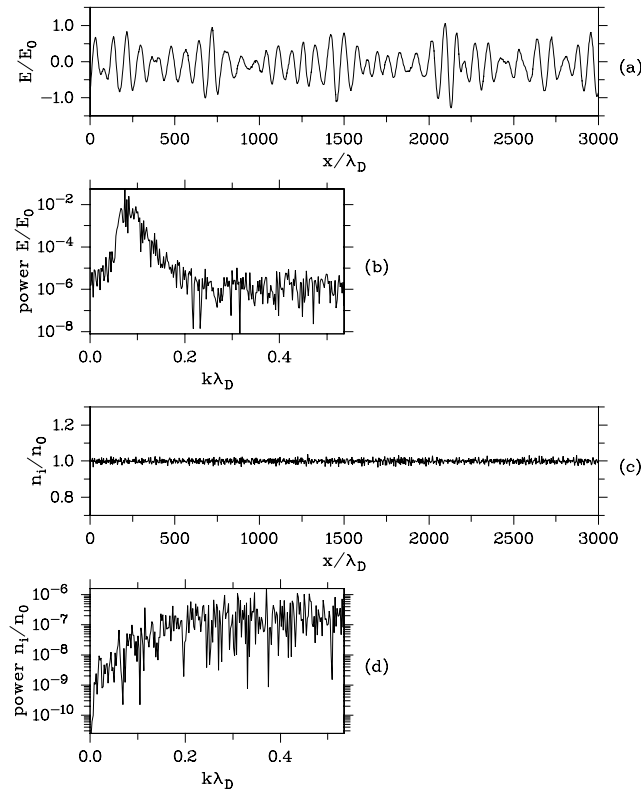


Figure 1. Spatial profiles of field (a), proton density (c) and associated power spectra (b), (d) at an early time $t = 200 \omega_{pe}^{-1}$ of the beam–plasma evolution. The almost coherent field structure is dominated by the wave number $k\lambda_D \approx 0.075$ of the fastest growing mode. Beam velocity $V_b = 16 v_{the}$, beam density $n_b = 0.0057 n_0$.

($t = 200 \omega_{pe}^{-1}$). The almost coherent field structure shown in panel (a) consists of a number of wave packets and is dominated by the fastest growing Langmuir mode, as indicated by the pronounced peak at $k_L \lambda_D \approx 0.075$ in the power spectrum (panel b). The amplitude modulation is the result of linear interference of unstable waves with wave numbers in a small range round k_L . The structure moves in beam direction with almost the group velocity of the dominating mode $v_{gr} \approx 0.22 v_{the}$, accompanied by a continuous change of the envelope. Due to the random phases of the waves that have grown from noise, occasionally strong localizations of the field intensity may occur.

Specific low-frequency response is not yet seen in Fig. 1c although the noise level has considerably grown from its initial value 10^{-10} . Up to the time $t = 600 \omega_{pe}^{-1}$ the low-frequency power has continued to increase, as seen in Fig. 2, with a peak at $k_s \lambda_D \approx 0.18$, almost twice that of the maximum field intensity. This is a clear indication of parametric Langmuir wave decay. The peak exhibits an appreciable width suggesting that low-frequency fluctuations from a broad range of wave numbers are involved in the decay process.

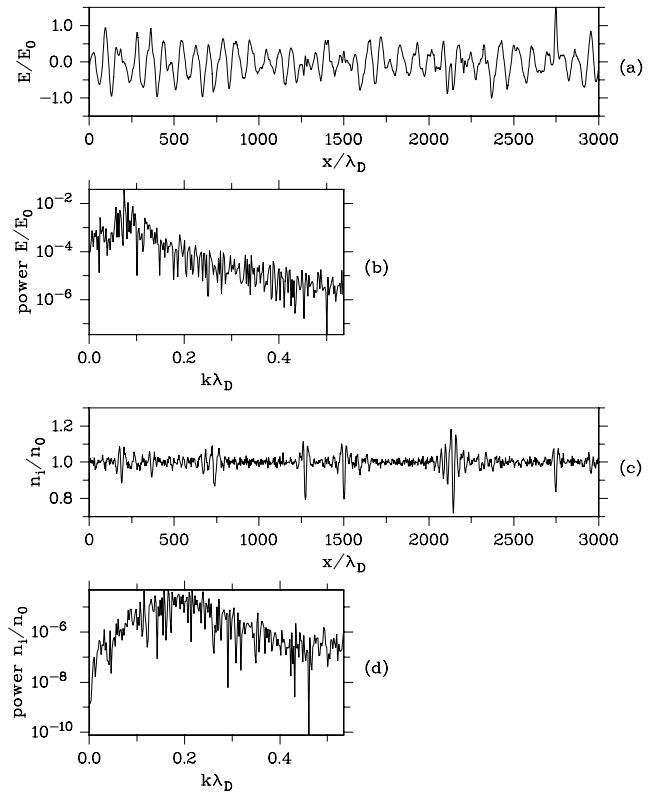


Figure 2. The same as Fig. 1 at a later time $t = 600 \omega_{pe}^{-1}$. The most power of the low-frequency response is concentrated near $k\lambda_D \approx 0.18$, almost twice the wave number of the fastest growing mode, suggesting Langmuir wave decay. The power spectrum (b) is falsified by backscattered waves.

