

# Models of field-aligned currents needful to simulate the substorm variations of the electric field and other parameters observed by EISCAT

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**Abstract.** We have used the global numerical model of the coupled ionosphere-thermosphere-protonosphere system to simulate the electric-field, ion- and electron-temperature and -concentration variations observed by EISCAT during the substorm event of 25 March 1987. In our previous studies we adopted the model input data for field-aligned currents and precipitating electron fluxes to obtain an agreement between observed and modelled ionospheric variations. Now, we have calculated the field-aligned currents needful to simulate the substorm variations of the electric field and other parameters observed by EISCAT. The calculations of the field-aligned currents have been performed by means of numerical integration of the time-dependent continuity equation for the cold magnetospheric electrons. This equation was added to the system of the modelling equations including the equation for the electric-field potential to be solved jointly. In this case the inputs of the model are the spatial and time variations of the electric-field potential at the polar-cap boundaries and those of the cold magnetospheric electron concentration which have been adopted to obtain the agreement between the observed and modelled ionospheric variations for the substorm event of 25 March 1987. By this means it has been found that during the active phase of the substorm the current wedge is formed. It is connected with the region of the decreased cold magnetospheric electron content travelling westwards with a velocity of about  $1 \text{ km s}^{-1}$  at ionospheric levels.

sphere-protonosphere system (Namgaladze *et al.*, 1988, 1991) has been used to calculate the variations in electric field and ion and electron temperature and concentration for the quiet day of 24 March 1987 and disturbed day of 25 March. The model input data for field-aligned currents and precipitating electron fluxes have been selected to obtain an acceptable agreement between variations observed by EISCAT (Collis and Häggström, 1989, 1991) and those from the ionospheric modes. The best agreement has been achieved when the field-aligned currents of the substorm current wedge were added to the region-1 and 2-field-aligned currents during an active phase of a substorm.

The three-dimensional current system, named the substorm current wedge, has been suggested and discussed by many authors (e.g. Bonnevier *et al.*, 1970; McPherron *et al.*, 1973; Kamide *et al.*, 1976; Rothwell *et al.*, 1984; Rostoker and Eastman, 1987; Kan *et al.*, 1988, 1992; Kan, 1993). It consists of the field-aligned currents flowing out of the ionosphere at the pre-midnight sector and flowing in at the post-midnight sector closed by the horizontal ionospheric currents and magnetospheric currents perpendicular to the geomagnetic field. In Namgaladze *et al.* (1996) the spatial and time variations of such a field-aligned current system were not calculated but selected to obtain the best fit to the electric-field variations observed by EISCAT.

In the present paper an attempt is made to calculate the field-aligned currents of region 2 and those of the substorm current wedge for the same event of 25 March 1987 rather than selecting them. In this case the field-aligned currents are transferred from the category of input parameters for the model to the category of calculated parameters. Simultaneously, new input parameters, namely electric-field potential at the polar-cap boundaries and equivalent magnetospheric conductivity, are introduced and variations of these parameters are selected to obtain the best agreement between EISCAT-observed and modelled ionospheric variations. In this way we attempt to answer the question: what magnetospheric conductivity variations can be responsible for the formation of the

## 1 Introduction

The behaviour of the high-latitude ionosphere during an isolated substorm observed on 25 March 1987 has been simulated numerically by Namgaladze *et al.* (1996). The global numerical model of the Earth's thermosphere-ionosphere-protonosphere system (Namgaladze *et al.*, 1988, 1991) has been used to calculate the variations in electric field and ion and electron temperature and concentration for the quiet day of 24 March 1987 and disturbed day of 25 March. The model input data for field-aligned currents and precipitating electron fluxes have been selected to obtain an acceptable agreement between variations observed by EISCAT (Collis and Häggström, 1989, 1991) and those from the ionospheric modes. The best agreement has been achieved when the field-aligned currents of the substorm current wedge were added to the region-1 and 2-field-aligned currents during an active phase of a substorm.

substorm current wedge and for the corresponding ionospheric variations of the electric field and electron and ion temperature and concentration? As it will be shown, the development of the current wedge during the substorm active phase can be related to the region of the decreased cold magnetospheric electron content travelling westwards with a velocity of about  $1 \text{ km s}^{-1}$  at ionospheric levels.