Since a spatial power spectrum at a fixed time does not distinguish between positive and negative wave numbers, backscattered daughter Langmuir waves are hidden in Fig. 2b and falsify the power spectrum. To make them visible Fig. 3 displays a dynamic spectrum for the time period $0 < t < 750 \omega_{pe}^{-1}$ and the wave number range $-0.5 < k\lambda_D < 0.5$. The bottom panel of Fig. 3 presents a cut through the color graphic for a frequency slightly below ω_{pe} , selected such that the mother wave attains its highest field strength. The backscatter wave intensity remains 1 order of magnitude below that of the mother wave and does not exhibit a similar sharp spectral peak. This is consistent with the less pronounced maximum of the low-frequency power spectrum (Fig. 2d) and suggests the Langmuir decay is broadband in nature with respect to the wave number. This property and the significantly smaller power in the backscattered wave make a subsequent decay to produce a multiple spectral peak very unlikely.

If one assumes that the waves involved satisfy the standard dispersion relations for Langmuir waves and ion acoustic waves

$$\omega_L^2 = \omega_{pe}^2 + 3k_L^2 v_{the}^2, \quad \omega_s = k_s c_s \tag{4}$$

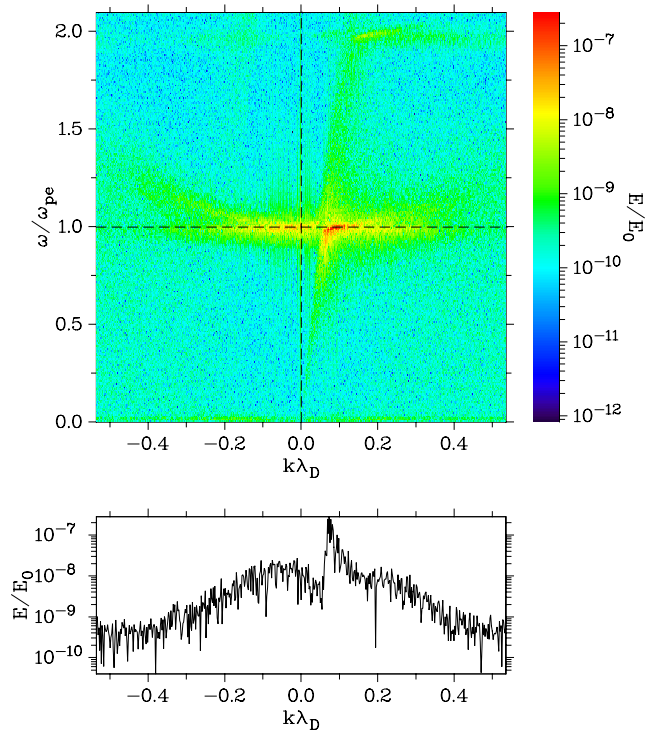


Figure 3. $\omega - k$ dispersion diagram for the longitudinal field within the time interval $0 < t < 750 \omega_{pe}^{-1}$ (top) and cut through the plot for the frequency $\omega/\omega_{pe} \approx 0.99$ for which the mother wave attains its maximum amplitude (bottom). Backscattered Langmuir waves appear for $k\lambda_D < 0$. Parameters as in Fig. 1.

with $c_s = [k_B(T_e + 3T_i)/m_i]^{1/2}$ the ion acoustic velocity, the resonance conditions for electrostatic decay $L \rightarrow L' + S$

$$\omega_L = \omega_{L'} + \omega_s, \quad k_L = k_{L'} + k_s \quad (5)$$

predict values

$$k_{L'} = -k_L + \frac{2}{3} \frac{c_s}{v_{the}\lambda_D}, \quad k_s = 2k_L - \frac{2}{3} \frac{c_s}{v_{the}\lambda_D} \quad (6)$$

with

$$k_L = \omega_{pe}/V_b \quad (7)$$

the beam-driven wave number.

One may extract $k_L\lambda_D \approx 0.075$ from the bottom panel of Fig. 3 which deviates from the value $k_L\lambda_D = 0.063$ resulting from Eqs. (4)–(7) for $V_b/v_{the} = 16$, $T_i/T_e = 0.73$. This discrepancy is not unexpected and can be attributed to the changes in the dispersion properties of Langmuir waves associated with the presence of the beam, particularly with the non-Maxwellian character of the electron distribution function due to the plateau formation. An indication of the beam-related change in the Langmuir wave dispersion is the fact that the frequency of the fastest growing mode is always below ω_{pe} , with a downshift that increases with beam

density. The choice of the frequency for the cut in Fig. 3 ($\omega/\omega_{pe} \approx 0.99$) reflects this shift. The wave number resonance condition can be satisfied with values from the ranges $-0.2 < k'_L\lambda_D < 0$ and $0.1 < k_s\lambda_D < 0.3$.

4 Generation of ion acoustic bursts

In the previous section evidence was given that Langmuir wave decay may proceed with some delay after the beam injection. In this section attention is drawn to a mechanism in which the high-frequency field affects heavy particles rather locally. This mechanism is based on the fact that the field energy may occasionally blow up to transient spiky events. The associated strong spatial gradients are the source of ponderomotive forces to which protons respond by the formation of isolated bursty regions of low-frequency electrostatic perturbations. Such events are already seen in the proton density profile in Fig. 2.

To get the spatial distribution of the field intensity in the simulation box, one has to build the time average of the field square E^2 at each grid point over a wave period, i.e., over the time $\Delta t = 2\pi \omega_{pe}^{-1}$. This quantity is henceforth denoted by $\langle E^2 \rangle$.

Figure 4 presents profiles of $\langle E^2 \rangle$ and proton density for two subsequent times. Notable features seen in this figure are the spatial correlation of the field intensity peaks at the earlier time $t = 300 \omega_{pe}^{-1}$ (a) and finite-amplitude proton density pulses at the later time $t = 800 \omega_{pe}^{-1}$ (b). For example, at positions $x/\lambda_D \approx 750, 1500, 2100$ the field energy peaks and the ion acoustic pulses synchronize. This strongly suggests that the latter are generated by the former. The spiky field events appear to be of transient nature, rarely lasting longer than some hundreds of ω_{pe}^{-1} . The low-frequency perturbations are supposed to propagate with ion sound speed ($c_s \approx 0.023 v_{the}$). That is, they do not move very much and may be considered as long-lived events on the timescale used here. Due to their different lifetimes the field peaks do in general not occur in coincidence with low-frequency bursts for longer time.

The detailed spatial shapes of proton density and bulk velocity, shown in the bottom panels, suggest the selected isolated event is a large-amplitude ion acoustic wave pulse with an extent of $\approx 25 \lambda_D$.

The signatures of low-frequency activity in the simulations are consistent with nonthermal, sporadic ion acoustic waves associated with bursty Langmuir waves in regions of type III solar radio sources, observed by Lin et al. (1986) and theoretically discussed by Robinson et al. (1993) and Cairns and Robinson (1995).

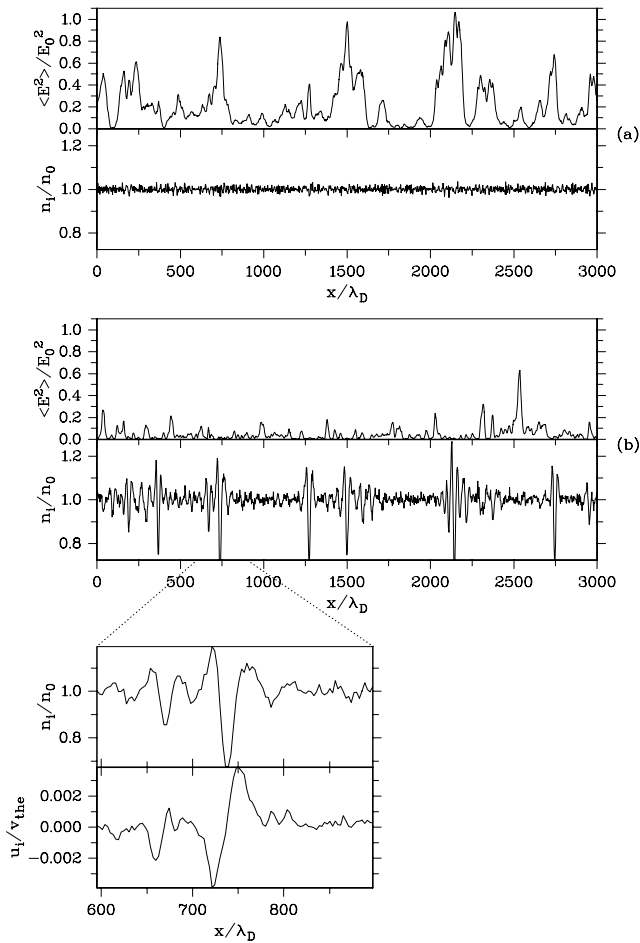


Figure 4. Spatial profiles of field energy and proton density at times $t = 300 \omega_{pe}^{-1}$ (a) and $t = 800 \omega_{pe}^{-1}$ (b), illustrating the formation and relaxation of spiky field events and the associated proton response. Bottom panels: spatial variation of proton density and bulk velocity of the ion acoustic pulse at $x/\lambda_D \approx 750$ in better resolution. Parameters as in Fig. 1.

5 Time variations

Figure 5 depicts the temporal variation of the longitudinal field at a fixed point ($x/\lambda_D = 1200$) in the simulation box (a), together with the power spectrum in panel (b). The initial growth phase within the interval $0 < t < 100 \omega_{pe}^{-1}$ is a result of the interaction of beam and background electrons only. Saturation is achieved by relaxation of the beam distribution to a plateau. Subsequently the system evolves randomly by linear interference of the amplified Langmuir waves. For example, the field drop, beginning at $t \sim 100 \omega_{pe}^{-1}$, is not typical and missing in time profiles at other positions. A common characteristic, however, is the longer period of enhanced field in which the low-frequency response takes place. As expected, the power spectrum exhibits a pronounced peak close to ω_{pe} . This peak comprises the frequencies of the beam-driven Langmuir waves, the backscattered daughter