## 2 Formulation of the problem, basic equations

The model calculations of the variations in ionospheric electric field and electron and ion temperature and concentration for the substorm event of 25 March 1987 have been performed using the new version (Namgaladze *et al.*, 1995a) of the global numerical model of the Earth's thermosphere-ionosphere-protonosphere system (Namgaladze *et al.*, 1988, 1994) analogous to the calculations made by Namgaladze *et al.* (1996). The main difference is that now the field-aligned currents are not the input parameters for the model, but have been calculated by solving the time-dependent continuity equation for the cold magnetospheric plasma-sheet electrons integrated along the closed geomagnetic field lines:

$$j_p = -B_i \partial \Sigma_m / \partial t - R_E^{-2} \sin^{-1} \theta [(\partial \Sigma_m / \partial \theta)(\partial \varphi / \partial \lambda) - (\partial \Sigma_m / \partial \lambda)(\partial \varphi / \partial \theta)], \quad (1)$$

where  $j_p$  is the field-aligned current density defined to be positive for currents flowing out the ionosphere;  $B_i$  is the geomagnetic field at the base of the field line in the ionosphere ( $h = 175 \text{ km}$ );  $\Sigma_m = eN/B_i$  is the integrated pseudo-Hall magnetospheric conductivity;  $e$  is the electron charge;  $N = B_i \int (n/B) dl$ , where the integration is carried out along geomagnetic field lines from  $h = 175 \text{ km}$  up to the top of the field line,  $n$  is the concentration of the magnetospheric plasma-sheet electrons, and so  $N$  is half of the total plasma-sheet electron content in the field line tube;  $t$  is time;  $R_E$  is the Earth's radius;  $\theta$  is the geomagnetic colatitude,  $\lambda$  is the geomagnetic longitude measured from magnetic midnight to east;  $\varphi$  is the electric-field potential determined from the continuity equation for the ionospheric currents:

$$\nabla[\hat{\sigma}_i(\nabla\varphi - \mathbf{v} \times \mathbf{B}) - \mathbf{j}_p] = 0. \quad (2)$$

Here  $\hat{\sigma}_i$  is the ionospheric conductivity tensor,  $\mathbf{v}$  is the neutral wind velocity vector. Both are calculated in the model by solving the continuity and momentum equations for the neutral and charged particles.  $\mathbf{B}$  and  $\mathbf{j}_p$  are the vectors of the geomagnetic field and field-aligned current density, respectively.

Equation 1 is obtained from the time-dependent continuity equation for the magnetospheric plasma-sheet electrons under the following assumptions. The field-aligned currents are carried by the electrons; the magnetospheric plasma-sheet electrons are cold, i.e. their gradient and other drifts are neglected in comparison with the electromagnetic one; the electric field is potential. The geomagnetic field lines are electrically equipotential;  $n$  is constant along the geomagnetic field lines. For the stationary case

Eq. 1 has been obtained by Vasyliunas (1972) and Maltsev (1974). In our calculations the field-aligned currents are assumed to be flowing only at the closed dipole geomagnetic field lines up to the polar-cap boundary, along which the distribution of the electric-field potential is taken in the following form:

$$\varphi_b = [\varphi_c(t)/2] \sin \lambda, \quad (3)$$

where  $\varphi_c$  is the potential drop across the polar cap. Its variation during the growth phase of the substorm (1540–1640 UT) is taken as the linear increase from 20 to 80 kV. The variations of the precipitating electron fluxes are taken in the same form as in Namgaladze *et al.* (1996).

The integrated magnetospheric conductivity distribution during the quiet conditions till up to the moment of the beginning of the growth phase (1540 UT) is taken in the form:

$$\Sigma_{m0} = \Sigma_0 \exp[-(\theta - \theta_b)^2 / (\Delta\theta)^2], \quad \theta \geq \theta_b = 16^\circ, \quad (4)$$

where  $\theta_b$  is the geomagnetic colatitude of the polar-cap boundary,  $\Delta\theta = 10^\circ$ ,  $\Sigma_0 = 100 \text{ Sm}$ . During the growth phase of the substorm (1540–1640 UT), the polar-cap boundary moves linearly  $4^\circ$  equatorwards.

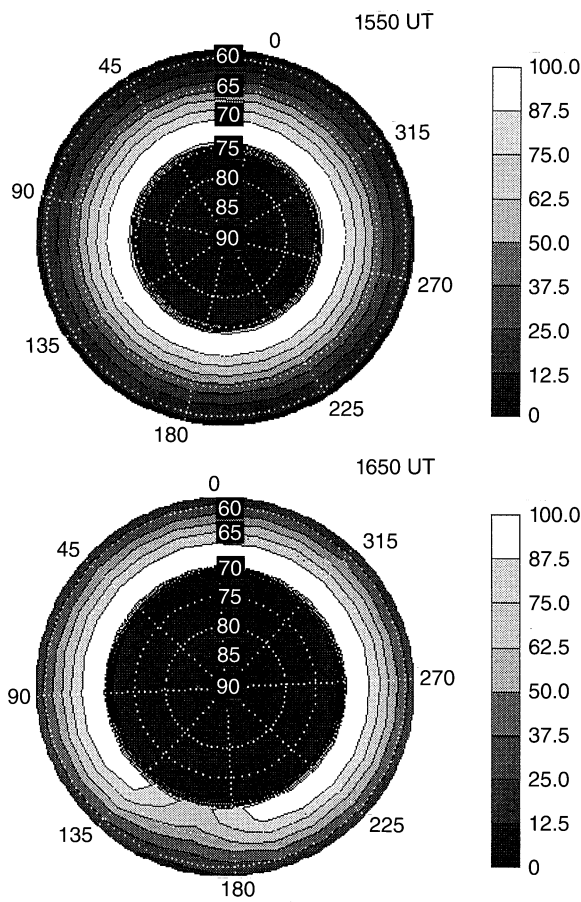
The expansion phase of the substorm continues for 20 min (1640–1700 UT). During this phase the integrated magnetospheric conductivity varies by the following means:

$$\Sigma_m = \Sigma_{m0} \{1 - 0.3 \exp[-(\lambda - \lambda_0(t))^2 / (\Delta\lambda)^2]\}, \quad (5)$$

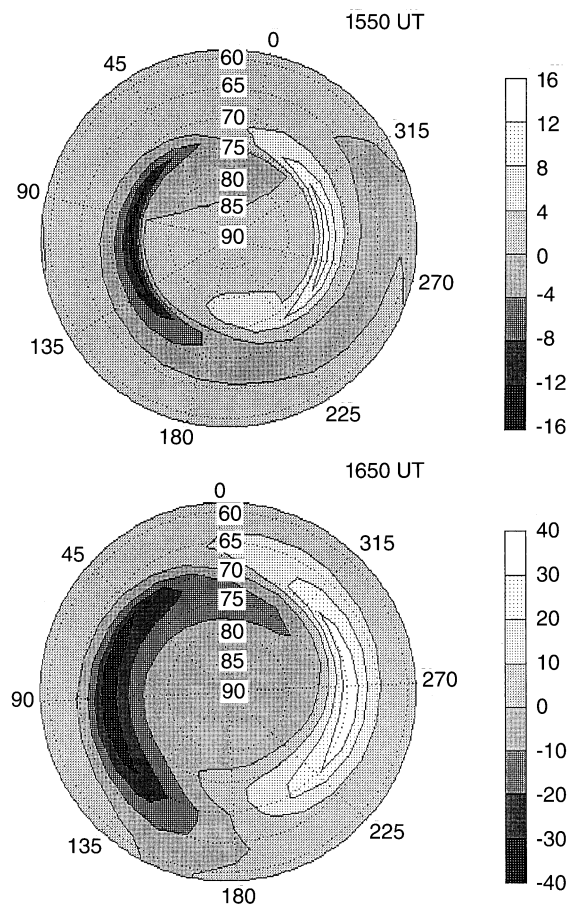
where  $\Delta\lambda = 23^\circ$  is the longitudinal half-width of the region of the decreased plasma-sheet electron content centred at the longitude  $\lambda_0$ . The centre of the region is moving westwards with a speed of  $1.2 \text{ km s}^{-1}$  at the ionosphere level. The maximum decrease in the plasma-sheet electron content, and correspondingly in the integrated magnetospheric conductivity, is 30%. Figure 1 shows the northern polar geomagnetic ( $\Phi, A$ ) plot of the integrated magnetospheric conductivity at 1550 UT (top panel) and 1650 UT (bottom panel).