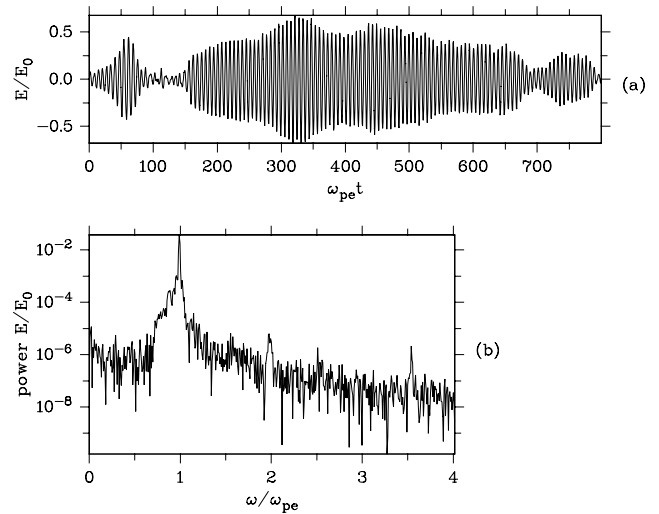


Figure 5. Time variation of the field at a fixed position $x/\lambda_D = 1200$ in the box (a) and corresponding power spectrum (b). Parameters as in Fig. 1.

waves and the $k = 0$ mode. Owing to the very small frequency difference between them, no multiple peak can be resolved. Spectral peaks at the harmonics of ω_{pe} have been commonly seen in previous simulations, the signal near the half-harmonic $3.5 \omega_{pe}$ is somewhat curious.

Unlike field and electron density the proton density varies on a much lower timescale. This is demonstrated in Fig. 6, which shows time profiles of the proton density at four equidistant positions within the simulation box. Each of them is Fourier analyzed, and the bottom panel presents the averaged low-frequency power spectrum with the frequency scaled by the proton plasma frequency. Most of the low-frequency power is seen for frequencies less than the ion plasma frequency, confirming that the proton dynamics is controlled by the ion acoustic mechanism.

As a consequence of the charge neutrality at the slow timescale, the time-averaged electron density is forced to match the proton density which is generally satisfied in the simulation.

Figure 7 illustrates the time history of the energy balance. It shows how the total energy content of the simulation box is distributed over background electrons, beam electrons, ions and the electrostatic field during the evolution of the beam plasma system. The beam energy rapidly turns down in the initial phase and is almost equally supplied to field energy and kinetic energy of background electrons. Ions play a minor role in the energy exchange. Note the limited period of enhanced field energy which lasts until $\sim 800 \omega_{pe}^{-1}$. The most intense fields, occasionally up to $2 E_0$, appear in the time period between $250 \omega_{pe}^{-1}$ and $500 \omega_{pe}^{-1}$. During this period Langmuir wave decay takes place and ion acoustic pulses are generated. Subsequently, the field energy is continuously converted into thermal energy of core electrons. This period is

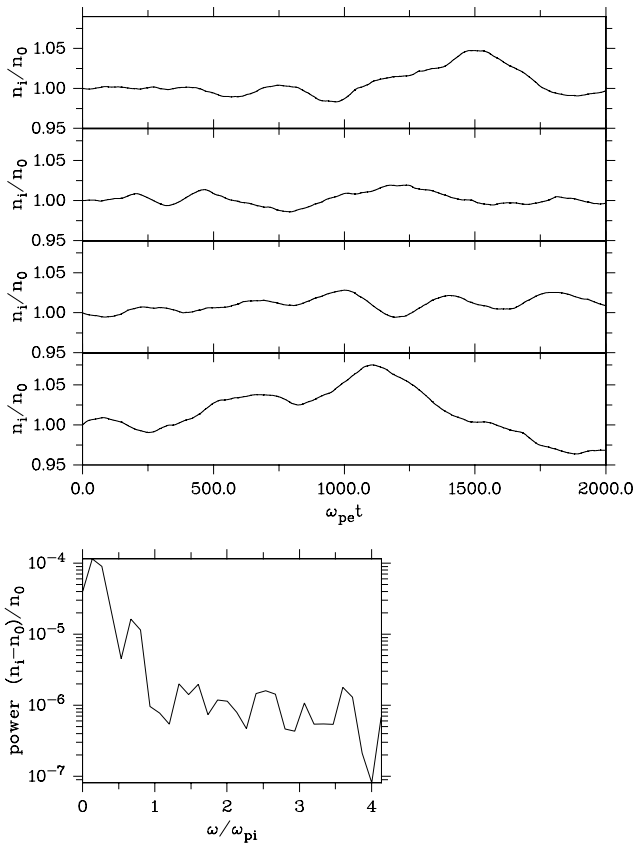


Figure 6. Time profiles of proton density at four positions $x/\lambda_D = 600, 1200, 1800, 2400$ within the box (top) and power spectrum averaged over the four profiles; frequency normalized by the ion plasma frequency ω_{pi} (bottom). Parameters as in Fig. 1.

accompanied by a loss of coherence. The wave packets seen in the early part of the evolution are disrupted, and the system approaches a phase of almost stationary energy partition with random spatial field fluctuations. A similar energy balance for an extremely low-energy beam was presented by Silin et al. (2007). The beam momentum is gradually transferred to the background electrons causing them to drift slowly in beam direction.