During the recovery phase of the substorm (after 1700 UT), the distributions of the magnetospheric conductivity and electric-field potential at the polar-cap boundary recover to the undisturbed state exponentially, with the characteristic time of 1.5 h.

Equations 1 and 2 were solved numerically together with all other equations of the model, namely the continuity, momentum and heat balance equations for the main neutral gases ( $\text{N}_2$ ,  $\text{O}_2$ ,  $\text{O}$ ), molecular ( $\text{O}_2^+$  and  $\text{NO}^+$ ) and atomic ( $\text{O}^+$  and  $\text{H}^+$ ) ions, and electrons for the height range of 80 km up to  $15 R_E$  geocentric distance. The detailed description of the model equations can be found in Namgaladze *et al.* (1988). In our new version of this model (Namgaladze *et al.*, 1995a) we use the variable latitudinal steps of numerical integration. They vary from  $10^\circ$  for the thermospheric parameters and  $5^\circ$  for the ionospheric F2-region and protonosphere parameters at the equator to  $2^\circ$  at the auroral zones for all parameters. In Namgaladze *et al.* (1996) we used the empirical MSIS-86 (Hedin, 1987) thermospheric model to calculate the temperature and composition of the thermosphere. In the present paper all calculations are self-consistent. It means



**Fig. 1.** The north geomagnetic ( $\Phi, A$ ) polar plots of the integrated magnetospheric conductivity (Sm) at the growth phase (top) and at the expansion phase (bottom) of the substorm; the Sun position is at the top of the figure



**Fig. 2.** The geomagnetic ( $\Phi, A$ ) polar plots of the calculated electric-field potential (kV) in the northern high-latitude ionosphere at the growth phase (top) and at the expansion phase (bottom) of the substorm; the Sun position is at the top of the figure

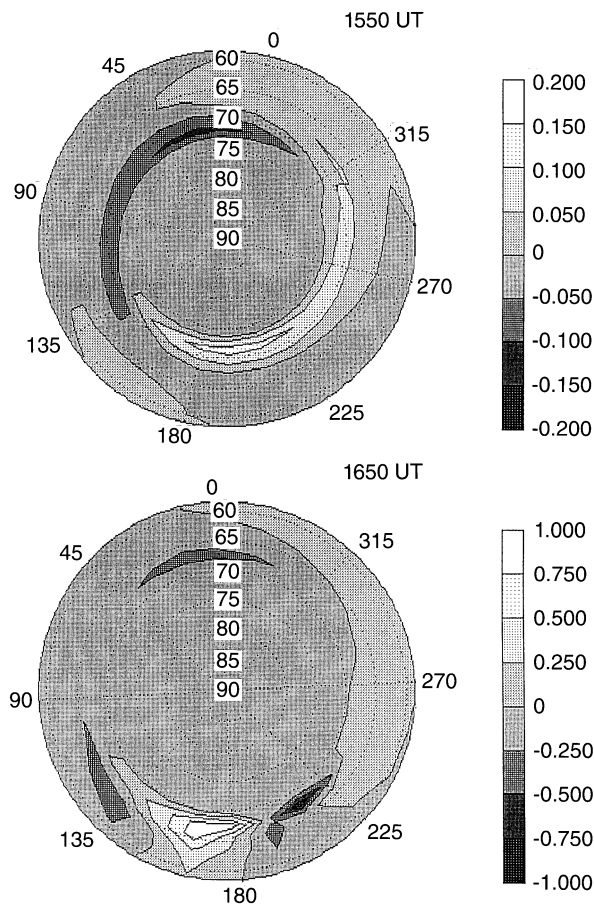
that the full system of the modelling equations for the neutral and charged particles is solved. The differences between the self-consistent solutions and those obtained by the use of the MSIS-86 model were discussed by Namgaladze *et al.* (1995b). These differences are significant for the calculated thermospheric wind disturbances but are not important for the calculated field-aligned current and electric-field variations discussed here.

### 3 The results of the model calculations

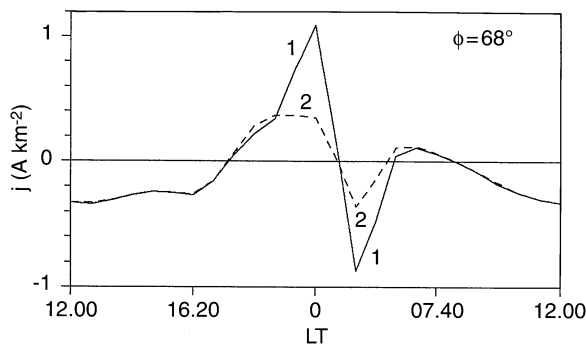
The calculated electric-field potential and field-aligned currents at the northern high-latitude ionosphere for the different phases of the substorm are shown in Figs. 2 and 3. The field-aligned currents of region 1 are distributed along the polar-cap boundary and are not shown in Fig. 3. During the quiet conditions and growth phase of the substorm, the calculated electric-field potential and field-aligned currents are consistent with the average statistical picture of these parameters for the weakly disturbed geomagnetic conditions (Heppner and Maynard, 1987; Iijima and Potemra, 1978). During the expansion phase of the substorm a pair of the field-aligned currents flowing out of and into the ionosphere (the substorm current

wedge) appears at the midnight sector. It is produced by the westward-travelling region of the decreased magnetospheric conductivity. The outflowing current is westward from the inflowing. The maximum density of the outflowing current is about  $1 \text{ A m}^{-2}$ . In the case when the region of the decreased magnetospheric conductivity is not travelling, the current-wedge field-aligned currents are generated by  $-\mathbf{V}_E \cdot \nabla N$  in magnetospheric plasma, where  $\mathbf{V}_E$  is  $\mathbf{E} \times \mathbf{B}$  plasma drift. Therefore they are generated at the eastern and western edges of the region of decreased plasma content as far as  $\mathbf{V}_E$  is eastward in the region of decreased plasma content. We can see that it is really so in the midnight sector in our calculations when comparing Figs. 1, 2 and 3 (bottom panels).

An influence of the westward travelling of the region of the decreased magnetospheric conductivity on the calculated field-aligned current density is illustrated in Fig. 4. It shows the longitudinal variations of the field-aligned current density along the geomagnetic latitude  $68^\circ$  calculated for the cases when the region of the decreased magnetospheric conductivity is travelling westwards and when it is motionless. In the last case the field-aligned current density is noticeably less than in the case of the travelling region. Correspondingly, the electric field in the midnight sector is decreased. The influence of the



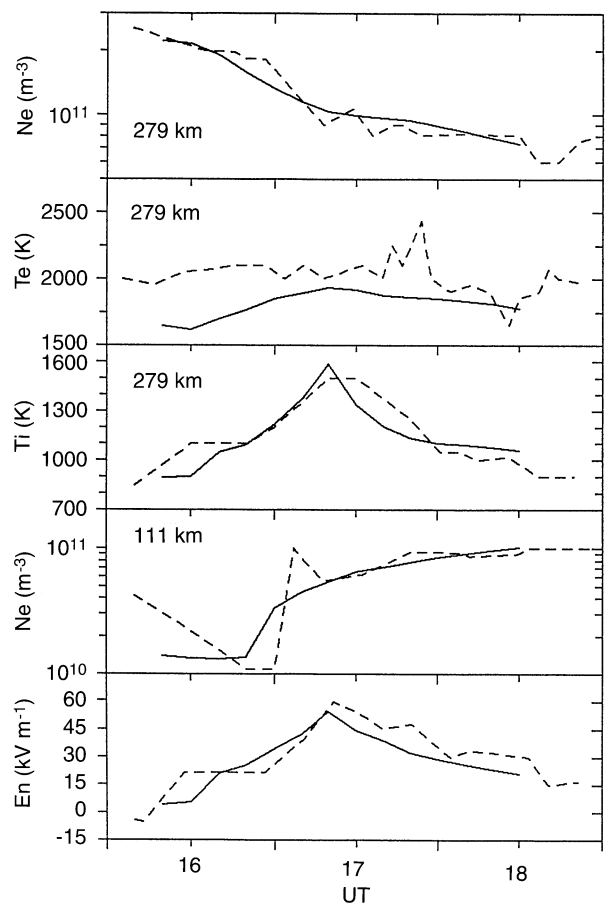
**Fig. 3.** The geomagnetic ( $\Phi, \Lambda$ ) polar plots of the calculated field-aligned current density ( $\text{A km}^{-2}$ ) in the northern high-latitude ionosphere at the growth phase (top) and at the expansion phase (bottom) of the substorm; the Sun position is at the top of the figure



**Fig. 4.** The calculated longitudinal variations of the field-aligned current density along the  $68^\circ$  geomagnetic latitude in the end of the substorm expansion phase for the cases: 1, the region of decreased magnetospheric conductivity is travelling westwards and 2, it is at rest

travelling speed  $V_{tr}$  of the decreased plasma content region on the current wedge field-aligned current generation is opposite that of  $V_E$ : the westward travelling of the “hole” acts as the eastward electromagnetic plasma drift.