6 Dense beam effects

As mentioned in the introduction, not all of the frequency spectra of observed Langmuir amplitude time series are consistent with the decay scenario. In this section we present an alternative mechanism able to produce a spectral twin peak without decay. This mechanism, described earlier in the limit of rigid ions (Baumgärtel 2013), comes into play when a more dense beam ($n_b/n_0 \gtrsim 0.05$) penetrates the plasma. The frequency ω_L of the fastest growing mode is then downshifted and separated from ω_{pe} , the frequency of the $k = 0$ mode. Due to the higher beam density the latter becomes

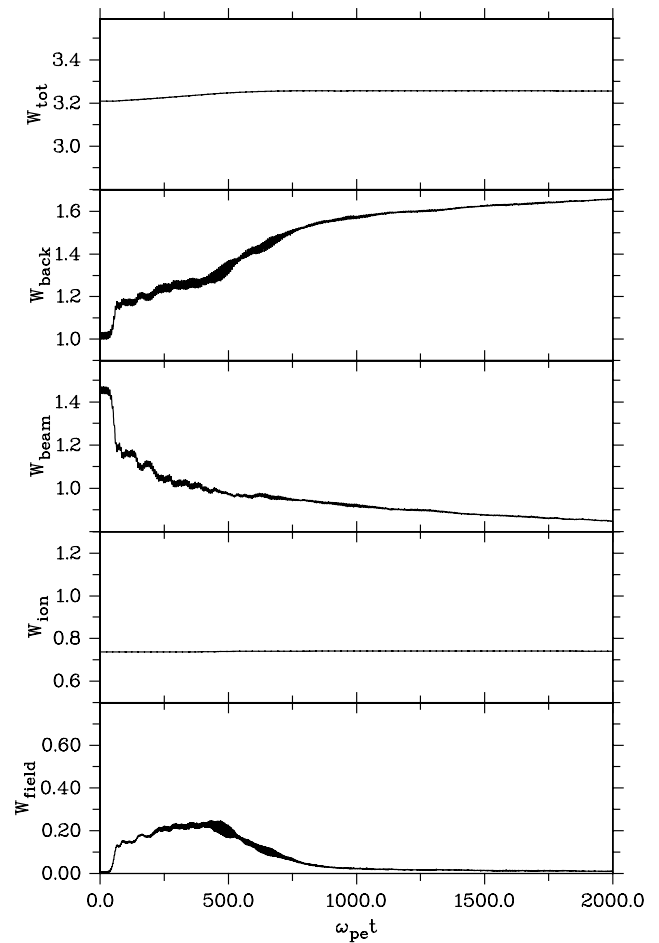


Figure 7. Distribution of the energy content W_{tot} of the simulation box over background electrons (W_{back}), beam electrons (W_{beam}), ions (W_{ion}) and the electrostatic field (W_{field}) as function of time. The energy is in units of the initial thermal energy of the background electrons. E_{tot} remains constant within $\sim 2\%$.

comparable in amplitude to the beam-driven Langmuir wave. That is, two high-frequency modes with slightly different frequencies are present at an early stage, able to produce a beat-type waveform. With respect to the ion dynamics, a different scenario is created. Langmuir wave decay is quenched, and the wave number of the excited low-frequency waves turns from $2k_L$ (for decay) to k_L , the wave number of the fastest growing Langmuir mode. Figure 8 illustrates such a situation showing results of a run with a beam of density $n_b/n_0 = 0.05$ and beam velocity $V_b/v_{the} = 8$. The proton density clearly peaks near k_L . This can be explained in terms of the spatial shape of the beat waves. If one of the two interfering waves is a $k = 0$ mode (as plasma oscillations), the spatial variation of the beat wave is determined by the wave number of the second mode.

Note that the spectral double peak here is the result of a linear interaction. That is, this process does not need a threshold field strength to occur and may be seen with weak fields

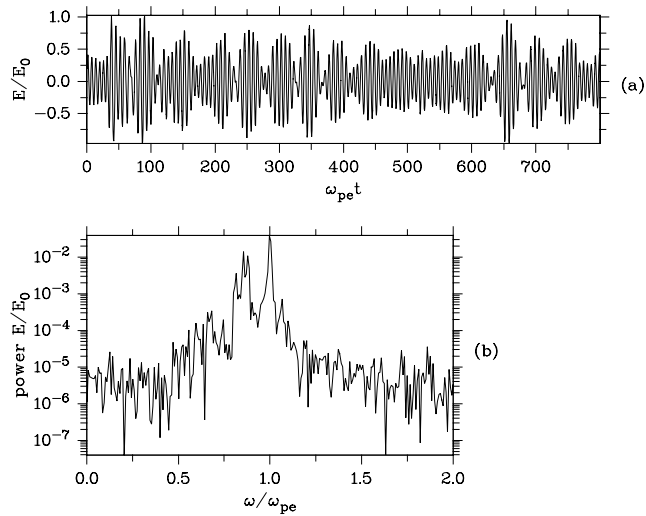


Figure 8. Beat-type waveform generated by a dense beam $n_b/n_0 = 0.05$ at position $x/\lambda_D = 2400$ in the box (a), and corresponding power spectrum (b) with two distinct peaks. Beam velocity $V_b = 8 v_{the}$.

and negligible ion response. It could thus be a candidate to explain the observation of beat-type waveforms without ion acoustic signatures (Sigsbee et al., 2010, their Fig. 3c). Figure 9 illustrates the spatial behavior of field and proton density in a way similar to Fig. 1.

A direct comparison between simulations with and without the presence of beam-driven plasma oscillations, i.e., with and without an initial current, was made by Baumgärtel (2013) in the limit of immobile ions.

7 Discussion

The simulation replaces in a certain sense an observation under rigorously idealized conditions, such as one-dimensional geometry, a uniform region for the beam–plasma interaction and the electrostatic approach. A handicap of a simulation experiment is that spectral peaks are not always suitable for comparison with a real observation because of frequency changes due to Doppler shift. Another weakness concerns the unrealistically high field strengths produced in the simulation which exceed considerably the observed ones. For a real space plasma embedded in a magnetic field, the one-dimensional geometry, the restriction to purely longitudinal waves and the assumption of both a uniform background plasma and a uniform beam may be not a good approximation. Thus the field intensities in the simulation should rather be considered as an upper limit of what might be reached under realistic conditions.

In addition, the electrostatic approximation prevents the model from describing Langmuir-like waves with complex polarization, e.g., Langmuir/ z -modes in weakly magnetized

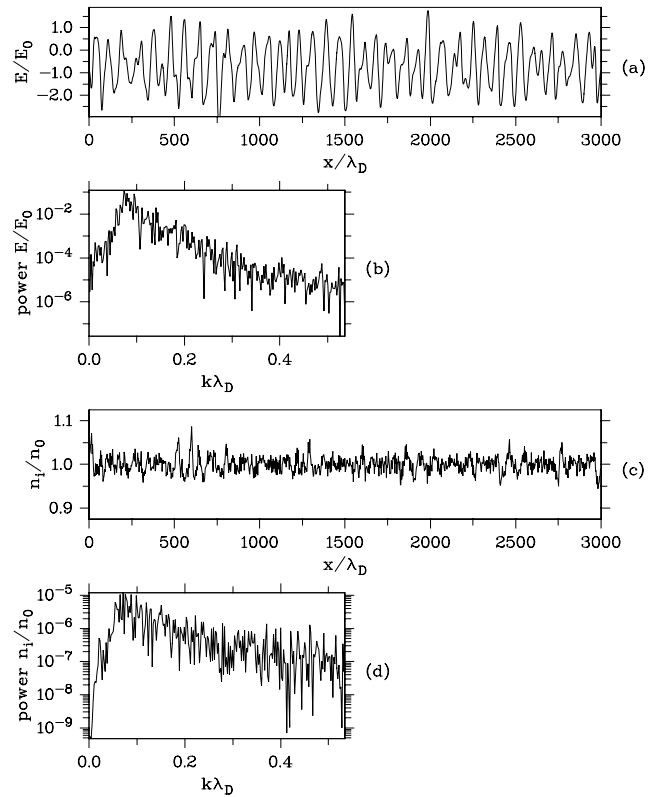


Figure 9. The same as Fig. 1 but for a dense beam; $n_b/n_0 = 0.05$, $V_b = 16 v_{the}$. The low-frequency power spectrum (d) peaks at the wave number of the mother wave.

plasmas, which appear with strong transverse field components for high beam velocities and small wave numbers. Recently observed waveforms with multiple spectral peaks were interpreted in terms of these waves (Malaspina et al., 2011; Graham and Cairns, 2013a; Kellog et al., 2013; Layden et al., 2013).

An advantage of simulations, on the other hand, is that, unlike one-point observations in space plasmas, spatial structures of field and density can be inspected and examined. Evidence for Langmuir wave decay came about by the analysis of spatial structures of field and proton density, the signatures of which were consistent with the wave number resonance conditions.

The presented results pertain mainly to the parameter set listed in Table 1, but a series of runs with other parameter combinations have been carried out. Since according to Eq. (7) the wave number of the fastest growing Langmuir mode is inversely proportional to V_b , increasing (decreasing) beam velocity results in extended (reduced) characteristic spatial scales, e.g., the width of the wave packets. A less energetic beam with $V_b/v_{the} = 8$ and $n_b/n_0 = 0.0057$ appears too weak for decay to proceed. It produces a broadband proton density power spectrum without decay signatures. A very fast and thin beam with 2 times the standard speed ($V_b/v_{the} = 32$,

i.e., $V_b/c \approx 0.14$, $n_b/n_0 = 0.001$) turned out to produce a field/ion density pattern similar to that of the standard case, including decay.

A crucial parameter for the onset of nonlinear processes such as decay or generation of ion acoustic perturbations is the initial ratio $W_{\text{beam}}/W_{\text{back}}$ of beam energy to kinetic energy of background electrons, which controls the saturation level of the field intensity. It takes the value 1.47 for the standard parameters and 0.37 in the weak beam case where decay is missing. This suggests a threshold value on the order of 1.

The evolution of the beam plasma system appears to be insensitive to the ion-to-electron temperature ratio, as runs in the range $0.1 < T_i/T_e < 1$ indicate. The same is true for the beam temperature. Simulation results do not change when the warm beam ($v_{\text{thb}} = v_{\text{the}}$) is replaced by a cold one.

The longitudinal field calculated from the current Eq. (1) was repeatedly compared to the field resulting from the Poisson Eq. (2). There was always an excellent agreement. The relatively small amount of numerical effort required by the implicit PIC algorithm used here is at the cost of the energy conservation which is not exactly ensured. The total energy (field + electrons + protons) is conserved during runs until $2000 \omega_{\text{pe}}^{-1}$ typically by $\sim 2\%$. The final electron velocity distribution shows a plateau with small slope but no high-energy tail.

Since both beam energy and beam momentum are continuously transferred to the background electrons, the electrostatic 1-D simulations suggest that the beam is eventually completely absorbed.