The calculated time variations of the northward electric-field component, electron concentration at the heights



**Fig. 5.** The calculated variations (solid curves) and those observed by EISCAT on 25 March 1987 (dashed curves) in the northward electric field (bottom panel), E-region electron concentration at 111-km altitude and F2-region ion and electron temperature and electron concentration at 279-km altitude

111 and 279 km, and electron and ion temperature at the 279-km altitude over the EISCAT transmitter position are shown in Fig. 5 together with the variations of these parameters observed by EISCAT on 25 March 1987 (Collis and Häggström, 1989, 1991). As can be seen in this figure, the agreement between the observed and calculated variations is quite satisfactory.

#### 4 Discussion of the results

The presented results show that the behaviour of the electric field, electron concentration and electron and ion temperature observed by EISCAT during the isolated substorm on 25 March 1987 can be satisfactorily simulated in the numerical model calculations assuming the appearance of the westward-travelling region of the decreased plasma-sheet electron content during the expansion phase of the substorm. Due to the appearance of this region, the substorm current wedge is formed in accordance with the ideas of Bonnevier *et al.* (1970), McPherron *et al.* (1973), Kamide *et al.* (1976) and others, and with the observations of the field-aligned currents during the substorm expansion phase (Oppenoorth *et al.*, 1983; Lopez *et al.*, 1991; Hoffman *et al.*, 1994).

Opgenoorth *et al.* (1983) presented the results of the observations of the field-aligned currents at the western and eastern edges of the auroral surge. The field-aligned current flowing out of the ionosphere is connected with the westward-travelling bend of auroras at the western edge of the auroral surge. The speed of the travelling is about  $1\text{--}2\text{ km s}^{-1}$  at the ionosphere level. Baumjohann *et al.* (1991) presented the satellite observation data of plasma-sheet variations during the substorm expansion phase for 39 substorm events. In all these cases decreases in the central-plasma-sheet ion concentration of about 50% were observed simultaneously with temperature increases. These variations are apparently related with the geomagnetic-field-line reconnection processes leading to the plasma heating and the pushing out of the region of the heating. The conductivity of this region is decreased and a part of the transverse magnetospheric current is closed through the ionosphere forming the current wedge. The observations of the decreased magnetospheric plasma concentration by Baumjohann *et al.* (1991) are not direct evidence of the decreased plasma tube content. Nevertheless, we consider it is reasonable to assume that the variations in magnetospheric plasma concentration during the substorm expansion phase reflect the variations in plasma tube content. Due to the dipolarization of the geomagnetic field inside the current wedge (Kan *et al.*, 1992) the volume of the geomagnetic field tube should be decreased, and if the total plasma tube content is not decreased the plasma concentration should be increased, in contradiction with the observations by Baumjohann *et al.* (1991).

## 5 Conclusions

We have obtained the magnetospheric conductivity variations permitting us to simulate numerically the behaviour of the field-aligned currents, electric fields and high-latitude ionosphere parameters in agreement with the observations. During quiet geomagnetic conditions and at the substorm growth phase, the distribution of the field-aligned currents and electric-field potential in the high-latitude ionosphere corresponds to the magnetospheric conductivity model which is uniform in longitude and drops exponentially with latitude equatorward from the polar-cap boundary with the characteristic latitude scale of about the auroral-zone width.

During the substorm expansion phase a region of decreased (about 30% in comparison with a ground state) plasma-sheet electron content in the geomagnetic field tube appears at the midnight sector and travels westwards with a speed of about  $1\text{ km s}^{-1}$  at the ionosphere level, forming the substorm current wedge. An appearance of such a region of decreased magnetospheric conductivity agrees with the decreases in central-plasma-sheet ion concentration observed simultaneously with increases in their temperature during the substorm expansion phase (Baumjohann *et al.*, 1991).

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