8 Summary

In this paper the self-consistent evolution of an electron beam–plasma system including ions is investigated by particle-in-cell (PIC) simulations using a one-dimensional electrostatic standard particle code with periodic boundary conditions. Initial conditions are set up by background electrons and protons at rest – thus allowing an initial current due to the beam. The initial growth of Langmuir waves is according to the classical electron beam instability without participation of protons. Saturation is achieved by rapid relaxation of the beam velocity distribution to a plateau, accompanied by a loss of beam energy. A wave packet structure develops as a result of linear interference of waves that have grown from noise. In case of sufficiently intense fields, nonlinear processes including ion response such as Langmuir wave decay can occur. Spatial profiles of field and proton density are inspected, and it was found that for low-density beams the wave numbers of the forward and backward propagating Langmuir waves and ion sound modes match the resonance conditions for decay. In time representation, Langmuir wave decay cannot be seen in the plasma frame owing to the very low frequency difference between beam–driven waves and backscattered waves.

With growing time the wave envelope undergoes significant variations and may become disrupted. Spiky field events can transiently occur with strong local increase of field intensity. Heavy particles respond to the associated ponderomotive forces by generation of ion acoustic bursts. Due to the different space/time variation of field energy spikes and low-frequency bursts, there is in general no coincidence between them for longer time.

For dense beams where the frequency of the fastest growing mode is downshifted from ω_{pe} , beam-aligned plasma oscillations ($k = 0$) come into play and establish early in the course of the instability the presence of two high-frequency waves of comparable amplitude and slightly different frequency, resulting in a beat wave structure. The corresponding spectral double peak is visible in the plasma frame. The most power of the low-frequency fluctuations is then concentrated near to the wave number of the dominant Langmuir wave instead of 2 times this value as for decay.

For nonlinear effects and ion response to become important in the beam–plasma interaction, the simulations suggest a ratio of beam energy to thermal energy of core electrons no less than 1.

The simulation confirms that the beam–plasma system goes through several characteristic phases on its way to a state without net energy exchange between particles and field.

Cases with repeatedly occurring decay resulting in multiple distinct spectral peaks as described by Graham and Cairns (2013a) could not be reproduced in the simulations, probably as consequence of the electrostatic limit. Waveforms of Langmuir eigenmodes in density cavities as observed and theoretically explained by Ergun et al. (2008) and Graham and Cairns (2013b) were not a target of the simulations.

Acknowledgements. The author wishes to acknowledge useful discussions with K. Sauer.

Topical Editor E. Roussos thanks two anonymous referees for their help in evaluating this paper.

References

- Akimoto, K., Omura, Y., and Natsumoto, H.: Rapid generation of Langmuir wave packets during electron beam–plasma instabilities, *Phys. Plasmas*, 3, 2559–2563, 1996.
- Bale, S. D., Burgess, D., Kellogg, P. I., Goetz, K., Howard, R. L., and Monson, S. J.: Phase coupling in Langmuir wave packets: Possible evidence of three–wave interactions in the upstream solar wind, *Geophys. Res. Lett.*, 23, 109–112, 1996.
- Baumgärtel, K.: Coherent amplitude modulation of electron-beam-driven Langmuir waves, *Ann. Geophys.*, 31, 633–638, doi:10.5194/angeo-31-633-2013, 2013.
- Cairns, I. H. and Melrose, D. B.: A theory for the 2p radiation upstream of Earth's bow shock, *J. Geophys. Res.*, 90, 6637–6640, 1985.

- Cairns, I. H. and Robinson, P. A.: Ion acoustic wave frequencies and onset times during type II solar radio bursts, *Astrophys. J.*, 453, 959–972, 1995.
- Daldorff, L. K. S., Pecseli, H. L., Trulsen, J. K., Ulriksen, M. I., Eliasson, B., and Stenflo, L.: Nonlinear beam generated plasma waves as a source for enhanced plasma and ion acoustic lines, *Phys. Plasmas*, 18, 052107, doi:10.1063/1.3582084, 2011.
- Ergun, R. E., Malaspina, D. M., Cairns, I. H., Goldman, M. V., Newman, D. L., Robinson, P. A., Ericsson, S., Bougeret, J. L., Briand, C., Bale, S. D., Cattell, C. A., Kellogg, P. J., and Kaiser, M. L.: Eigenmode structure in solar–wind Langmuir waves, *Phys. Rev. Lett.*, 101, 051101, doi:10.1103/PhysRevLett.101.051101, 2008.
- Graham, D. B. and Cairns, I. H.: Electrostatic decay of Langmuir/z–mode waves in type III solar radio bursts, *J. Geophys. Res.*, 118, 3968–3984, doi:10.1002/jgra.50402, 2013a.
- Graham, D. B. and Cairns, I. H.: Constraints on the formation and structure of Langmuir eigenmodes in the solar wind, *Phys. Rev. Lett.*, 111, 121101, doi:10.1103/PhysRevLett.111.121101, 2013b.
- Gurnett, D. A., Maggs, J. E., Gallagher, D. L., Kuhrt, W. S., and Scarf, F. L.: Parametric interaction and spatial collapse of beam–driven Langmuir waves in the solar wind, *J. Geophys. Res.*, 86, 8833–8841, 1981.
- Gurnett, D. A., Hospodarsky, G. B., Kurth, W. S., Williams, D. J., and Bolton, S. J.: Fine structure of Langmuir waves produced by a solar electron event, *J. Geophys. Res.*, 98, 5631–5637, 1993.
- Hospodarsky, G. R., Gurnett, D. A., Kurth, S. W., Kivelson, M. G., Strangeway, R. J., and Bolton, S. J.: Fine structure of Langmuir waves observed upstream of the bow shock at Venus, *J. Geophys. Res.*, 99, 13363–13371, 1994.
- Hospodarsky, G. R. and Gurnett, D. A.: Beat–type Langmuir wave emissions associated with a type III solar radio burst: Evidence of parametric decay, *Geophys. Res. Lett.*, 22, 1161–1164, 1995.
- Kellogg, P. I., Monson, S. J., Goetz, K., Howard, R., Bougeret, J. L., and Kaiser, M. L.: Early wind observations of bow shock and foreshock waves, *Geophys. Res. Lett.*, 23, 1243–1246, 1996.
- Kellogg, P. I., Goetz, K., Monson, S. J., and Opitz, A.: Observations of transverse Z mode and parametric decay in the solar wind, *J. Geophys. Res.*, A118, 4766–4775, 2013.
- Kojima, H., Furuya, H., Usui, H., and Matsumoto, H.: Modulated electron plasma waves observed in the tail lobe: Geotail waveform observations, *Geophys. Res. Lett.*, 24, 3049–3052, 1997.
- Langdon, A. B.: Implicit plasma simulations, *Space Sci. Rev.*, 42, 67–83, 1985.
- Layden, A., Cairns, I. H., Li, B., and Robinson, P. A.: Electrostatic decay in a weakly magnetized plasma, *Phys. Rev. Lett.*, 110, 185001, doi:10.1103/PhysRevLett.110.185001, 2013.
- Lin, R. P., Levedahl, W. K., Lotko, W., Gurnett, D. A., and Scarf, F. L.: Evidence for nonlinear wave–wave interactions in solar type III radio bursts, *Astrophys. J.*, 308, 954–965, 1986.
- Malaspina, D. M., Cairns, I. H., and Ergun, R. E.: Dependence of Langmuir wave polarization on electron beam speed in type II solar radio bursts, *Geophys. Res. Lett.*, 38, L13101, doi:10.1029/2011GL047642, 2011.
- Matsukiyo, S., Treumann, R. A., and Scholer, M.: Coherent waveforms in the auroral upward current region, *J. Geophys. Res.*, 109, A06212, doi:10.1029/2004JA010477, 2004.
- Muschietti, L., Roth, I., and Ergun, R. E.: On the formation of wave packets in planetary foreshocks, *J. Geophys. Res.*, 101, 15605–15613, 1996.
- Omura, Y., Matsumoto, H., Miyake, T., and Kojima, H.: Electron beam instabilities as generation mechanism of electrostatic solitary waves in the magnetotail, *J. Geophys. Res.*, 101, 2685–2697, 1996.
- Pottelette, R., Ergun, R. E., Treumann, R. A., Berthomier, M., Carlson, C. W., McFadden, J. P., and Roth, I.: Modulated electron–acoustic waves in auroral density cavities: Fast observations, *Geophys. Res. Lett.*, 26, 2629–2632, 1999.
- Robinson, P. A., Willes, A. J., and Cairns, I. H.: Dynamics of Langmuir and ion–sound waves in type III solar radio sources, *Astrophys. J.*, 408, 720–734, 1993.
- Sauer, K. and Sydora, R.: Mode crossing effects at electron beam–plasma interaction and related phenomena, *Plasma Phys. Control. Fusion*, 54, 124054, doi:10.1088/0741-3335/54/12/124045, 2012.
- Sigsbee, K., Kletzing, C. A., Pickett, J. S., Gurnett, D. A., Schwartz, S. J., Levevre, B., Lucek, E., Fazakerley, A. N., and Kucharek, H.: Characteristics of Langmuir electric field waveforms and power spectra exhibiting nonlinear behavior in Earth’s foreshock, *J. Geophys. Res.*, 115, A10251, doi:10.1029/2009JA014948, 2010.
- Silin, I., Sydora, R., and Sauer, K.: Electron beam–plasma interaction: Linear theory and Vlasov–Poisson simulations, *Phys. Plasmas*, 14, 012106, doi:10.1063/1.2430518, 2007.
- Stasiewicz, K., Holback, B., Krasnoselskikh, V., Boehm, M., Boström, R., and Kintner, P. M.: Parametric instabilities of Langmuir waves observed by Freija, *J. Geophys. Res.*, 101, 21515–21525, 1996.
- Thejappa, G., MacDowall, R. J., and Bergamo, M.: Evidence for four- and three-wave interactions in solar type III radio emissions, *Ann. Geophys.*, 31, 1417–1428, doi:10.5194/angeo-31-1417-2013, 2013.
- Umeda, T.: Vlasov simulation of amplitude modulated Langmuir waves, *Phys. Plasmas*, 13, 092304, doi:10.1063/1.2348088, 2006.
- Umeda, T.: Vlasov simulation of Langmuir wave packets, *Nonlin. Processes Geophys.*, 14, 671–679, doi:10.5194/npg-14-671-2007, 2007.
- Umeda, T. and Ito, T.: Vlasov simulation of Langmuir decay instability, *Phys. Plasmas*, 15, 084503, doi:10.1063/1.2965494, 2008.
- Usui, H., Furuya, H., Kojima, H., Matsumoto, H., and Omura, Y.: Computer experiments of amplitude–modulated Langmuir waves: Application to Geotail observation, *J. Geophys. Res.*, 110, A06203, doi:10.1029/2004JA010703, 2005.